



Pre-Algebra

Student Workbook

$$a + b = c$$

Adding Whole Numbers

EXAMPLE

Combine like places when adding.

$$\begin{array}{r} 1 \\ 47 \\ + 28 \\ \hline 75 \end{array}$$

Add the ones. Regroup.

$$\begin{array}{r} 1 \\ 17a \\ + 39a \\ \hline 56a \end{array}$$

Add the ones. Regroup.

$$\begin{array}{r} 1 \\ 47 \\ + 28 \\ \hline 75 \end{array}$$

Add the tens.

Check. $28 + 47 = 75$

$$\begin{array}{r} 1 \\ 17a \\ + 39a \\ \hline 56a \end{array}$$

Add the tens.

Check. $39a + 17a = 56a$

Directions Write each problem in vertical form. Then solve it by adding.

1. $32 + 28$

tens	ones

2. $23 + 49$

tens	ones

3. $297a + 39a$

hundreds	tens	ones	letters

4. $1,238x + 246x + 99x$

thousands	hundreds	tens	ones	letters

5. $943b + 644b + 86b$

thousands	hundreds	tens	ones	letters

Directions Add the following addends. Show how to check each problem.

6.

44
+ 17
<hr/>

Check

10.

$38b$
$467b$
+ $877b$
<hr/>

Check

13.

$1,412y$
$391y$
+ $2,744y$
<hr/>

Check

7.

91
+ 89
<hr/>

11.

$312a$
$29a$
+ $443a$
<hr/>

14.

27
4,281
+ 916
<hr/>

8.

$77x$
+ $139x$
<hr/>

12.

808
913
+ 97
<hr/>

15.

$2,491z$
$3,647z$
+ $244z$
<hr/>

Subtracting Whole Numbers

EXAMPLE

Sometimes when subtracting, you will need to rename.

To check a subtraction problem, use addition.

		Rename	Check
14	$17x$	$\overset{2}{\cancel{3}} \overset{14}{\cancel{4}}$	
$\underline{- 8}$	$\underline{- 12x}$	$\overset{-1}{1} \overset{6}{8}$	$\overset{18}{+ 16}$
$\underline{\quad 6}$	$\underline{\quad 5x}$	$\underline{\quad 1 \quad 8}$	$\underline{\quad 34}$

Directions Write each problem in vertical form. Then subtract.

1. $27 - 14$

5. $45c - 39c$

9. $750b - 243b$

2. $56 - 22$

6. $63 - 27$

10. $912c - 728c$

3. $84 - 31$

7. $144 - 28$

11. $1,874y - 678y$

4. $77y - 42y$

8. $233 - 118$

12. $3,135a - 2,679a$

Directions Subtract. Then show how to check each problem.

13. $\begin{array}{r} 37 \\ - 16 \\ \hline \end{array}$

Check

16. $\begin{array}{r} 325c \\ - 66c \\ \hline \end{array}$

Check

19. $\begin{array}{r} 3,131z \\ - 1,967z \\ \hline \end{array}$

Check

14. $\begin{array}{r} 142x \\ - 87x \\ \hline \end{array}$

17. $\begin{array}{r} 291y \\ - 36y \\ \hline \end{array}$

20. $\begin{array}{r} 5,416a \\ - 879a \\ \hline \end{array}$

15. $\begin{array}{r} 421 \\ - 277 \\ \hline \end{array}$

18. $\begin{array}{r} 1,044b \\ - 426b \\ \hline \end{array}$

Estimating Sums and Differences

EXAMPLE

Use an estimate to check whether a sum or a difference makes sense. To estimate, look at the numeral next to the greatest place value.

Round up if the numeral is 5 or more.	$\begin{array}{r} \downarrow \\ 59 \longrightarrow \\ \downarrow \\ 263 \longrightarrow \\ \downarrow \\ + 1,720 \longrightarrow \end{array}$	$\begin{array}{r} 60 \\ 300 \\ + 2,000 \\ \hline 2,360 \text{ estimate} \end{array}$
Round down if the numeral is less than 5.	$\begin{array}{r} \downarrow \\ 1,065 \longrightarrow \\ \downarrow \\ - 237 \longrightarrow \end{array}$	$\begin{array}{r} 1,000 \\ - 200 \\ \hline 800 \text{ estimate} \end{array}$

Directions Round each number to the greatest place value.

- | | | |
|----------------|----------------|-----------------|
| 1. 67 _____ | 6. 362 _____ | 11. 8,125 _____ |
| 2. 136 _____ | 7. 5,187 _____ | 12. 654 _____ |
| 3. 241 _____ | 8. 488 _____ | 13. 5,871 _____ |
| 4. 1,047 _____ | 9. 237 _____ | 14. 453 _____ |
| 5. 2,668 _____ | 10. 551 _____ | 15. 9,412 _____ |

Directions Estimate each sum. Use rounding. Then find the exact sum.

- | | | |
|----------------------------|------------------------------|------------------------------|
| 16. $64 + 87 =$
_____ | 18. $714 + 892 =$
_____ | 20. $3,821 + 451 =$
_____ |
| 17. $252 + 524 =$
_____ | 19. $1,561 + 243 =$
_____ | |

Directions Estimate each difference. Use rounding. Then find the exact difference.

- | | | |
|----------------------------|----------------------------|------------------------------|
| 21. $65 - 42 =$
_____ | 23. $852 - 361 =$
_____ | 25. $1,961 - 457 =$
_____ |
| 22. $431 - 297 =$
_____ | 24. $631 - 288 =$
_____ | |

Multiplying Whole Numbers

EXAMPLE

Sometimes when multiplying, you will need to rename.
When a letter is part of the answer, remember to include it in the answer.

$$\begin{array}{r} 2 \\ 27a \\ \times 64 \\ \hline 108 \end{array}$$

Multiply ones.
Rename.

$$\begin{array}{r} 4 \\ 27a \\ \times 64 \\ \hline 108 \end{array}$$

Multiply tens.
Rename.

$$\begin{array}{r} 27a \\ \times 64 \\ \hline 108 \end{array}$$

1,620
1,728a
Add.

Directions Multiply the following problems.

1. $4 \times 8 =$ _____

3. $9 \cdot 9 =$ _____

5. $(4)(3b) =$ _____

2. $(7)(9) =$ _____

4. $5a \cdot 6 =$ _____

6. $10y \times 4 =$ _____

Directions Multiply. Remember to rename.

7. $\begin{array}{r} 16 \\ \times 24 \\ \hline \end{array}$

9. $\begin{array}{r} 35x \\ \times 17 \\ \hline \end{array}$

11. $\begin{array}{r} 87z \\ \times 9 \\ \hline \end{array}$

8. $\begin{array}{r} 34 \\ \times 23 \\ \hline \end{array}$

10. $\begin{array}{r} 91 \\ \times 8x \\ \hline \end{array}$

12. $\begin{array}{r} 19c \\ \times 8 \\ \hline \end{array}$

Directions Write each problem in vertical form. Then multiply.

13. $28 \times 76y$

14. $19 \times 32z$

15. $81b \times 22$

Dividing Whole Numbers

EXAMPLE

When dividing, place the numbers correctly in each step.

To check an answer, use multiplication and add the remainder.

$$\begin{array}{r} 59 \text{ r}1 \\ 8 \overline{)473} \\ \underline{40} \\ 73 \\ \underline{72} \\ 1 \end{array}$$

Check

$$8 \times 59 + 1 = 473$$

Directions Divide these problems.

1. $45 \div 9 =$ _____

5. $36 \div 6 =$ _____

9. $10 \div 5 =$ _____

2. $16 \div 2 =$ _____

6. $9 \div 3 =$ _____

10. $33 \div 11 =$ _____

3. $27 \div 3 =$ _____

7. $18 \div 2 =$ _____

11. $48 \div 12 =$ _____

4. $14 \div 2 =$ _____

8. $72a \div 9 =$ _____

12. $54y \div 6 =$ _____

Directions Divide these problems.

13. $7 \overline{)434}$

16. $8 \overline{)272x}$

19. $9 \overline{)463}$

14. $4 \overline{)296}$

17. $3 \overline{)402a}$

20. $2 \overline{)365}$

15. $5 \overline{)625}$

18. $6 \overline{)528b}$

21. $8 \overline{)682}$

Directions Divide. Check your work.

Check

22. $18 \overline{)4,482}$

24. $61 \overline{)8,419}$

Check

23. $27 \overline{)2,457x}$

25. $43 \overline{)5,762a}$

Basic Operations

EXAMPLE

There are four basic operations.

addition $32 + 9 = 41$

multiplication $8 \times 7 = 56$

subtraction $44 - 20 = 24$

division $36 \div 4 = 9$

Directions Solve each problem.

1.
$$\begin{array}{r} 112a \\ + 9a \\ \hline \end{array}$$

6.
$$\begin{array}{r} 99 \\ - 47 \\ \hline \end{array}$$

11. $24 \overline{)192a}$

2. $75 \overline{)750}$

7. $74 \overline{)2,368b}$

12. $48 \overline{)96x}$

3. $16 \overline{)224x}$

8.
$$\begin{array}{r} 639 \\ + 124 \\ \hline \end{array}$$

13.
$$\begin{array}{r} 92x \\ + 12x \\ \hline \end{array}$$

4.
$$\begin{array}{r} 15 \\ \times 15 \\ \hline \end{array}$$

9.
$$\begin{array}{r} 34a \\ \times 22 \\ \hline \end{array}$$

14.
$$\begin{array}{r} 1,432b \\ + 3,698b \\ \hline \end{array}$$

5.
$$\begin{array}{r} 77a \\ - 76a \\ \hline \end{array}$$

10. $36 \overline{)936}$

15.
$$\begin{array}{r} 198 \\ - 163 \\ \hline \end{array}$$

Directions Use a calculator to solve each problem.

16. $112,342 - 9,479 =$

18. $206 \cdot 432 =$

20. $114,204 \div 62 =$

17. $6,048 \div 72 =$

19. $1,210 + 6,352 + 4,418 =$

Estimating Products and Quotients

EXAMPLE

To estimate a product, round to the greatest place value. Round up if 5 or more. Round down if less than 5.

$$23 \times 67 =$$

estimate $20 \times 70 = 1,400$

To estimate a quotient, use two numbers that form a basic division fact.

$$1,721 \div 61 =$$

$17 \div 6$ is not a basic fact.
 $18 \div 6$ is a basic fact.
 estimate $1,800 \div 60 = 300$

Directions Round. Estimate. Then find the exact product.

Problem	Rounded	Estimate	Exact Product
1. 63×24	_____	_____	_____
2. 85×36	_____	_____	_____
3. 17×42	_____	_____	_____
4. 44×75	_____	_____	_____
5. 59×14	_____	_____	_____
6. 32×55	_____	_____	_____
7. 73×64	_____	_____	_____
8. 27×83	_____	_____	_____

Directions Round. Estimate. Then find the exact quotient.

Problem	Rounded	Estimate	Exact Quotient
9. $534 \div 6$	_____	_____	_____
10. $736 \div 8$	_____	_____	_____
11. $1,380 \div 23$	_____	_____	_____
12. $2,862 \div 54$	_____	_____	_____
13. $6,290 \div 74$	_____	_____	_____
14. $4,758 \div 78$	_____	_____	_____
15. $11,613 \div 49$	_____	_____	_____

Arithmetic and Algebra

EXAMPLE**Four Basic Operations**

addition $21 + 7 = 28$

subtraction $16 - 4 = 12$

multiplication $8 \times 3 = 24$

division $18 \div 9 = 2$

True, False, and Open Statements

True $31 + 4 = 35$

False $27 - 4 = 12$

Open $45 + n = 51$

Directions Write the operation or operations used in each expression.

- | | | | |
|-----------------|-------|-----------------------|-------|
| 1. $6 + n$ | _____ | 6. $16 \cdot 18$ | _____ |
| 2. $48 \div b$ | _____ | 7. $3 \overline{)27}$ | _____ |
| 3. $3x$ | _____ | 8. $3x - 15$ | _____ |
| 4. $27 - y$ | _____ | 9. $74 + 6n$ | _____ |
| 5. $54n \div 9$ | _____ | 10. $6x + 17 - 8$ | _____ |

Directions Write *true* if the statement is true or *false* if it is false. Write *open* if the statement is neither true nor false.

- | | | | |
|-----------------------|-------|-----------------------|-------|
| 11. $13 + 8 = 21$ | _____ | 21. $6n = 36$ | _____ |
| 12. $48 - 12 = 36$ | _____ | 22. $12 \cdot 3 = 30$ | _____ |
| 13. $6 \times 9 = 48$ | _____ | 23. $n + 18 = 25$ | _____ |
| 14. $42 \div 7 = 7$ | _____ | 24. $64 - 23 = 41$ | _____ |
| 15. $83 + n = 92$ | _____ | 25. $12n = 144$ | _____ |
| 16. $5 \cdot 4 = 20$ | _____ | 26. $66 \div 11 = 6$ | _____ |
| 17. $21 \div 7 = 3$ | _____ | 27. $16 - 6 = 20$ | _____ |
| 18. $16 - b = 12$ | _____ | 28. $75 + 15 = 90$ | _____ |
| 19. $15 \div 4 = 5$ | _____ | 29. $n \div 8 = 2$ | _____ |
| 20. $126 + 10 = 116$ | _____ | 30. $6 \times 7 = 42$ | _____ |

Representing Numbers Using Letters

EXAMPLE

Numerical Expressions (only numbers are used)

$42 - 12$ 3×3

Algebraic Expressions (numbers and letters are used)

$2x + 6$ $7a \div 3$

Variables (letters) n in $7n + 4$

Operations (addition, subtraction, multiplication, division)

$6x + 4$ (multiplication and addition)

$(18 \div 3) - 8$ (division and subtraction)

Directions Write *numerical* or *algebraic* for each expression.

- | | | | |
|-----------------|-------|--------------------|-------|
| 1. $6x + 3$ | _____ | 6. $n + 19$ | _____ |
| 2. $24 - 16$ | _____ | 7. $64 \div 8 - 7$ | _____ |
| 3. $55 \div 11$ | _____ | 8. 63×8 | _____ |
| 4. $9x + 17$ | _____ | 9. $8b + 7b$ | _____ |
| 5. $128 + 76$ | _____ | 10. $17c \div 3$ | _____ |

Directions Identify the variable in each expression.

- | | | | |
|-----------------|-------|-----------------|-------|
| 11. $6x + 17$ | _____ | 16. $x - 83$ | _____ |
| 12. $8 \div 2b$ | _____ | 17. $4 + y$ | _____ |
| 13. $16y - 8$ | _____ | 18. $3m \div 5$ | _____ |
| 14. $k + 12$ | _____ | 19. $4x + 12$ | _____ |
| 15. $d \div 4$ | _____ | 20. $5d$ | _____ |

Directions List the operation or operations used in each expression.

- | | |
|-----------------------|-------|
| 21. $8y - 16$ | _____ |
| 22. 16×32 | _____ |
| 23. $32 + 6b$ | _____ |
| 24. $9 \cdot 17$ | _____ |
| 25. $(16 \div 8) - y$ | _____ |

Replacing Variables

EXAMPLE

This is how to evaluate whether an open statement is true or false.

Step 1 Substitute a number for the variable.

$$6 + x = 11 \quad \text{when } x = 5$$

$$6 + 5 = \square$$

$$8 - a = 6 \quad \text{when } a = 3$$

$$8 - 3 = \square$$

Step 2 Perform the operation.

$$6 + 5 = 11 \quad \text{is a true statement}$$

$$8 - 3 = 6 \quad \text{is a false statement}$$

Directions Read each statement. Substitute each given number for n .

Write whether the statement is *true* or *false* for the value of n .

Statement: $6n = 30$

1. $n = 3$ _____

2. $n = 6$ _____

3. $n = 5$ _____

Statement: $21 + n = 28$

7. $n = 4$ _____

8. $n = 16$ _____

9. $n = 7$ _____

Statement: $12 - n = 7$

4. $n = 10$ _____

5. $n = 5$ _____

6. $n = 7$ _____

Statement: $36 \div n = 4$

10. $n = 9$ _____

11. $n = 6$ _____

12. $n = 5$ _____

Directions Evaluate each expression.

13. $m + 17$ when m is 15 _____

14. $3x - 6$ when x is 3 _____

15. $18 \div g$ when g is 6 _____

16. $21 + 2c$ when c is 5 _____

17. $48 - g$ when g is 17 _____

18. $n \div 4$ when n is 24 _____

19. $8x$ when x is 8 _____

20. $27 - 3y$ when y is 3 _____

Place Value

EXAMPLE

165.8742

The digit 1 is in the hundreds place.

The digit 6 is in the tens place.

The digit 5 is in the ones place.

The digit 8 is in the tenths place.

The digit 7 is in the hundredths place.

The digit 4 is in the thousandths place.

The digit 2 is in the ten-thousandths place.

The value of the digit 6 is 60. The value of the digit 7 is 0.07.

0.7 = seven tenths 0.42 = forty-two hundredths

Directions Write each number in words.

1. 0.3 _____

2. 0.81 _____

3. 0.12 _____

4. 0.077 _____

5. 0.325 _____

Directions Write the number expressed by each phrase.

6. forty-two one-hundredths

7. seven tenths

8. two one-hundredths

9. thirty-three one-thousandths

10. twenty-five one-hundredths

Comparing and Rounding Decimals

EXAMPLE

Round 4.26 to the nearest tenth: 4.3
Round 8.241 to the nearest hundredth: 8.24
Round 2.7835 to the nearest thousandth: 2.784
Compare 6.8621 and 6.86.
Add two zeros to 6.86: 6.8600
6.8621 > 6.8600 6.8621 > 6.86

Directions Round each decimal to the nearest tenth.

1. 46.87 _____ 4. 2.098 _____
2. 108.21 _____ 5. 39.03 _____
3. 16.967 _____

Directions Round each decimal to the nearest hundredth.

6. 199.987 _____ 9. 77.8061 _____
7. 20.062 _____ 10. 10.7777 _____
8. 5.9927 _____

Directions Round each decimal to the nearest thousandth.

11. 13.4259 _____ 14. 12.6669 _____
12. 0.0571 _____ 15. 251.7032 _____
13. 399.1129 _____

Directions Compare each pair of decimals. Write < or >.

16. 17.092 17.09 _____ 21. 25.77 25.771 _____
17. 2.3 2.31 _____ 22. 0.8871 0.88711 _____
18. 937.328 937.32 _____ 23. 33.99 33.909 _____
19. 14.8276 14.82 _____ 24. 406.22 406.222 _____
20. 8.901 8.9017 _____ 25. 7.63954 7.639549 _____

Adding and Subtracting Decimals

EXAMPLE

To find the perimeter of a triangle, use the formula $P = a + b + c$ where a , b , and c are the lengths of the sides of the triangle.

Triangle A: $a = 4.23$ cm $b = 13.1$ cm $c = 10.012$ cm

To add or subtract decimals, add zeros where necessary and line up the decimal points.

$$\begin{array}{r} 4.230 \\ 13.100 \\ + 10.012 \\ \hline 27.342 \text{ cm} \end{array}$$

Directions The numbers below show the length of each side of a triangle. Find the perimeter of each triangle.

- | | |
|---------------------------------------|--|
| 1. 3.42 cm, 8.19 cm, 4.5 cm _____ | 6. 13.459 cm, 17.847 cm, 19.003 cm _____ |
| 2. 0.663 cm, 1.12 cm, 0.997 cm _____ | 7. 29.317 cm, 33.822 cm, 21.1 cm _____ |
| 3. 18.02 cm, 16.477 cm, 13.9 cm _____ | 8. 0.168 cm, 3.04 cm, 2.3 cm _____ |
| 4. 1.7 cm, 2.34 cm, 2.11 cm _____ | 9. 7.65 cm, 6.011 cm, 9.7 cm _____ |
| 5. 8.176 cm, 12.5 cm, 10.015 cm _____ | |

Directions Add or subtract the dollar amounts.

- | | |
|--------------------------------|-------------------------------|
| 10. $\$39.75 - \18.98 _____ | 14. $\$1.45 - \0.76 _____ |
| 11. $\$0.84 - \0.67 _____ | 15. $\$991.81 - \4.92 _____ |
| 12. $\$494.16 + \78.87 _____ | 16. $\$323.13 + \9.99 _____ |
| 13. $\$100.00 - \16.29 _____ | 17. $\$17.32 - \0.54 _____ |

Directions Solve the problems.

18. Jon and Brooke each planted a bean seed. Jon's plant grew to 9.967 cm. Brooke's plant grew to 13.14 cm. How much taller was Brooke's plant than Jon's? _____
19. Alana earned \$9.75 selling vegetables from her garden in June, \$62 in July, and \$109.25 in August. What were Alana's total earnings from her garden for the three months? _____
20. Julio rode his bicycle 32.097 miles on Saturday and 9.84 miles on Sunday. How many more miles did he ride on Saturday than on Sunday? _____

Multiplying Decimals by Powers of 10

EXAMPLE

$10^2 = 100 \quad 10^3 = 1,000 \quad 10^4 = 10,000$

$8.52 \times 100 = 852$

Move the decimal point two places to the right.

$5.37 \times 10^3 = 5,370$

Move the decimal point three places to the right.

Directions Rewrite each operation by replacing the power of 10 with its equivalent number. Then multiply.

45.6×10^3	$45.6 \times 1,000$	45,600
2.345×10^1	1. _____	2. _____
17.425×10^2	3. _____	4. _____
8.7×10^4	5. _____	6. _____
0.0651×10^5	7. _____	8. _____
643×10^2	9. _____	10. _____

Directions Rewrite each operation by writing the multiple of 10 as a power of 10. Then multiply.

12.8×100	12.8×10^2	1,280
$0.53219 \times 1,000$	11. _____	12. _____
44.22×10	13. _____	14. _____
$1.359 \times 10,000$	15. _____	16. _____
$39.71 \times 100,000$	17. _____	18. _____
0.07125×100	19. _____	20. _____

Multiplying Decimals

EXAMPLE

To find the circumference of a circle, use the formula $C = \pi d$.

C = circumference π = pi (about 3.14) d = diameter

Find the circumference of a circle with a diameter of 4.3 cm.

$$C = \pi \times 4.3$$

$$C = 3.14 \times 4.3$$

$$\begin{array}{r} 3.14 \\ \times 4.3 \\ \hline 942 \\ 1256 \\ \hline 13.502 \end{array}$$

$$C = 13.502 \text{ cm}$$

Directions Find the circumference of each circle with the diameter shown.
You may use your calculator.

1. $d = 7.2$ cm _____

6. $d = 0.53$ inches _____

2. $d = 2.9$ inches _____

7. $d = 64.3$ cm _____

3. $d = 14$ cm _____

8. $d = 29.1$ inches _____

4. $d = 18.12$ cm _____

9. $d = 13.37$ cm _____

5. $d = 5.67$ inches _____

10. $d = 3.693$ cm _____

Directions Multiply.

11. 4.36×7 _____

16. 8.13×23.22 _____

12. 9.11×4 _____

17. 90.17×3.21 _____

13. 5.46×3 _____

18. 4.305×0.216 _____

14. 12.07×3.2 _____

19. 77.12×9.332 _____

15. 2.8×7.1 _____

20. 81.51×3.67 _____

Dividing Decimals by Powers of 10

EXAMPLE

$$2.6 \div 100 = 0.026$$

Move the decimal point two places to the left.

$$643.50 \div 1,000 = 0.6435$$

Move the decimal point three places to the left.

Directions Complete the chart by dividing each number by the power of 10 shown.

	10^1	10^2	10^3	10^4
824.2	82.42	1.	0.8242	2.
61.49	3.	4.	5.	6.
0.267	7.	8.	9.	10.
3.195	11.	12.	13.	14.
0.53	15.	16.	17.	18.
184.75	19.	20.	21.	22.
7.08	23.	24.	25.	26.
14.85	27.	28.	29.	30.

Dividing Decimals

EXAMPLE

$$\begin{array}{r} 3.68 \\ 5 \overline{)18.40} \\ -15 \\ \hline 34 \\ -30 \\ \hline 40 \\ -40 \\ \hline 0 \end{array}$$

$$1.5 \overline{)9.75}$$

$$\begin{array}{r} 6.5 \\ 15 \overline{)97.5} \\ -90 \\ \hline 75 \\ -75 \\ \hline 0 \end{array}$$

Directions Divide.

1. $18.76 \div 4$ _____

6. $59.90 \div 5$ _____

2. $78.84 \div 8$ _____

7. $121.28 \div 32$ _____

3. $48.96 \div 3$ _____

8. $223.14 \div 6$ _____

4. $18.84 \div 12$ _____

9. $154.62 \div 9$ _____

5. $28.71 \div 9$ _____

10. $119.32 \div 4$ _____

Directions Divide. Round your answer to the nearest hundredth.
You may use your calculator.

11. $58.86 \div 0.6$ _____

16. $728.52 \div 1.2$ _____

12. $4.851 \div 0.3$ _____

17. $34.84 \div 0.04$ _____

13. $137.28 \div 5.2$ _____

18. $0.8665 \div 0.05$ _____

14. $35.87 \div 1.74$ _____

19. $75.12 \div 0.823$ _____

15. $155.52 \div 8.1$ _____

20. $385.14 \div 2.1$ _____

Using Decimals

1. Luis brought 12 pounds of aluminum cans to the recycling center. He received \$3.36. How much does the recycling center pay for each pound of aluminum? _____
2. The average temperature in Key West, Florida, is 77.7°F . The average temperature in International Falls, Minnesota, is 36.4°F . On average, how much warmer is it in Key West than in International Falls? _____
3. A small swimming pool holds 5,263 gallons of water. A bathtub holds 55.4 gallons of water. How many times would you have to fill the bathtub to use the amount of water it takes to fill the pool? _____
4. Sam earned \$5.75 for mowing the lawn, \$14.50 for delivering newspapers, and \$12.00 for washing windows last week. How much did he earn? _____
5. The George Washington Bridge is 1,066.8 m long. The Golden Gate Bridge is 213.4 m longer than the George Washington Bridge. How long is the Golden Gate Bridge? _____
6. Gina rode 496.24 miles on a bicycle trip. The trip took 9 days. What was the average number of miles Gina rode each day? Round your answer to the nearest tenth. _____
7. A recipe for fruit salad calls for 1.5 pounds of apples, 2 pounds of oranges, and 1.25 pounds of grapes. At the market, apples cost \$0.69 per pound, oranges cost \$0.79 per pound, and grapes cost \$0.86 per pound. How much will it cost to make the fruit salad? _____
8. Jim's grandparents sent him \$35.00 for his birthday. He bought a CD for \$12.99 and put \$15.00 in his savings account. How much did Jim have left? _____
9. Kay purchased 16 tomato plants for \$0.48 each. How much did she spend? _____
10. A camper hiked 41.7 kilometers on the first day, 21.2 kilometers on the second day, and 37.4 kilometers on the third day. How many more kilometers did the camper hike on the first two days than on the third day? _____

Decimals and Fractions

EXAMPLE

Write 0.25 as a fraction. 5 is in the hundredths place. The denominator is 100.

$$\frac{25}{100} = \frac{1}{4}$$

Write $\frac{29}{100}$ as a decimal. 0.29

Write $\frac{30}{50}$ as a decimal. $\frac{30}{50} = \frac{30 \times 2}{50 \times 2} = \frac{60}{100}$ $\frac{60}{100} = 0.60$

Directions Write the denominator that would be used to change each decimal to a fraction.

1. 0.7 _____

4. 0.1 _____

2. 0.21 _____

5. 0.119 _____

3. 0.03 _____

Directions Write each decimal as a fraction. Simplify.

6. 0.34 _____

11. 0.13 _____

7. 0.24 _____

12. 3.08 _____

8. 0.45 _____

13. 0.006 _____

9. 0.010 _____

14. 0.36 _____

10. 0.2 _____

15. 7.8 _____

Directions Write each fraction as a decimal.

16. $\frac{8}{25}$ _____

21. $3\frac{18}{25}$ _____

17. $\frac{3}{20}$ _____

22. $\frac{3}{8}$ _____

18. $1\frac{7}{50}$ _____

23. $7\frac{1}{5}$ _____

19. $\frac{29}{40}$ _____

24. $\frac{61}{100}$ _____

20. $\frac{13}{20}$ _____

25. $\frac{16}{25}$ _____

Repeating Decimals

EXAMPLE

To change degrees Fahrenheit to degrees Celsius, use the formula $C = \frac{5}{9}(F - 32)$.

45 degrees F = how many degrees Celsius?

$$C = \frac{5}{9}(45 - 32)$$

$$C = \frac{5}{9}(13)$$

$$C = \frac{65}{9}$$

$C = 7.2222$ To write a repeating decimal, write a bar over the repeating digits.

$$7.\overline{2}$$

You may round off a temperature to the nearest degree: 7°C

Directions Find the Celsius temperature for each Fahrenheit temperature.
Round each answer to the nearest whole degree.

1. $F = 24^{\circ}$ _____

6. $F = 76^{\circ}$ _____

2. $F = 109^{\circ}$ _____

7. $F = 42^{\circ}$ _____

3. $F = 84^{\circ}$ _____

8. $F = 164^{\circ}$ _____

4. $F = 68^{\circ}$ _____

9. $F = 52^{\circ}$ _____

5. $F = 32^{\circ}$ _____

10. $F = 90^{\circ}$ _____

Directions Write each fraction as a repeating decimal.

11. $\frac{2}{9}$ _____

16. $\frac{7}{9}$ _____

12. $\frac{8}{15}$ _____

17. $\frac{3}{11}$ _____

13. $\frac{5}{9}$ _____

18. $\frac{7}{12}$ _____

14. $\frac{1}{6}$ _____

19. $\frac{13}{18}$ _____

15. $\frac{4}{15}$ _____

20. $\frac{2}{11}$ _____

Renaming Percents to Decimals

EXAMPLE

$$5\% = 0.05$$

$$8\frac{1}{2}\% = .085$$

What is the interest for one year on a principal of \$600 at a rate of 7%?

$$I = p \times r \times t$$

$$I = 600 \times 0.07 \times 1$$

$$I = \$42.00$$

Directions Change each percent to a decimal.

1. 18% _____

2. 94% _____

3. 0.3% _____

4. $2\frac{3}{4}\%$ _____

5. 29% _____

6. 300% _____

7. 48% _____

8. 1.2% _____

9. 81% _____

10. 2% _____

Directions Find the interest each principal will earn. If necessary, round each answer to the nearest cent.

11. Principal: \$18,500
Rate: 9.75%
Time: 9 months

14. Principal: \$6,400
Rate: 5%
Time: 2 years

12. Principal: \$750
Rate: 6.75%
Time: 6 months

15. Principal: \$11,650
Rate: 7%
Time: 3 months

13. Principal: \$1,200
Rate: 5.75%
Time: 1 year

Evaluating Expressions with Decimals

EXAMPLEEvaluate $6.21n$ when $n = 3.2$

$$6.21 \times 3.2 = 19.872$$

Directions Evaluate each expression.

- $p - 8.02$ when $p = 62.35$ _____
- $n + 14.375$ when $n = 0.027$ _____
- $s \div 0.125$ when $s = 3$ _____
- $73.21a$ when $a = 1.19$ _____
- $9p + 16n$ when $p = 7.26$ and $n = 0.24$ _____

Directions Solve each problem.

- Lucia has n dollars. Kelly has \$12.81 more than Lucia. Write an algebraic expression for how much money Kelly has. Then evaluate the expression when $n = \$37.65$.

- Fox Hills has l number of lots with 4.2 acres in each lot. Forest Point has m number of lots with 5.6 acres in each lot. Write an algebraic expression showing how many acres are in Fox Hills and Forest Point combined. Then evaluate the expression when $l = 13$ and $m = 8$.

- Anthony has p dollars in his bank account. He spends \$42.95 on a sweater. Write an algebraic expression for how much Anthony will have left in the bank after he buys the sweater. Then evaluate the expression when $p = \$116.80$.

- Jim has n number of employees. His payroll totals \$4,503.04 per week. Write an algebraic expression for how much each employee is paid per week if all employees receive equal pay. Then evaluate the expression when $n = 8$.

- Martina sold l number of paintings. Each painting cost \$125.75. Write an algebraic expression for the total amount Martina made on her paintings. Then evaluate the expression when $l = 18$.

Divisibility Rules

EXAMPLE

A number that can be divided by a whole number with no remainder is said to be divisible. The symbol $|$ means divides.

$2|10$ is a true statement because 10 is divisible by 2 and there is no remainder.
 $10 \div 2 = 5$ (no remainder)

$2|17$ is a false statement because 17 is not divisible by 2 without leaving a remainder.
 $17 \div 2 = 8 \text{ r}1$

Directions Write *true* if the statement is true and *false* if the statement is false. Write a division equation to prove your answer.

1. $5|15$ _____
2. $4|36$ _____
3. $6|39$ _____
4. $8|40$ _____
5. $9|82$ _____
6. $6|46$ _____
7. $3|90$ _____
8. $5|85$ _____
9. $4|128$ _____
10. $8|374$ _____
11. $2|577$ _____
12. $4|634$ _____
13. $9|567$ _____
14. $7|473$ _____
15. $8|688$ _____

Prime and Composite Numbers

EXAMPLE

A prime number has two factors: 1 and itself

5 is a prime number. Its factors are 5 and 1. $5 \times 1 = 5$

A composite number has factors other than 1 and itself.

14 is a composite number. Its two factors are 7 and 2. $7 \times 2 = 14$

Directions Write the numbers in each pair in the correct column to show which number is a prime number and which number is a composite number.

	Prime	Composite		Prime	Composite
1. 3, 6			11. 7, 12		
2. 8, 17			12. 20, 37		
3. 27, 31			13. 38, 41		
4. 5, 12			14. 81, 89		
5. 13, 16			15. 67, 121		
6. 43, 50			16. 72, 79		
7. 20, 41			17. 177, 691		
8. 83, 106			18. 197, 221		
9. 125, 149			19. 109, 301		
10. 97, 221			20. 108, 239		

Directions Circle two factors for each composite number.

21. 18	2	5	8	9	26. 35	4	5	6	7
22. 21	3	5	7	8	27. 48	5	6	8	9
23. 15	3	4	5	6	28. 45	2	4	5	9
24. 24	4	5	6	9	29. 12	3	4	5	7
25. 32	3	4	6	8	30. 30	4	5	6	8

Greatest Common Divisor

EXAMPLE

To find the greatest common divisor (GCD) of two numbers, list all the factors.
The greatest common factor is the greatest common divisor.

(14, 21)	14:	1	2	7	14
	21:	1	3	7	21

7 is the greatest common divisor (GCD) of 14 and 21.

Directions Write the factors for each number. Then write the greatest common divisor (GCD).

	Factors	GCD
1. (9, 24)	9: _____ 24: _____	_____
2. (14, 28)	14: _____ 28: _____	_____
3. (8, 16)	8: _____ 16: _____	_____
4. (11, 77)	11: _____ 77: _____	_____
5. (4, 20)	4: _____ 20: _____	_____
6. (3x, 21)	3x: _____ 21: _____	_____
7. (8, 48y)	8: _____ 48y: _____	_____
8. (12x, 60x)	12x: _____ 60x: _____	_____
9. (7a, 42a)	7a: _____ 42a: _____	_____
10. (6c, 54c)	6c: _____ 54c: _____	_____

Factoring

EXAMPLE

Factor $6x + 8$.

Step 1 Find the greatest common divisor.

$$6x: \quad 1 \quad \textcircled{2} \quad 3 \quad 6 \quad x$$

$$8: \quad 1 \quad \textcircled{2} \quad 4 \quad 8$$

Step 2 Write the GCD outside parentheses. $2(\quad)$

Step 3 Use the distributive property in reverse. $2(3x + 4)$

Step 4 Check using the distributive property.

$$2(3x + 4) = (2 \cdot 3x) + (2 \cdot 4) = 6x + 8$$

Directions Circle the GCD for each expression.

1. $3x + 9$ 1 3 9

6. $30y + 36z$ 3 5 6

2. $12y + 18$ 2 3 6

7. $9d + 54e$ 3 6 9

3. $32b + 8$ 4 8 16

8. $3c + 7y$ 1 3 7

4. $44a + 4$ 2 4 11

9. $25d + 100c$ 4 5 25

5. $10z + 50b$ 2 5 10

10. $18x + 33y$ 3 6 11

Directions Use the distributive property to factor each expression.

11. $18x + 12$ _____

16. $54b + 9w$ _____

12. $6y + 8$ _____

17. $20m + 15k$ _____

13. $3c + 9$ _____

18. $12n + 4p$ _____

14. $6a + 15$ _____

19. $9q + 81c$ _____

15. $2h + 11$ _____

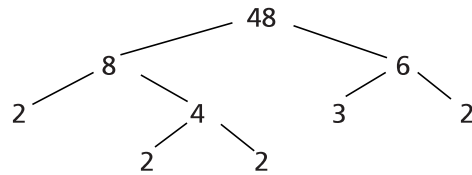
20. $ab + bc$ _____

Least Common Multiple

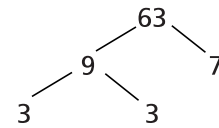
EXAMPLE

Find the least common multiple (LCM) of 48 and 63.

Step 1 Write the prime factorization of each number.



$2 \cdot 2 \cdot 2 \cdot 2 \cdot 3$ or $2^4 \cdot 3$
(prime factorization)



$3 \cdot 3 \cdot 7$ or $3^2 \cdot 7$
(prime factorization)

Step 2 Identify the greatest power of each prime factor.

The greatest power of the prime factor 2 is 2^4 .

The greatest power of the prime factor 3 is 3^2 .

The greatest power of the prime factor 7 is 7.

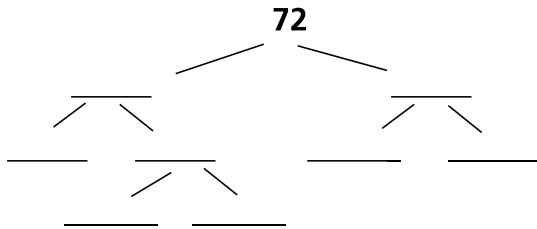
Step 3 Find the product.

$$2^4 \cdot 3^2 \cdot 7 = 16 \cdot 9 \cdot 7 = 1,008$$

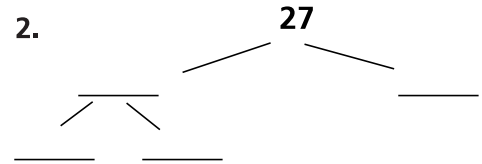
The LCM of 48 and 63 is 1,008.

Directions Complete each factor tree.

1.



2.



Directions Write the prime factorization for each factor tree above.

3. _____

4. _____

Directions Find each least common multiple (LCM).

5. LCM (4, 12) _____

9. LCM (10, 28) _____

6. LCM (5, 18) _____

10. LCM (21, 24) _____

7. LCM (30, 60) _____

8. LCM (16, 35) _____

Scientific Notation

EXAMPLE

To write large numbers using scientific notation, move the decimal to make a number between 1 and 10.

Count the number of places the decimal was moved.

$$65,000,000 = 6.5 \times 10^7$$

7 654 321 (number of places from the decimal point = 7)

$$0.658 = 6.58 \times 10^{-1} \text{ (number of places from the decimal point = 1)}$$

If the decimal is moved to the left, the exponent is positive. (10^7)

If the decimal is moved to the right, the exponent is negative. (10^{-1})

Directions To write the number in scientific notation: Write how many places each decimal must be moved. Write *left* or *right* to tell in which direction to move the decimal point.

Number	Places Moved	Direction	Scientific Notation
1. 325,000	_____	_____	_____
2. 27,800	_____	_____	_____
3. 105,000,000	_____	_____	_____
4. 0.653	_____	_____	_____
5. 0.0325	_____	_____	_____
6. 0.0000817	_____	_____	_____
7. 681,000,000,000	_____	_____	_____
8. 0.000000783	_____	_____	_____
9. 0.00001818	_____	_____	_____
10. 86,000,000,000	_____	_____	_____

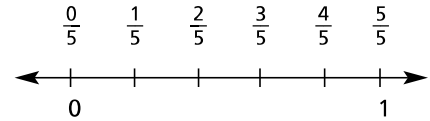
Directions Write the number that each example of scientific notation stands for.

- | | | | |
|------------------------|-------|---------------------------|-------|
| 11. 6.2×10^2 | _____ | 14. 7.15×10^{-1} | _____ |
| 12. 8.7×10^4 | _____ | 15. 3.84×10^{-2} | _____ |
| 13. 3.87×10^8 | _____ | | |

Proper Fractions

EXAMPLE

Which proper fractions are named by this number line?

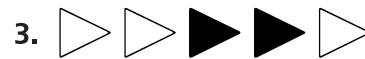


Step 1 Count the total number of marks between 0 and 1, including the mark at 1. This will tell you the denominator.

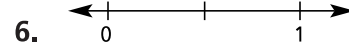
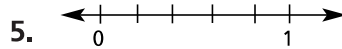
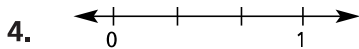
Step 2 Counting each mark away from 0 will tell you the numerator.

The following are proper fractions: $\frac{0}{5}$ $\frac{1}{5}$ $\frac{2}{5}$ $\frac{3}{5}$ $\frac{4}{5}$.

Directions Write the proper fraction that represents the shaded part of each whole or set.



Directions Which proper fractions are named by these number lines?



Directions Write a proper fraction to answer each question.

7. Julie has 15 new pencils. Eleven of them are primary colors. What part of the total number of pencils are primary colors? _____
8. Ed took a survey of students in his math class. Fifteen out of a total of twenty-one students have pets. What part of the total number of students have pets? _____
9. Twenty-three students in Mrs. Edwards' music class were also taking Spanish. Mrs. Edwards has a total of 27 students. What part of the total class was taking Spanish? _____
10. Isaac checked out eight books from the library. He read only three of them before he had to return them. What part of the whole number of books did he read? _____

Improper Fractions and Mixed Numbers

EXAMPLE

Express $\frac{11}{3}$ as a mixed number.

$$\frac{11}{3} = 11 \div 3 = 3 \overline{)11} \begin{array}{r} 3 \\ -9 \\ \hline 2 \end{array}$$

Write the remainder as a fraction: $\frac{11}{3} = 3\frac{2}{3}$

Directions Express each improper fraction as a mixed or whole number.

1. $\frac{8}{3}$ _____

9. $\frac{36}{6}$ _____

2. $\frac{9}{5}$ _____

10. $\frac{32}{10}$ _____

3. $\frac{10}{2}$ _____

11. $\frac{15}{4}$ _____

4. $\frac{21}{6}$ _____

12. $\frac{7}{7}$ _____

5. $\frac{11}{8}$ _____

13. $\frac{9}{2}$ _____

6. $\frac{25}{8}$ _____

14. $\frac{26}{19}$ _____

7. $\frac{32}{5}$ _____

15. $\frac{8}{7}$ _____

8. $\frac{12}{11}$ _____

Directions Express each number as an improper fraction.

16. $4\frac{2}{3}$ _____

24. $12\frac{3}{4}$ _____

17. $2\frac{5}{8}$ _____

25. $7\frac{1}{2}$ _____

18. $5\frac{1}{3}$ _____

26. $9\frac{3}{4}$ _____

19. $1\frac{9}{11}$ _____

27. $33\frac{1}{2}$ _____

20. $4\frac{2}{7}$ _____

28. $14\frac{1}{5}$ _____

21. $68\frac{1}{3}$ _____

29. $9\frac{9}{10}$ _____

22. $12\frac{1}{2}$ _____

30. $18\frac{4}{5}$ _____

23. $7\frac{7}{8}$ _____

Equivalent Fractions

EXAMPLE

Write an equivalent fraction for $\frac{2}{5}$.

Multiply the numerator and the denominator of $\frac{2}{5}$ by 3.

$$\frac{2}{5} \cdot \frac{3}{3} = \frac{6}{15}$$

Directions Write two equivalent fractions for each fraction.

1. $\frac{2}{3}$ _____

5. $\frac{2}{5}$ _____

9. $\frac{1}{2}$ _____

2. $\frac{3}{4}$ _____

6. $\frac{7}{10}$ _____

10. $\frac{3}{10}$ _____

3. $\frac{5}{6}$ _____

7. $\frac{2}{7}$ _____

4. $\frac{1}{16}$ _____

8. $\frac{5}{9}$ _____

EXAMPLE

Use a calculator to decide if $\frac{3}{8}$ and $\frac{9}{24}$ are equal.

For $\frac{3}{8}$: Press 3 \div 8 $=$. The display reads 0.375.

For $\frac{9}{24}$: Press 9 \div 24 $=$. The display reads 0.375.

Since the answers are the same, the fractions are equal.

If the answers are not the same, the fractions are not equivalent.

Directions Use your calculator to decide if the two fractions are equivalent.

Write *yes* or *no*.

11. $\frac{1}{2}$ and $\frac{15}{30}$ _____

19. $\frac{7}{8}$ and $\frac{28}{32}$ _____

12. $\frac{16}{35}$ and $\frac{8}{17}$ _____

20. $\frac{15}{30}$ and $\frac{5}{10}$ _____

13. $\frac{11}{12}$ and $\frac{33}{40}$ _____

21. $\frac{9}{15}$ and $\frac{6}{8}$ _____

14. $\frac{4}{20}$ and $\frac{1}{4}$ _____

22. $\frac{3}{21}$ and $\frac{2}{14}$ _____

15. $\frac{6}{7}$ and $\frac{30}{35}$ _____

23. $\frac{20}{30}$ and $\frac{4}{6}$ _____

16. $\frac{20}{55}$ and $\frac{2}{5}$ _____

24. $\frac{6}{12}$ and $\frac{9}{20}$ _____

17. $\frac{4}{5}$ and $\frac{8}{10}$ _____

25. $\frac{5}{8}$ and $\frac{15}{16}$ _____

18. $\frac{3}{4}$ and $\frac{2}{3}$ _____

Simplest Form

EXAMPLE

Find GCD (10, 15).

List all of the factors of each number and circle the common factors.

10: ① 2 ⑤ 10

15: ① 3 ⑤ 15

Choose the *greatest* common factor. GCD (10, 15) = 5

Directions Find the greatest common divisor (GCD) of each pair of numbers.

- | | | |
|------------------|-------------------|------------------|
| 1. (8, 24) _____ | 3. (14, 16) _____ | 5. (8, 10) _____ |
| 2. (5, 10) _____ | 4. (9, 12) _____ | |

Directions Express each fraction in simplest form.

- | | | |
|---------------------------|----------------------------|----------------------------|
| 6. $\frac{10}{15}$ _____ | 12. $\frac{8}{20}$ _____ | 18. $\frac{27}{54}$ _____ |
| 7. $\frac{16}{24}$ _____ | 13. $\frac{6}{9}$ _____ | 19. $\frac{16}{48}$ _____ |
| 8. $\frac{78}{90}$ _____ | 14. $\frac{18}{20}$ _____ | 20. $\frac{81}{108}$ _____ |
| 9. $\frac{10}{50}$ _____ | 15. $\frac{48}{60}$ _____ | 21. $\frac{60}{90}$ _____ |
| 10. $\frac{55}{66}$ _____ | 16. $\frac{20}{80}$ _____ | 22. $\frac{30}{65}$ _____ |
| 11. $\frac{12}{15}$ _____ | 17. $\frac{63}{108}$ _____ | |

Directions Solve the problems.

23. Shelly said she has $\frac{6}{8}$ of all the 1998 NFL collectors' cards. Mark said he has $\frac{9}{12}$ of them. Do they have the same number of cards? Explain.
- _____
24. Ashley said $\frac{3}{4}$ of her stuffed animals have button eyes. Pam said Ashley has 15 stuffed animals. Is it possible that Pam is correct? Explain.
- _____
25. Vince said his survey showed $\frac{2}{3}$ of his math class liked rap music. There are 24 students in the class. Is it possible that Vince's survey is correct? Explain.
- _____

Comparing and Ordering Fractions

EXAMPLE

Compare the fractions. Write $>$ or $<$.

$$\frac{4}{5} \text{ — } \frac{3}{4}$$

Step 1 Write equivalent fractions using the LCM.

$$\frac{4}{5} = \frac{16}{20}$$

$$\frac{3}{4} = \frac{12}{20}$$

Step 2 Compare $\frac{16}{20}$ and $\frac{12}{20}$. $\frac{16}{20}$ is greater than $\frac{12}{20}$. $\frac{4}{5} > \frac{3}{4}$

Directions Compare the fractions. Write $>$ or $<$.

1. $\frac{5}{8}$ — $\frac{1}{2}$

4. $\frac{4}{7}$ — $\frac{2}{5}$

7. $\frac{2}{3}$ — $\frac{5}{12}$

10. $4\frac{1}{2}$ — $5\frac{2}{3}$

2. $\frac{8}{9}$ — $\frac{2}{3}$

5. $\frac{1}{5}$ — $\frac{1}{3}$

8. $\frac{3}{16}$ — $\frac{1}{4}$

11. $6\frac{2}{5}$ — $6\frac{3}{10}$

3. $\frac{3}{4}$ — $\frac{4}{5}$

6. $\frac{6}{15}$ — $\frac{9}{15}$

9. $\frac{7}{8}$ — $\frac{3}{4}$

EXAMPLE

Order $\frac{2}{3}$, $\frac{1}{2}$, and $\frac{3}{4}$ from least to greatest.

Step 1 Write equivalent fractions using the LCM.

$$\frac{2}{3} = \frac{8}{12}$$

$$\frac{1}{2} = \frac{6}{12}$$

$$\frac{3}{4} = \frac{9}{12}$$

Step 2 Compare $\frac{8}{12}$, $\frac{6}{12}$, and $\frac{9}{12}$. $\frac{6}{12} < \frac{8}{12} < \frac{9}{12}$

Therefore, the order from least to greatest is $\frac{1}{2}$, $\frac{2}{3}$, $\frac{3}{4}$.

Directions Order from least to greatest.

12. $\frac{2}{3}$, $\frac{3}{8}$, $\frac{1}{2}$ _____

17. $\frac{7}{10}$, $\frac{3}{5}$, $\frac{17}{20}$ _____

13. $\frac{1}{2}$, $\frac{1}{3}$, $\frac{1}{4}$ _____

18. $\frac{5}{16}$, $\frac{9}{32}$, $\frac{1}{4}$ _____

14. $\frac{3}{4}$, $\frac{3}{5}$, $\frac{2}{3}$ _____

19. $\frac{3}{35}$, $\frac{3}{7}$, $\frac{3}{5}$ _____

15. $\frac{7}{8}$, $\frac{1}{2}$, $\frac{3}{4}$ _____

20. $\frac{3}{8}$, $\frac{5}{16}$, $\frac{1}{2}$ _____

16. $\frac{3}{16}$, $\frac{7}{8}$, $\frac{2}{3}$ _____

Fractions—Like Denominators

EXAMPLE

 Find $(1\frac{2}{3} + 2\frac{2}{3}) - 3\frac{1}{3}$
Step 1 Perform the computation inside the () first.

$$\begin{aligned} (1\frac{2}{3} + 2\frac{2}{3}) - 3\frac{1}{3} &= \\ 4\frac{1}{3} - 3\frac{1}{3} &= \end{aligned}$$

Step 2 Perform the remaining computation.

$$4\frac{1}{3} - 3\frac{1}{3} = 1$$

Directions Add or subtract. If necessary, perform the computation inside the () first. Write your answer in simplest form.

1. $\frac{3}{5} - \frac{2}{5}$ _____

2. $\frac{5}{6} + \frac{5}{6}$ _____

3. $\frac{9}{10} - \frac{7}{10}$ _____

4. $2\frac{15}{16} - 1\frac{7}{16}$ _____

5. $11\frac{11}{12} - 5\frac{9}{12}$ _____

6. $4\frac{3}{4} - 2\frac{1}{4}$ _____

7. $6\frac{7}{15} + 8\frac{14}{15}$ _____

8. $\frac{5x}{8} - \frac{3x}{8}$ _____

9. $\frac{9x}{10} - \frac{6x}{10}$ _____

10. $\frac{6}{y} + \frac{7}{y}$ _____

11. $\frac{4}{y} + \frac{x}{y}$ _____

12. $\frac{3x}{4} - \frac{x}{4}$ _____

13. $\frac{y}{16} + \frac{9y}{16}$ _____

14. $\frac{3y}{12} + \frac{5}{12}$ _____

15. $\frac{4x}{9} + \frac{10x}{9}$ _____

16. $(\frac{9}{10} + \frac{3}{10}) - \frac{4}{10}$ _____

17. $\frac{3}{8} + (\frac{7}{8} - \frac{4}{8})$ _____

18. $\frac{7}{16} - (\frac{1}{16} + \frac{3}{16})$ _____

19. $(\frac{8}{11} - \frac{5}{11}) + \frac{6}{11}$ _____

20. $\frac{11}{12} + (\frac{6}{12} - \frac{1}{12})$ _____

21. $\frac{4}{6} - (\frac{4}{6} - \frac{2}{6})$ _____

22. $\frac{3}{25} + (\frac{24}{25} - \frac{16}{25})$ _____

23. $(\frac{3x}{8} + \frac{9x}{8}) - \frac{5x}{8}$ _____

24. $\frac{2x}{3} + (\frac{2x}{3} - \frac{x}{3})$ _____

25. $\frac{3y}{12} + (\frac{9y}{12} - \frac{5y}{12})$ _____

Fractions—Unlike Denominators

EXAMPLE

 Add $6\frac{2}{3} + 3\frac{1}{2}$.

Step 1 Find the LCM of the denominators.

$$\text{LCM}(2, 3) = 6$$

Step 2 Write an equivalent mixed number for each fraction using the LCM.

$$\frac{2}{3} \cdot \frac{2}{2} = \frac{4}{6}$$

$$6\frac{2}{3} = 6\frac{4}{6}$$

$$\frac{1}{2} \cdot \frac{3}{3} = \frac{3}{6}$$

$$3\frac{1}{2} = 3\frac{3}{6}$$

Step 3 Add. $6\frac{4}{6} + 3\frac{3}{6} = 9\frac{7}{6}$
Step 4 Simplify. $9\frac{7}{6} = 10\frac{1}{6}$
Directions Add or subtract. Write your answer in simplest form.

1. $\frac{2}{3} + \frac{5}{6}$ _____

6. $\frac{19}{20} - \frac{3}{4}$ _____

2. $\frac{7}{8} - \frac{7}{16}$ _____

7. $\frac{5}{8} + \frac{5}{6}$ _____

3. $\frac{3}{4} + \frac{2}{3}$ _____

8. $\frac{4}{5} - \frac{2}{3}$ _____

4. $\frac{9}{10} - \frac{3}{4}$ _____

9. $\frac{15}{16} + \frac{1}{2}$ _____

5. $\frac{3}{5} - \frac{7}{45}$ _____

10. $\frac{11}{12} + \frac{3}{4}$ _____

Directions Add or subtract. Write your answer in simplest form.

11. $\frac{4x}{7} - \frac{x}{3}$ _____

14. $\frac{1}{2y} + \frac{5}{16y}$ _____

12. $\frac{1}{x} + \frac{4}{y}$ _____

15. $\frac{3x}{4} - \frac{2x}{3}$ _____

13. $\frac{5x}{12} + \frac{7x}{8}$ _____

Directions Add or subtract. Write your answer in simplest form.

16. $5\frac{7}{8} + 6\frac{3}{5}$ _____

21. $16\frac{5}{16} - 10\frac{7}{32}$ _____

17. $2\frac{3}{7} - 1\frac{1}{3}$ _____

22. $5\frac{5}{8} - 4\frac{2}{5}$ _____

18. $8\frac{9}{10} + 6\frac{1}{5}$ _____

23. $42\frac{5}{6} + 22\frac{7}{12}$ _____

19. $10\frac{3}{5} - 2\frac{3}{10}$ _____

24. $6\frac{3}{4}x + 2\frac{5}{8}x$ _____

20. $2\frac{7}{12} + 13\frac{3}{4}$ _____

25. $3\frac{4}{5}x - 2\frac{3}{10}x$ _____

Subtracting Fractions with Regrouping

EXAMPLE

Solve $4\frac{3}{8} - 2\frac{2}{3}$.

Step 1 Find the LCM of the denominators.
LCM (8, 3) = 24

Step 2 Write equivalent mixed numbers for $4\frac{3}{8}$ and $2\frac{2}{3}$ using the LCM (24) as denominators.

$$4\frac{3}{8} = 4\frac{9}{24} \qquad 2\frac{2}{3} = 2\frac{16}{24}$$

Step 3 Since $\frac{16}{24}$ cannot be subtracted from $\frac{9}{24}$, it must be renamed.

$$4\frac{9}{24} = 3\frac{33}{24} \quad (\text{Think: } 4\frac{9}{24} = 3\frac{9}{24} + \frac{24}{24} = 3\frac{33}{24})$$

Step 4 Subtract.

$$\begin{array}{r} 3\frac{33}{24} \\ - 2\frac{16}{24} \\ \hline 1\frac{17}{24} \end{array}$$

Directions Subtract. Write your answer in simplest form.

1. $2\frac{1}{3} - 1\frac{5}{8}$ _____ 5. $16\frac{1}{8} - 8\frac{3}{8}$ _____ 9. $8\frac{3}{8} - 5\frac{3}{4}$ _____

2. $6\frac{3}{4} - 2\frac{1}{2}$ _____ 6. $9\frac{3}{7} - 4\frac{6}{7}$ _____ 10. $4\frac{1}{3} - 1\frac{5}{6}$ _____

3. $4\frac{3}{10} - 3\frac{13}{15}$ _____ 7. $21\frac{9}{15} - 6\frac{14}{15}$ _____ 11. $12\frac{15}{16} - 4\frac{3}{4}$ _____

4. $6\frac{7}{10} - 4\frac{9}{10}$ _____ 8. $15\frac{3}{10} - 8\frac{1}{2}$ _____ 12. $32\frac{4}{9} - 17\frac{13}{18}$ _____

Directions Add or subtract.

13. Kerim jogged $3\frac{3}{4}$ miles on Thursday. On Friday, he jogged $\frac{2}{3}$ of a mile farther. How far did he jog on Friday? _____

14. Lejla caught a bass that was $1\frac{7}{8}$ pounds and a trout that was $3\frac{5}{8}$ pounds. How much heavier was the trout? _____

15. Mike studied $3\frac{1}{3}$ hours after school on Tuesday. On Wednesday, he studied $1\frac{3}{4}$ hours. How much longer did he study on Tuesday? _____

Multiplying Fractions and Mixed Numbers

EXAMPLE

Multiply $1\frac{2}{3} \cdot 2\frac{1}{2}$.

Step 1 Change the mixed numbers to improper fractions.

$$1\frac{2}{3} = \frac{5}{3} \qquad 2\frac{1}{2} = \frac{5}{2}$$

Step 2 Multiply the numerators and denominators.

$$\frac{5}{3} \cdot \frac{5}{2} = \frac{5 \cdot 5}{3 \cdot 2} = \frac{25}{6}$$

Step 3 Simplify. $\frac{25}{6} = 4\frac{1}{6}$

Directions Multiply. Write your answer in simplest form.

1. $\frac{1}{5} \cdot \frac{5}{6}$ _____

4. $\frac{5}{9} \cdot \frac{9}{10}$ _____

7. $\frac{2}{9} \cdot \frac{3}{4}$ _____

2. $\frac{3}{4} \cdot \frac{4}{5}$ _____

5. $\frac{6}{7} \cdot \frac{1}{2}$ _____

8. $\frac{19}{20}y \cdot \frac{5}{6}x$ _____

3. $\frac{3}{8} \cdot \frac{2}{3}$ _____

6. $\frac{3}{7} \cdot \frac{7}{12}$ _____

9. $\frac{4}{5} \cdot \frac{5}{8}y$ _____

Directions Multiply. Write your answer in simplest form.

10. $2\frac{3}{8} \cdot 1\frac{5}{19}$ _____

13. $4\frac{1}{2} \cdot 2\frac{1}{9}$ _____

16. $2\frac{5}{6} \cdot 3\frac{4}{17}a$ _____

11. $1\frac{3}{4} \cdot 1\frac{6}{7}$ _____

14. $5\frac{1}{3} \cdot 2\frac{2}{5}$ _____

17. $4\frac{4}{5}y \cdot 2\frac{7}{12}$ _____

12. $3\frac{1}{5} \cdot 1\frac{3}{16}$ _____

15. $3\frac{3}{4} \cdot 1\frac{3}{10}$ _____

18. $1\frac{2}{3}x \cdot 2\frac{7}{8}$ _____

Directions Multiply to solve each problem. Write your answer in simplest form.

19. Four-fifths of Mrs. Martinez's class likes the color purple, while $\frac{7}{8}$ of Mr. Burns's class likes the color. What fraction of both classes like purple?

20. Bobbie made a cake, which needed $4\frac{1}{3}$ cups of flour. Each cup weighs $8\frac{3}{4}$ ounces. How many ounces of flour did she use?

Dividing Fractions and Mixed Numbers

EXAMPLE

Divide $1\frac{1}{3} \div 2\frac{1}{3}$.

Step 1 Change each mixed number into an improper fraction.

$$1\frac{1}{3} = \frac{4}{3} \qquad 2\frac{1}{3} = \frac{7}{3}$$

Step 2 Multiply the dividend by the reciprocal of the divisor.

$$\frac{4}{3} \div \frac{7}{3} \text{ becomes } \frac{4}{3} \cdot \frac{3}{7}.$$

$$\frac{4}{3} \cdot \frac{3}{7} = \frac{12}{21}$$

Step 3 If possible, simplify. $\frac{12}{21} = \frac{4}{7}$

Directions Divide. Write your answer in simplest form.

1. $\frac{5}{8} \div \frac{5}{6}$ _____

4. $\frac{3}{8} \div \frac{3}{5}$ _____

7. $\frac{1}{3} \div \frac{3}{7}$ _____

2. $\frac{1}{5} \div \frac{3}{4}$ _____

5. $\frac{7}{8} \div \frac{1}{2}$ _____

8. $\frac{6}{11n} \div \frac{4}{11}$ _____

3. $\frac{7}{10} \div \frac{14}{15}$ _____

6. $\frac{9}{10} \div \frac{3}{8}$ _____

9. $\frac{15}{16} \div \frac{5}{8y}$ _____

Directions Divide. Write your answer in simplest form.

10. $2\frac{2}{5} \div 1\frac{3}{5}$ _____

13. $3\frac{1}{3} \div 1\frac{1}{3}$ _____

16. $2\frac{2}{3} \div 5\frac{1}{3}$ _____

11. $6\frac{5}{8} \div 2\frac{1}{2}$ _____

14. $1\frac{3}{4} \div 2\frac{1}{2}$ _____

17. $1\frac{2}{7} \div 3\frac{6}{7}j$ _____

12. $1\frac{2}{3} \div 1\frac{1}{4}$ _____

15. $4\frac{3}{8} \div 3\frac{1}{2}$ _____

18. $5\frac{3}{8}w \div 1\frac{19}{24}$ _____

Directions Solve each problem. If necessary, reduce to simplest form.

19. Kelvin has a log that is $15\frac{1}{3}$ feet long. He must cut it into pieces that each measure $\frac{1}{2}$ foot. How many pieces can he cut?

20. Melissa walked $12\frac{2}{3}$ miles in $2\frac{2}{3}$ hours. How many miles per hour did she walk?

Using Fractions

Directions Complete the chart.

- Sara surveyed 30 of her classmates for a civics project. In the group, $\frac{1}{2}$ said they watched TV for 2 hours every day. $\frac{1}{3}$ said they watched for 1 hour. $\frac{1}{15}$ said they watched for less than $\frac{1}{2}$ hour each day. The rest of the group said they did not watch television on a daily basis.

30 Classmates	How Many?
$\frac{1}{2}$ watch television 2 hours	_____
$\frac{1}{3}$ watch television 1 hour	_____
$\frac{1}{15}$ watch television $<\frac{1}{2}$ hour	_____
_____ do not watch daily	_____

Directions Solve each problem.

- Mike can walk a mile in $\frac{2}{3}$ of an hour. Dennis can walk a mile in $\frac{5}{8}$ of an hour. Who walks a mile faster? _____
- On Wednesday, Elaine told Sam she finished $\frac{7}{8}$ of her science project. Sam said he finished $\frac{15}{16}$. Who has finished more of the project? _____
- Kendra lives $\frac{6}{7}$ of a mile from the mall. Ali lives $\frac{5}{9}$ of a mile from the mall. Who lives closer to the mall? _____
- To go to the video store, Jennifer walks $2\frac{5}{8}$ blocks north and $4\frac{1}{2}$ blocks east. How many blocks does she walk to the video store? _____
- To build a birdhouse, Pat needs $16\frac{5}{8}$ inches of pine and $9\frac{2}{3}$ inches of cedar. How many more inches of pine does she need? _____
- Darlene walked for $2\frac{3}{8}$ hours at $3\frac{2}{3}$ miles per hour. How many miles did she walk? _____
- Grass seed costs \$3.50 ($3\frac{1}{2}$) a pound. Frank needs $2\frac{1}{2}$ pounds of grass seed. How much will the grass seed cost? _____
- Jack and Bill disagreed over their homework. Jack said $10\frac{1}{3} \cdot 4\frac{7}{8} = 50\frac{3}{8}$. Is he correct? _____
- At lunch, Ti's restaurant sells 150 sandwiches. $\frac{3}{5}$ of the sandwiches are beef, $\frac{3}{10}$ are chicken, and $\frac{1}{25}$ are cheese. The rest of the sandwiches are ham. How many ham sandwiches are sold? _____

The Order of Operations

EXAMPLE

$$5(3 + 2) - 8 \div 4$$

Step 1 Do the operation inside the parentheses.

$$5(5) - 8 \div 4$$

Step 2 Multiply and divide from left to right.

$$25 - 2$$

Step 3 Subtract.

$$25 - 2 = 23$$

Directions Simplify each expression using the order of operations.

- | | | | |
|--------------------------------|-------|----------------------------------|-------|
| 1. $16 - 5 \cdot 3$ | _____ | 11. $9(1 + 4) - 3 \cdot 8$ | _____ |
| 2. $9 + 11 \cdot 2$ | _____ | 12. $35 \div (5 \cdot 7) + 1$ | _____ |
| 3. $4(6 - 3)$ | _____ | 13. $25(8 \div 2) - 10(22 - 19)$ | _____ |
| 4. $8(42 \div 7)$ | _____ | 14. $15 \div 3 \div 5 + 6$ | _____ |
| 5. $3 + 5(20 - 18)$ | _____ | 15. $8 + 28 \div 7$ | _____ |
| 6. $(4 \cdot 2) \div 2 + 10$ | _____ | 16. $9 - 12 \div 4 + 2$ | _____ |
| 7. $25 - 4(10 - 4)$ | _____ | 17. $6 \cdot 2 + 25 \div 5$ | _____ |
| 8. $3 + 4 \cdot 5 - 12 \div 4$ | _____ | 18. $8(6 - 3) - 4 \div 2$ | _____ |
| 9. $7 \cdot 6 + 20 \div 10$ | _____ | 19. $16 \div (2 \cdot 2) - 3$ | _____ |
| 10. $20 - 10 \div 2 \cdot 3$ | _____ | 20. $20(20 \div 4) + 3 - 2$ | _____ |

Directions Use a calculator to simplify each expression.

- | | | | |
|--|-------|-------------------------------------|-------|
| 21. $100 - 8 \cdot 7 + 23$ | _____ | 26. $42 \div 7 + 6(154 \div 11)$ | _____ |
| 22. $7(625 \div 25) - 4 \cdot 5 \cdot 5$ | _____ | 27. $97 - 128 \div 4 \cdot 3$ | _____ |
| 23. $32 \div 4(62 - 60)$ | _____ | 28. $(18 + 6) \div 4 \cdot 10$ | _____ |
| 24. $16 + 5 \cdot 7 - 81 \div 9 + 30$ | _____ | 29. $19 - 3 \cdot 2 \cdot 8 \div 6$ | _____ |
| 25. $20 + 12(169 \div 13) \div 6$ | _____ | 30. $45 + 10(32 - 32) + 40$ | _____ |

Evaluating Algebraic Expressions

EXAMPLE

 Evaluate $5y + 2$, when $y = 1, 2, 3$.

 When $y = 1$:

$$5(1) + 2 =$$

$$5 + 2 = 7$$

 When $y = 2$:

$$5(2) + 2 =$$

$$10 + 2 = 12$$

 When $y = 3$:

$$5(3) + 2 =$$

$$15 + 2 = 17$$

Directions Evaluate each expression for $n = 6$.

1. $n + 4$ _____

2. $n - 3$ _____

3. $42 - 3n$ _____

4. $5n + 2$ _____

5. $14 + \frac{n}{3}$ _____

6. $\frac{n}{2} - 1$ _____

7. $4n - 13$ _____

8. $2 + \frac{n}{4}$ _____

9. $\frac{5}{2n} + \frac{3}{3n}$ _____

10. $3n - 2n$ _____

Directions Evaluate each expression for $y = 7$.

11. $y + 3$ _____

12. $2y - 10$ _____

13. $21 - 3y$ _____

14. $6y + 1$ _____

15. $12 + \frac{y}{7}$ _____

16. $\frac{y}{3} - 1$ _____

17. $4y - 16$ _____

18. $6 + \frac{1}{y}$ _____

19. $\frac{2}{3y} + \frac{2y}{3}$ _____

20. $4y + 2y$ _____

Directions Evaluate each expression for $z = 10$.

21. $4z - 12$ _____

22. $z + 8$ _____

23. $52 - 5z$ _____

24. $3z + 4$ _____

25. $11 + \frac{z}{2}$ _____

26. $\frac{z}{3} - 1$ _____

27. $5z - 3z$ _____

28. $1 + \frac{1}{z}$ _____

29. $3\frac{z}{5} + \frac{5}{z}$ _____

30. $z + 2z$ _____

Equations—Solution by Substitution

EXAMPLE

Substitute numbers into $2x + 3 = 13$ to find the root of the equation.

Substitute 0 for the variable.

$$2(0) + 3 = 13$$

$$3 = 13 \text{ is false.}$$

When $x = 5$, $2x + 3 = 13$ is true.

Therefore, $x = 5$ is true.

Directions Substitute numbers into each equation to find the root of the equation.

1. $6x + 1 = 19$ _____

2. $12x - 4 = 44$ _____

3. $28 - 2x = 14$ _____

4. $\frac{1}{2}x + 2 = 7$ _____

5. $3 + 4x = 3$ _____

6. $9 \cdot x = 27$ _____

7. $6 + 4x = 26$ _____

8. $15 - 6x = 3$ _____

9. $7x - 14 = 14$ _____

10. $x \cdot 5 = 35$ _____

11. $2 + 3x = 8$ _____

12. $x + x = 10$ _____

13. $4x - 4 = 20$ _____

14. $60 - 2x = 40$ _____

15. $\frac{5}{8}x + \frac{3}{8} = 1$ _____

16. $2x + 13 = 25$ _____

17. $10 - 3x = 1$ _____

18. $23 - 4x = 15$ _____

19. $20x - 15 = 65$ _____

20. $\frac{1}{2}x + 3 = 7$ _____

21. $5 + 3x = 26$ _____

22. $8 \cdot x = 72$ _____

23. $2 + 6x = 62$ _____

24. $x \cdot 4 = 8$ _____

25. $x - 3 = 1$ _____

Solving Addition Equations

EXAMPLESolve $5 + x = 16$ for x .**Step 1** Subtract 5 from each side.

$$5 + x - 5 = 16 - 5$$

Step 2 Perform the operations.

$$x = 11$$

Step 3 Check by substitution.

$$5 + 11 = 16 \text{ is true.}$$

Directions Solve for each variable. Write your answer in simplest form.
Check each solution.

1. $a + 11 = 17$ _____

2. $x + 16 = 38$ _____

3. $42 + y = 72$ _____

4. $29 + b = 46$ _____

5. $x + 19 = 37$ _____

6. $n + 16 = 32$ _____

7. $x + 9 = 29$ _____

8. $19 + m = 30$ _____

9. $67 + x = 72$ _____

10. $v + 15 = 28$ _____

11. $c + 7 = 28$ _____

12. $36 + e = 59$ _____

13. $w + \frac{5}{8} = 1$ _____

14. $\frac{1}{2} + b = \frac{11}{16}$ _____

15. $\frac{1}{3} + f = \frac{5}{6}$ _____

16. $x + \frac{3}{4} = \frac{7}{8}$ _____

17. $\frac{4}{5} + t = 1\frac{2}{5}$ _____

18. $c + \frac{1}{5} = \frac{13}{15}$ _____

19. $j + \frac{1}{5} = 1$ _____

20. $\frac{1}{2} = \frac{1}{3} + g$ _____

21. $\frac{7}{8} = \frac{5}{8} + p$ _____

22. $1\frac{3}{8} = y + \frac{5}{8}$ _____

23. $1\frac{2}{15} = \frac{4}{5} + d$ _____

24. $\frac{1}{2} = s + \frac{1}{4}$ _____

25. $\frac{5}{6} = h + \frac{1}{6}$ _____

Solving Subtraction Equations

EXAMPLE

Solve $x - \frac{1}{2} = \frac{3}{4}$ for x .

Step 1 Isolate the variable x by adding the inverse.

$$x - \frac{1}{2} + \frac{1}{2} = \frac{3}{4} + \frac{1}{2}$$

Step 2 Perform each operation.

$$x - \frac{1}{2} + \frac{1}{2} = \frac{3}{4} + \frac{2}{4}$$

$$x = \frac{5}{4}$$

Step 3 Simplify if necessary.

$$x = 1\frac{1}{4}$$

Directions Solve for each variable. Write your answer in simplest form.

1. $x - 13 = 25$ _____

10. $g - \frac{1}{4} = \frac{1}{4}$ _____

2. $y - 7 = 8$ _____

11. $v - \frac{3}{8} = \frac{1}{4}$ _____

3. $a - 19 = 23$ _____

12. $c - \frac{1}{6} = \frac{1}{2}$ _____

4. $d - 9 = 2$ _____

13. $z - \frac{3}{16} = \frac{9}{16}$ _____

5. $e - 17 = 33$ _____

14. $n - \frac{1}{2} = \frac{3}{8}$ _____

6. $s - 25 = 42$ _____

15. $h - \frac{5}{8} = \frac{5}{8}$ _____

7. $t - 18 = 20$ _____

16. $x - \frac{1}{2} = \frac{7}{16}$ _____

8. $n - 23 = 49$ _____

17. $j - \frac{3}{10} = \frac{3}{5}$ _____

9. $f - 16 = 39$ _____

18. $x - \frac{1}{10} = \frac{3}{10}$ _____

Directions Use addition or subtraction to solve these problems.

19. The United States and Canada produced 16 million ounces of gold. Canada alone produced 5 million ounces of gold. How much gold did the U.S. produce?
- _____

20. Mexico and Congo produced 578 thousand ounces of gold. Congo produced 257 thousand ounces of gold. How much gold did Mexico produce?
- _____

Complex Fractions

EXAMPLE

Simplify $\frac{\frac{2}{3}}{\frac{2}{5}}$.

Step 1 Rewrite the complex fraction horizontally $\frac{\frac{2}{3}}{\frac{2}{5}} = \frac{2}{3} \div \frac{2}{5}$

Step 2 To divide, multiply the dividend by the reciprocal of the divisor.

$$\frac{2}{3} \div \frac{2}{5} = \frac{2}{3} \cdot \frac{5}{2} = \frac{10}{6} \quad \text{or} \quad \frac{\frac{2}{3} \cdot \left(\frac{5}{2}\right)}{\frac{2}{5} \cdot \left(\frac{5}{2}\right)} = \frac{\frac{2}{3} \cdot \frac{5}{2}}{1} = \frac{2}{3} \cdot \frac{5}{2} = \frac{10}{6}$$

Step 3 Simplify.

$$\frac{10}{6} = 1\frac{4}{6} = 1\frac{2}{3}$$

Directions Simplify each complex fraction.

1. $\frac{\frac{2}{3}}{\frac{1}{3}}$ _____

10. $\frac{\frac{3}{4}}{6}$ _____

19. $\frac{4}{\frac{2}{3}}$ _____

2. $\frac{\frac{5}{8}}{\frac{3}{4}}$ _____

11. $\frac{7}{\frac{3}{8}}$ _____

20. $\frac{\frac{7}{9}}{3}$ _____

3. $\frac{\frac{1}{5}}{\frac{3}{8}}$ _____

12. $\frac{\frac{5}{9}}{\frac{2}{3}}$ _____

21. $\frac{\frac{1}{4}}{\frac{3}{4}}$ _____

4. $\frac{\frac{15}{16}}{\frac{1}{8}}$ _____

13. $\frac{1}{\frac{3}{10}}$ _____

22. $\frac{16}{\frac{5}{8}}$ _____

5. $\frac{6}{\frac{2}{3}}$ _____

14. $\frac{\frac{3}{5}}{\frac{9}{10}}$ _____

23. $\frac{\frac{4}{5}}{\frac{5}{14}}$ _____

6. $\frac{\frac{4}{5}}{\frac{4}{9}}$ _____

15. $\frac{\frac{1}{2}}{\frac{7}{8}}$ _____

24. $\frac{\frac{1}{2}}{6}$ _____

7. $\frac{\frac{6}{7}}{\frac{5}{7}}$ _____

16. $\frac{\frac{5}{6}}{\frac{2}{3}}$ _____

25. $\frac{5}{\frac{1}{3}}$ _____

8. $\frac{\frac{3}{8}}{\frac{3}{4}}$ _____

17. $\frac{8}{\frac{4}{11}}$ _____

9. $\frac{\frac{7}{9}}{\frac{7}{8}}$ _____

18. $\frac{\frac{2}{5}}{\frac{7}{10}}$ _____

Simplifying by Addition

EXAMPLE

Simplify $\frac{3x}{8} + \frac{5x}{12}$.

Step 1 Find the LCM of the denominators.

$$\text{LCM} = 24$$

Step 2 Write equivalent fractions.

$$\frac{3x \cdot 3}{8 \cdot 3} + \frac{5x \cdot 2}{12 \cdot 2} = \frac{9x}{24} + \frac{10x}{24}$$

Step 3 Add the equivalent fractions.

$$\frac{9x}{24} + \frac{10x}{24} = \frac{19x}{24}$$

Step 4 Simplify if possible. $\frac{19x}{24}$ is in simplest form.

Directions Simplify. Write your answer in simplest form.

1. $\frac{1}{5x} + \frac{2}{5x}$ _____

6. $\frac{3}{8j} + \frac{2}{8j}$ _____

11. $\frac{4g}{5} + \frac{1g}{5}$ _____

2. $\frac{2c}{4} + \frac{1c}{4}$ _____

7. $\frac{3w}{10} + \frac{2w}{10}$ _____

12. $\frac{1}{4b} + \frac{1}{4b}$ _____

3. $\frac{5}{8y} + \frac{2}{8y}$ _____

8. $\frac{3}{4x} + \frac{3}{4x}$ _____

13. $\frac{3}{10q} + \frac{9}{10q}$ _____

4. $\frac{4b}{7} + \frac{6b}{7}$ _____

9. $\frac{13d}{16} + \frac{3d}{16}$ _____

14. $\frac{5x}{8} + \frac{7x}{8}$ _____

5. $\frac{3z}{5} + \frac{4z}{5}$ _____

10. $\frac{5}{9y} + \frac{2}{9y}$ _____

15. $\frac{2}{11p} + \frac{5}{11p}$ _____

Directions Simplify by collecting like terms. Write your answer in simplest form.

16. $\frac{2}{5c} + \frac{1}{3c}$ _____

20. $\frac{3}{5r} + \frac{1}{6r}$ _____

24. $\frac{2n}{9} + \frac{1n}{3}$ _____

17. $\frac{5b}{8} + \frac{3b}{16}$ _____

21. $\frac{2e}{7} + \frac{5e}{14}$ _____

25. $\frac{1}{5v} + \frac{3}{4v}$ _____

18. $\frac{1y}{4} + \frac{2y}{3}$ _____

22. $\frac{5}{12k} + \frac{3}{4k}$ _____

19. $\frac{2}{3j} + \frac{11}{12j}$ _____

23. $\frac{7}{9m} + \frac{2}{3m}$ _____

Simplifying by Subtraction

EXAMPLE

 Simplify $\frac{b}{2} - \frac{b}{5}$.

Step 1 Find the LCM of the denominators. LCM = 10

Step 2 Write equivalent fractions. $\frac{b \cdot 5}{2 \cdot 5} - \frac{b \cdot 2}{5 \cdot 2} = \frac{5b}{10} - \frac{2b}{10}$
Step 3 Subtract the equivalent fractions. $\frac{5b}{10} - \frac{2b}{10} = \frac{3b}{10}$
Step 4 Simplify if possible. $\frac{3b}{10}$ is in simplest form.

Directions Simplify. Write your answer in simplest form.

1. $\frac{5c}{8} - \frac{3c}{8}$ _____

4. $\frac{15}{16e} - \frac{7}{16e}$ _____

7. $\frac{5}{6s} - \frac{1}{6s}$ _____

2. $\frac{3}{4d} - \frac{1}{4d}$ _____

5. $\frac{11}{14h} - \frac{5}{14h}$ _____

8. $\frac{7b}{9} - \frac{4b}{9}$ _____

3. $\frac{3w}{5} - \frac{2w}{5}$ _____

6. $\frac{9g}{10} - \frac{3g}{10}$ _____

9. $\frac{2}{3q} - \frac{1}{3q}$ _____

Directions Simplify by collecting like terms. Write your answer in simplest form.

10. $\frac{9}{10a} - \frac{1}{2a}$ _____

13. $\frac{2}{3r} - \frac{5}{8r}$ _____

16. $\frac{5}{9k} - \frac{1}{3k}$ _____

11. $\frac{8c}{9} - \frac{2c}{3}$ _____

14. $\frac{4x}{5} - \frac{5x}{8}$ _____

17. $\frac{11y}{16} - \frac{1y}{2}$ _____

12. $\frac{5p}{16} - \frac{1p}{4}$ _____

15. $\frac{3s}{4} - \frac{7s}{16}$ _____

Directions Solve these problems.

 18. Ed spends $\frac{3}{8}$ of his study time on history. How much of his study time does he have left?

 20. Jenny's survey showed that $\frac{11}{16}$ of her class picked blue as their favorite color. What part of her class picked a different color?

 19. Juan has $\frac{7}{8}$ yards of string. He used $\frac{2}{3}$ yards of string. How much does he have left?

Multiplying Rational Expressions

EXAMPLE

Multiply $\frac{5}{8} \cdot \frac{2}{5}$.

Step 1 Multiply the numerators and the denominators.

$$\frac{5}{8} \cdot \frac{2}{5} = \frac{5 \cdot 2}{8 \cdot 5} = \frac{10}{40}$$

Step 2 If possible, simplify the fraction.

$$\frac{10}{40} = \frac{1}{4}$$

Directions Multiply. Write your answer in simplest form.

1. $\frac{3}{4} \cdot \frac{4}{5}$ _____

9. $\frac{5}{12} \cdot \frac{24}{25}$ _____

17. $\frac{7}{15m} \cdot \frac{5}{7}$ _____

2. $\frac{5}{8} \cdot \frac{8}{9}$ _____

10. $\frac{1}{9} \cdot \frac{2}{3}$ _____

18. $\frac{9}{10n} \cdot \frac{2n}{3}$ _____

3. $\frac{14}{15} \cdot \frac{5}{7}$ _____

11. $\frac{5}{16} \cdot \frac{8}{9}$ _____

19. $\frac{9x}{13} \cdot \frac{13}{27}$ _____

4. $\frac{9}{10} \cdot \frac{5}{6}$ _____

12. $\frac{1}{2s} \cdot \frac{1}{6}$ _____

20. $\frac{5}{6a} \cdot \frac{1a}{2}$ _____

5. $\frac{6}{7} \cdot \frac{14}{15}$ _____

13. $\frac{4v}{7} \cdot \frac{7}{16v}$ _____

21. $\frac{4b}{15} \cdot \frac{5}{6}$ _____

6. $\frac{1}{5} \cdot \frac{8}{9}$ _____

14. $\frac{7}{8} \cdot \frac{16g}{17}$ _____

22. $\frac{8v}{9} \cdot \frac{1}{2v}$ _____

7. $\frac{2}{3} \cdot \frac{3}{4}$ _____

15. $\frac{3}{8c} \cdot \frac{7c}{21}$ _____

8. $\frac{8}{11} \cdot \frac{11}{12}$ _____

16. $\frac{4}{5} \cdot \frac{10}{11d}$ _____

Directions Solve each problem. Write your answer in simplest form.

23. Glenn has $\frac{2}{5}$ of a granola bar. If he eats $\frac{7}{8}$ of it, how much of the granola bar is left?

25. The Jordan River is $\frac{1}{3}$ the length of the Tisza River. The Tisza River is 600 miles long. How long is the Jordan River?

24. Amanda pours $\frac{2}{9}$ of a bag of pretzels into a dish. She eats $\frac{1}{2}$ of the pretzels in the dish. How much of the bag did she eat?

Ratios

EXAMPLE

A ratio is a comparison of two quantities using fractions.

Here are some ways to write a ratio: $\frac{3}{8}$ 3 to 8 3:8

Express a ratio in simplest form.

$$\frac{10}{24} = \frac{10 \div 2}{24 \div 2} = \frac{5}{12} \quad 5 \text{ to } 12 \quad \text{or} \quad 5:12$$

Directions Complete the chart to show how to write each ratio two other ways.

1. $\frac{8}{13}$		
2.	4 to 11	
3.		5:17
4.	16 to 9	
5. $\frac{12}{7}$		
6.		21:14
7. $\frac{11}{15}$		
8.	27 to 41	
9.		37:19
10.	53 to 61	

Directions Write *OK* if each ratio is a fraction expressed in its simplest form. If the fraction is *not* expressed in its simplest form, write the simplest form.

11. $\frac{5}{15}$ _____

16. $\frac{14}{56}$ _____

12. $\frac{2}{5}$ _____

17. $\frac{32}{57}$ _____

13. $\frac{6}{8}$ _____

18. $\frac{9}{24}$ _____

14. $\frac{3}{24}$ _____

19. $\frac{7}{15}$ _____

15. $\frac{17}{25}$ _____

20. $\frac{32}{9}$ _____

Proportions

EXAMPLE

A proportion is an equation made up of two equal ratios: $\frac{a}{b} = \frac{c}{d}$

A proportion is a true proportion if this equation is true: $ad = bc$.

The terms ad and bc are called cross products and can be used to solve for a missing variable.

$$\frac{16}{24} = \frac{2}{n} \quad (16)(n) = (24)(2) \quad 16(n) = 48 \quad n = 3$$

Directions Write *yes* or *no* to show whether each proportion is a true proportion.

1. $\frac{6}{13} = \frac{18}{39}$ _____ 3. $\frac{9}{12} = \frac{3}{5}$ _____ 5. $\frac{10}{16} = \frac{5}{8}$ _____

2. $\frac{2}{7} = \frac{4}{13}$ _____ 4. $\frac{4}{16} = \frac{1}{4}$ _____ 6. $\frac{5}{8} = \frac{40}{64}$ _____

Directions Write the proportions as an equation of cross products.

7. $\frac{2}{3} = \frac{6}{x}$ _____ 10. $\frac{x}{12} = \frac{30}{72}$ _____

8. $\frac{1}{9} = \frac{b}{81}$ _____ 11. $\frac{42}{48} = \frac{t}{8}$ _____

9. $\frac{6}{c} = \frac{36}{42}$ _____ 12. $\frac{3}{8} = \frac{30}{w}$ _____

Directions Solve for the variable in each proportion.

13. $\frac{2}{5} = \frac{x}{20}$ _____ 17. $\frac{4}{15} = \frac{d}{75}$ _____

14. $\frac{3}{8} = \frac{c}{24}$ _____ 18. $\frac{3}{4} = \frac{6}{y}$ _____

15. $\frac{5}{w} = \frac{1}{5}$ _____ 19. $\frac{3}{1} = \frac{x}{4}$ _____

16. $\frac{6}{9} = \frac{12}{a}$ _____ 20. $\frac{c}{3} = \frac{28}{21}$ _____

Ratios and Proportions

EXAMPLE

A table can be helpful in solving proportion problems.

A record store sold 1 tape for every 5 CDs. If 60 CDs were sold, how many tapes were sold?

Number of Tapes	1	x
Number of CDs	5	60

Write an equation and solve it.

$$\frac{1}{5} = \frac{x}{60} \quad (1)(60) = (5)(x) \quad 60 = 5x \quad x = 12$$

Directions Fill in each chart. Solve the problem.

1. Three cans of peas cost \$1.80. How much do 9 cans cost? _____

Number of Cans		
Cost		

2. A soccer player averaged 1 goal for every 18 tries. If the player made 6 goals, how many tries were made? _____

Goals		
Tries		

3. A bag of pecans has 2 broken pecans for each 84 nuts. How many broken pecans were found in a sack of 504 nuts? _____

Number of Broken Pecans		
Total Nuts		

4. In a class, two out of every nine students were left-handed. How many left-handers would be found in a group of 63 students? _____

Left-handers		
Total Students		

5. If 20 pounds of bird seed cost \$4.40, how much would 3 pounds cost? _____

Number of Pounds		
Cost		

Percents and Fractions

EXAMPLE

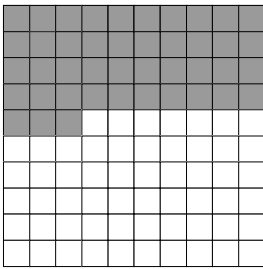
A percent is a ratio based on the number 100.

29 percent means 29 parts of a 100.

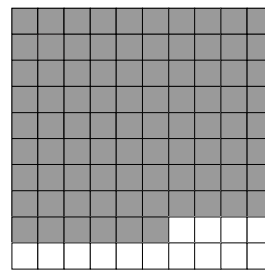
It can be written $\frac{29}{100}$ or 29%.

Directions Write a fraction to show the percent of each shaded square.

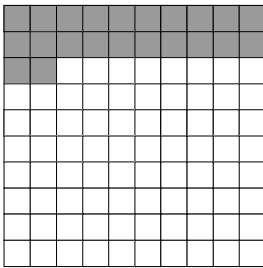
1.



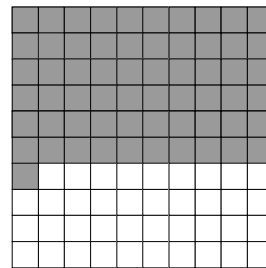
2.



3.

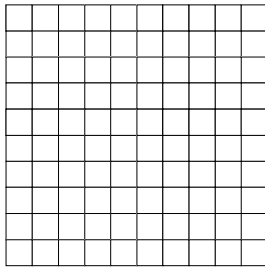


4.

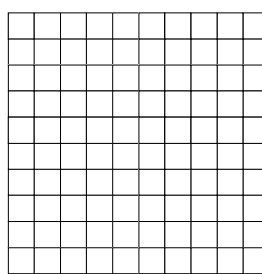


Directions Shade in the following percents.

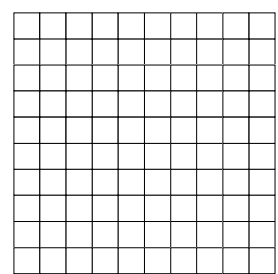
5. 8%



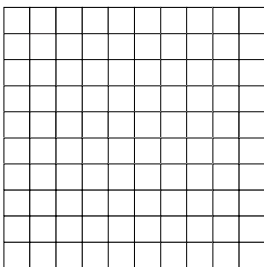
6. 25%



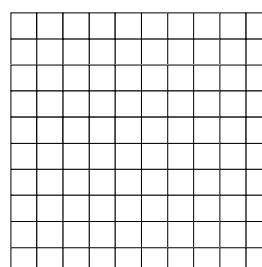
7. 87%



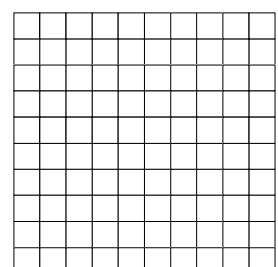
8. 43%



9. 92%



10. 12%



Percents and Decimals

EXAMPLE

Change a decimal to a percent. 0.35 to 35% 0.07 to 7%

Change a percent to a decimal. 46% to $\frac{46}{100}$ to 0.46

Change a fraction to a percent. $\frac{46}{100}$ to 46%

Change a fraction with a denominator that is not 100.

$\frac{3}{4}$ to $3 \div 4$ to 0.75 to 75%

Directions Complete the chart by filling in the missing numbers.

Decimal	Percent	Fraction
1.	63%	
2.		$\frac{2}{5}$
3. 0.10		
4.	25%	
5.		$\frac{51}{100}$
6. 0.41		
7.	55%	
8. 0.67		
9.		$\frac{9}{25}$
10.		$\frac{17}{20}$
11. 0.50		
12.	93%	
13.		$\frac{21}{50}$
14.		$\frac{7}{20}$
15.	88%	

More Percents and Decimals

Directions Change each fraction to a percent.

1. $\frac{1}{10}$ _____

2. $\frac{4}{5}$ _____

3. $\frac{1}{2}$ _____

4. $\frac{7}{8}$ _____

5. $\frac{1}{5}$ _____

6. $\frac{3}{5}$ _____

7. $\frac{1}{4}$ _____

8. $\frac{17}{25}$ _____

9. $\frac{3}{8}$ _____

10. $\frac{7}{16}$ _____

Directions Change each percent above to a decimal.

11. _____

12. _____

13. _____

14. _____

15. _____

16. _____

17. _____

18. _____

19. _____

20. _____

Directions Read each problem and write a percent *and* a decimal for the fraction used in the problem. Then solve the problem.

21. One-third of a school's students went to the football game. There are 270 students in the school. How many students attended the game? _____

22. Two-fifths of a school's 640 students eat a school lunch each day. How many students eat school lunches each day? _____

23. Of the 200 trees in the park, five-eighths are by the lake. How many trees are by the lake? _____

24. Three-tenths of the birds in the zoo live in the rainforest. The zoo has 470 birds. How many of the zoo's birds live in the rainforest? _____

25. Nine hundred people visit the elephants every day. That is three-fourths of the visitors to the zoo. How many people visit the zoo each day? _____

Finding the Percent of a Number

EXAMPLE

Here are some ways to find the percent of a number:

20% of 400

Use a proportion. $\frac{20}{100} = \frac{x}{400}$ to $(20)(400) = (100)(x)$ to $8,000 = 100x$ to $x = 80$

Use the 1% solution. $100\% = 400$ to $\frac{100\%}{100} = \frac{400}{100}$

1% of 400 is 4.

$1\% \cdot 20 = 4 \cdot 20$ $20\% = 80$

Use an equation. $(20\%)(400) = (.20)(400) = 80$

Directions Find the percent. Fill in the missing number to complete each equation. Then solve it.

1. 75% of 16 $(75\%)(\quad) = (\quad)(16) =$ _____

2. 30% of 30 $(\quad)(30) = (0.30)(\quad) =$ _____

3. 26% of 55 $(26\%)(\quad) = (\quad)(55) =$ _____

4. 93% of 70 $(\quad)(70) = (0.93)(\quad) =$ _____

5. 77% of 42 $(77\%)(\quad) = (\quad)(42) =$ _____

Directions Find the percent of each number.

6. 20% of 40 _____

11. 12% of 53 _____

7. 25% of 120 _____

12. 78% of 36 _____

8. 35% of 70 _____

13. 90% of 56 _____

9. 60% of 80 _____

14. 80% of 223 _____

10. 81% of 25 _____

15. 45% of 390 _____

Finding the Percent

EXAMPLE

What percent of 800 is 200?

Here are some ways to find out.

Use a ratio. $\frac{200}{800} = \frac{x}{100}$ to $(200)(100) = (800)(x)$ to $20,000 = 800x$ to $x = 25\%$

Use the 1% solution. $100\% = 800$ to $\frac{100\%}{100} = \frac{800}{100}$

$$1\% = 8 \quad \frac{200}{8} = 25\%$$

Use an equation. $(x)(800) = 200$ to $800x = 200$ to $x = \frac{2}{8} = \frac{1}{4} = 25\%$

Directions Find the missing percent.

- | | |
|-------------------------|--------------------------|
| 1. 15 is _____% of 20. | 4. 300 is _____% of 120. |
| 2. 64 is _____% of 320. | 5. 44 is _____% of 11. |
| 3. 48 is _____% of 96. | 6. 900 is _____% of 45. |

Directions Find the given percentage of each number.

	18% of	26% of	73% of
21	7. _____	8. _____	9. _____
73	10. _____	11. _____	12. _____
65	13. _____	14. _____	15. _____
56	16. _____	17. _____	18. _____
82	19. _____	20. _____	21. _____
37	22. _____	23. _____	24. _____
28	25. _____	26. _____	27. _____
45	28. _____	29. _____	30. _____

Percent of Increase and Decrease

EXAMPLE

A plant grew from 6 inches to 24 inches. By what percent did it increase?

To find an increase: Subtract. $24 - 6 = 18$

Write and solve an equation. 18 inches is what percent of 6 inches?

$$\frac{\text{amount of increase}}{\text{original amount}} = \frac{18}{6} = x \quad x = 3 = 300\%$$

There were 200 towels on a roll. Now there are 184 sheets.
What was the percent of decrease?

To find the decrease: Subtract. $200 - 184 = 16$

Write a proportion and solve.

$$\frac{\text{amount of decrease}}{\text{total}} = \frac{x}{100} \quad \frac{16}{200} = \frac{x}{100} \quad (16)(100) = (200)(x) \quad 1,600 = 200x \quad x = 8\%$$

Directions Solve each increase or decrease problem.

From	Amount of Increase	Percent of Increase
1. 120 to 200	_____	_____
2. 85 to 105	_____	_____
3. 60 to 72	_____	_____
4. 123 to 265	_____	_____
5. 212 to 316	_____	_____
6. 87 to 93	_____	_____
7. 212 to 444	_____	_____
From	Amount of Decrease	Percent of Decrease
8. 210 to 156	_____	_____
9. 84 to 64	_____	_____
10. 168 to 46	_____	_____
11. 454 to 360	_____	_____
12. 15 to 3	_____	_____
13. 344 to 268	_____	_____
14. 92 to 76	_____	_____
15. 212 to 146	_____	_____

Formulas and Percents

EXAMPLE

The formula for compound interest involves percents.

$$A = P(1 + i)^n$$

A = amount of money

$$A = \$200(1 + 0.04)^2$$

P = principal or original deposit

$$A = \$200(1.04)^2$$

i = interest rate per period (shown as a decimal)

$$A = \$200(1.0816)$$

n = number of compounding periods

$$A = \$216.32$$

Directions Write each percentage rate as a decimal.

1. $3\frac{3}{4}$ _____

4. $1\frac{1}{4}$ _____

7. $5\frac{1}{2}$ _____

2. $4\frac{1}{4}$ _____

5. $3\frac{1}{3}$ _____

8. $4\frac{1}{4}$ _____

3. $2\frac{1}{2}$ _____

6. $2\frac{3}{4}$ _____

9. $8\frac{3}{4}$ _____

Directions Solve each problem. Round to the fourth digit.

10. $(1.04)^3$ _____

13. $(1.0375)^2$ _____

11. $(1.034)^2$ _____

14. $(1.0875)^3$ _____

12. $(1.0425)^2$ _____

15. $(1.025)^2$ _____

Directions Solve each problem.

A bank advertised an interest rate on a savings account of $3\frac{1}{2}\%$ annually. How much did each person have at the end of two years?

Original Deposit

Amount After Two Years

16. \$250 _____

17. \$1,800 _____

18. \$735 _____

19. \$2,145 _____

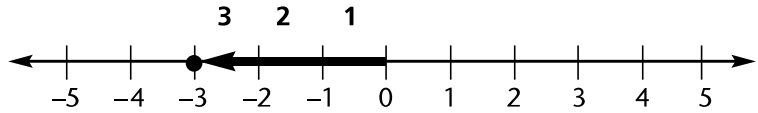
20. \$8,620 _____

The Real Number Line and Integers

EXAMPLE

$$|-3| = 3 \quad -3 \text{ is 3 units from 0.}$$

The absolute value of -3 is 3.



Directions Find the absolute value.

- | | | |
|-----------------|------------------|------------------|
| 1. $ -6 $ _____ | 5. $ 11 $ _____ | 9. $ -92 $ _____ |
| 2. $ 4 $ _____ | 6. $ -72 $ _____ | 10. $ 16 $ _____ |
| 3. $ -8 $ _____ | 7. $ -31 $ _____ | |
| 4. $ 0 $ _____ | 8. $ 25 $ _____ | |

Directions Name the opposite of each integer.

- | | | |
|-----------------|-----------------|-----------------|
| 11. -6 _____ | 15. 11 _____ | 19. -42 _____ |
| 12. -9 _____ | 16. -52 _____ | 20. 38 _____ |
| 13. 15 _____ | 17. 84 _____ | |
| 14. -24 _____ | 18. -5 _____ | |

Directions Write an integer that describes each situation.

21. The Chicago Bulls make a three-point shot in basketball. _____
22. The Green Bay Packers lose ten yards in a football game. _____
23. The stock of Company XYZ falls eight dollars in value. _____
24. School Inc., gains five dollars on the stock market. _____
25. Eighty dollars is taken out of a paycheck for taxes. _____
26. Pay fifty-five dollars for electric. _____
27. Win three hundred dollars in a raffle. _____
28. The temperature falls to twenty degrees below zero. _____
29. In five minutes, the test begins. _____
30. The test began four minutes ago. _____

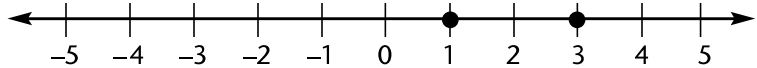
Comparing Integers—Greater Than

EXAMPLE

Compare $|-3|$ and 1.

$|-3|$ is 3 units from zero, so $|-3| = 3$.

1 is 1 unit from zero.

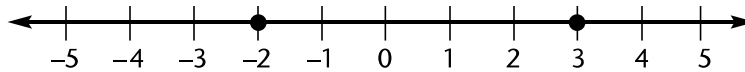


3 is farther to the right than 1, so $|-3| > 1$.

Directions Compare each pair. Use $>$ or $=$.

- | | | | |
|----------------------|-------|--------------------------|-------|
| 1. $7 \square 6$ | _____ | 18. $2 \square -1$ | _____ |
| 2. $11 \square 9$ | _____ | 19. $5 \square 2$ | _____ |
| 3. $4 \square 3$ | _____ | 20. $ -6 \square -6$ | _____ |
| 4. $-2 \square -3$ | _____ | 21. $10 \square -3$ | _____ |
| 5. $-8 \square -10$ | _____ | 22. $ -6 \square 6 $ | _____ |
| 6. $4 \square -5$ | _____ | 23. $8 \square 5$ | _____ |
| 7. $3 \square 3 $ | _____ | 24. $-8 \square -9$ | _____ |
| 8. $7 \square -1$ | _____ | 25. $6 \square -6 $ | _____ |
| 9. $10 \square 8$ | _____ | 26. $-2 \square -2$ | _____ |
| 10. $2 \square -3$ | _____ | 27. $-3 \square -6$ | _____ |
| 11. $-4 \square -5$ | _____ | 28. $ -1 \square -3$ | _____ |
| 12. $ -8 \square 6$ | _____ | 29. $ -9 \square 9$ | _____ |
| 13. $8 \square 6$ | _____ | 30. $ -10 \square -9 $ | _____ |
| 14. $-1 \square -5$ | _____ | | |
| 15. $3 \square -3$ | _____ | | |
| 16. $7 \square -7 $ | _____ | | |
| 17. $-1 \square -4$ | _____ | | |

Comparing Integers—Less Than

EXAMPLECompare -2 and 3 . -2 is to the left of 3 on the number line.Therefore, $-2 < 3$.**Directions** Compare each pair. Use $<$ or $=$.

- | | | |
|----------------------------|------------------------------|-----------------------------|
| 1. $-5 \square 1$ _____ | 10. $1 \square 8$ _____ | 19. $2 \square 6$ _____ |
| 2. $4 \square 8$ _____ | 11. $5 \square 6$ _____ | 20. $0 \square 4$ _____ |
| 3. $-9 \square -2 $ _____ | 12. $2 \square 8$ _____ | 21. $-1 \square 10$ _____ |
| 4. $3 \square -3 $ _____ | 13. $-6 \square 4$ _____ | 22. $-9 \square 3$ _____ |
| 5. $ -8 \square 9$ _____ | 14. $-12 \square 2 $ _____ | 23. $4 \square 6$ _____ |
| 6. $6 \square 6$ _____ | 15. $9 \square 10$ _____ | 24. $ 5 \square 5 $ _____ |
| 7. $-10 \square 3$ _____ | 16. $11 \square 12$ _____ | 25. $ -2 \square 2$ _____ |
| 8. $-2 \square -1$ _____ | 17. $ 8 \square -9 $ _____ | |
| 9. $3 \square 7$ _____ | 18. $6 \square 7$ _____ | |

Directions Solve these problems.

26. Tuesday's temperature was -3°F . On Wednesday the temperature was -7°F . Which day was warmer?

27. Draw a number line to show that $|-2|$ is less than $|-5|$.

28. Jimmy listed his last five golf scores for the first hole as $0, -1, 3, 1,$ and -2 . List these scores in order from least to greatest.

29. On Friday the temperature was 32°F . Saturday's temperature was 14°F . Which day was colder?

30. Jamie claims $-6, -2, 0,$ and 5 are in order from least to greatest. Is she correct?

Even and Odd Integers

EXAMPLE

Find the product of $27 \cdot 42$. Tell whether it is even or odd.

$27 \cdot 42 = 1,134$. This product is even, because odd \cdot even = even.

Directions Find each sum or difference. Tell whether it is *even* or *odd*.

1. $614 - 551$ _____

9. $128 + 147$ _____

2. $251 - 138$ _____

10. $791 - 543$ _____

3. $58 + 56$ _____

11. $360 + 369$ _____

4. $678 - 438$ _____

12. $192 + 189$ _____

5. $1,235 + 15$ _____

13. $372 - 276$ _____

6. $89 + 381$ _____

14. $2,541 + 591$ _____

7. $216 + 429$ _____

15. $168 - 55$ _____

8. $368 - 122$ _____

Directions Find each product. Tell whether it is *even* or *odd*.

16. $15 \cdot 52$ _____

26. $19 \cdot 17$ _____

17. $21 \cdot 23$ _____

27. $13 \cdot 64$ _____

18. $52 \cdot 36$ _____

28. $25 \cdot 59$ _____

19. $64 \cdot 82$ _____

29. $71 \cdot 17$ _____

20. $32 \cdot 48$ _____

30. $69 \cdot 24$ _____

21. $9 \cdot 12$ _____

22. $61 \cdot 53$ _____

23. $72 \cdot 24$ _____

24. $84 \cdot 30$ _____

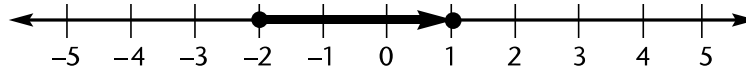
25. $60 \cdot 23$ _____

Adding Positive Integers

EXAMPLE

Find the sum of -2 and 3 .

Begin at -2 . Then move to the right 3 units. $-2 + 3 = 1$



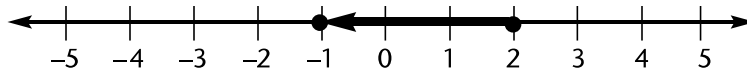
Directions Find each sum.

- | | | | |
|-------------|-------|--------------|-------|
| 1. $-5 + 5$ | _____ | 11. $-3 + 1$ | _____ |
| 2. $4 + 7$ | _____ | 12. $5 + 6$ | _____ |
| 3. $-2 + 3$ | _____ | 13. $-2 + 8$ | _____ |
| 4. $-9 + 9$ | _____ | 14. $9 + 8$ | _____ |
| 5. $4 + 5$ | _____ | 15. $-5 + 7$ | _____ |
| 6. $3 + 4$ | _____ | 16. $5 + 3$ | _____ |
| 7. $-8 + 2$ | _____ | 17. $7 + 2$ | _____ |
| 8. $1 + 9$ | _____ | 18. $-9 + 7$ | _____ |
| 9. $-6 + 7$ | _____ | 19. $-1 + 8$ | _____ |
| 10. $7 + 8$ | _____ | 20. $9 + 3$ | _____ |

Directions Find each sum using a calculator.

- | | | | |
|------------------|-------|------------------|-------|
| 21. $-251 + 787$ | _____ | 26. $-789 + 575$ | _____ |
| 22. $456 + 651$ | _____ | 27. $-123 + 261$ | _____ |
| 23. $-621 + 524$ | _____ | 28. $469 + 431$ | _____ |
| 24. $876 + 957$ | _____ | 29. $-921 + 951$ | _____ |
| 25. $426 + 436$ | _____ | 30. $-435 + 342$ | _____ |

Adding Negative Integers

EXAMPLEFind the sum of $2 + (-3)$.Begin at 2. Then move to the left 3 units. $2 + (-3) = -1$ **Directions** Find each sum.

- | | | |
|----------------------|-----------------------|------------------------|
| 1. $-5 + (-9)$ _____ | 6. $-2 + (-11)$ _____ | 11. $7 + (-3)$ _____ |
| 2. $10 + (-7)$ _____ | 7. $-3 + (-4)$ _____ | 12. $5 + (-8)$ _____ |
| 3. $9 + (-6)$ _____ | 8. $8 + (-5)$ _____ | 13. $-1 + (-4)$ _____ |
| 4. $-8 + (-3)$ _____ | 9. $-7 + (-7)$ _____ | 14. $-4 + (-12)$ _____ |
| 5. $1 + (-1)$ _____ | 10. $6 + (-2)$ _____ | |

Directions Find each sum using a calculator.

- | | | |
|---------------------------|---------------------------|---------------------------|
| 15. $-512 + (-613)$ _____ | 20. $712 + (-152)$ _____ | 25. $183 + (-161)$ _____ |
| 16. $452 + (-512)$ _____ | 21. $921 + (-671)$ _____ | 26. $-821 + (-687)$ _____ |
| 17. $329 + (-144)$ _____ | 22. $-159 + (-257)$ _____ | 27. $500 + (-425)$ _____ |
| 18. $-482 + (-169)$ _____ | 23. $-215 + (-812)$ _____ | 28. $-263 + (-691)$ _____ |
| 19. $519 + (-321)$ _____ | 24. $-812 + (-234)$ _____ | |

Directions Solve each problem by adding integers.

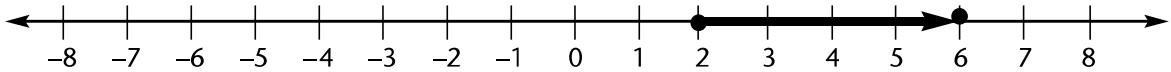
29. The Brazil Basin in the Atlantic Ocean is 20,076 feet deep, which is 2,195 feet deeper than the Eurasia Basin in the Arctic Ocean. How deep is the Eurasia Basin? _____
30. The Mariana Trench in the Pacific Ocean is 7,864 feet deeper than the Yap Trench. The Yap Trench is 27,976 feet deep. How deep is the Mariana Trench? _____

Subtracting Positive and Negative Integers

EXAMPLE

Find the difference of $2 - (-4)$.

Begin at 2. Then move to the right 4 units. $2 - (-4) = 6$



Notice that $2 - (-4) = 6$ and $2 + 4 = 6$, because subtracting -4 is the same as adding 4.

Directions Find the sum of the new expression. (Hint: First rewrite each subtraction expression as an addition expression.)

- | | | |
|-----------------------|-----------------------|-----------------------|
| 1. $-6 - 7$ _____ | 11. $-4 - 8$ _____ | 21. $7 - 8$ _____ |
| 2. $5 - (-8)$ _____ | 12. $3 - 3$ _____ | 22. $-2 - (-4)$ _____ |
| 3. $-8 - 9$ _____ | 13. $-8 - (-8)$ _____ | 23. $4 - 5$ _____ |
| 4. $7 - (-2)$ _____ | 14. $-9 - 5$ _____ | 24. $11 - (-7)$ _____ |
| 5. $-3 - 1$ _____ | 15. $7 - 3$ _____ | 25. $-10 - 5$ _____ |
| 6. $-2 - 9$ _____ | 16. $6 - (-9)$ _____ | 26. $-9 - (-4)$ _____ |
| 7. $1 - (-6)$ _____ | 17. $-10 - 2$ _____ | 27. $5 - 3$ _____ |
| 8. $0 - 4$ _____ | 18. $6 - (-4)$ _____ | 28. $-6 - (-8)$ _____ |
| 9. $-9 - 8$ _____ | 19. $12 - (-8)$ _____ | |
| 10. $5 - (-11)$ _____ | 20. $-8 - (-1)$ _____ | |

Directions Use integers to solve these problems.

29. The Nadelhorn, a mountain in Switzerland, is 14,196 feet.
The Nadelhorn is 6,124 feet lower than Mt. McKinley in Alaska.
How tall is Mt. McKinley? _____
30. Pikes Peak, Colorado, is 14,110 feet high. Mt. Kilimanjaro, Tanzania,
is 5,230 feet higher. How tall is Mt. Kilimanjaro? _____

Using Positive and Negative Integers

Directions Use the chart to find the difference in height between these points.

1. Mount Kenya and Turfan Depression

2. Turfan Depression and Death Valley

3. Annapurna I and Danakil Depression

4. Mont Blanc and Mount McKinley

5. Death Valley and Mont Blanc

Highest and Lowest Points in the World	
Annapurna I, Nepal	26,504 ft
Mount McKinley, U.S.	20,320 ft
Mount Kenya, Kenya	17,058 ft
Mont Blanc, France/Italy	15,771 ft
Death Valley, U.S.	-282 ft
Danakil Depression, Ethiopia	-383 ft
Turfan Depression, China	-505 ft
Dead Sea, Israel/Jordan	-1,312 ft

Directions Look at the chart. How many degrees separate the record high and low temperatures at these locations?

6. Seville and Roger's Pass

7. Ifrane and Northice

8. Vostok and El Azizia

9. Rivadavia and Death Valley

10. Ifrane and El Azizia

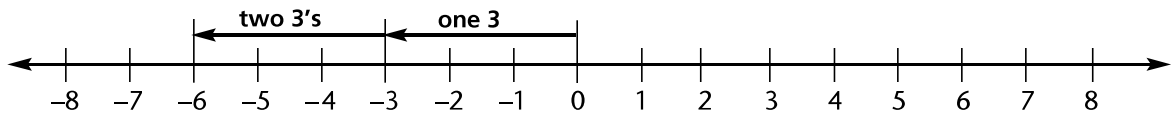
Highest and Lowest Temperatures in the World	
El Azizia, Libya	136°
Death Valley, U.S.	134°
Seville, Spain	122°
Rivadavia, Argentina	120°
Ifrane, Morocco	-11°
Roger's Pass, U.S.	-70°
Northice, Greenland	-87°
Vostok, Antarctica	-129°

Multiplying by Positive Integers

EXAMPLE

Find the product $(-2)(+3)$.

Begin at 0. Then count by 3's to the left. You will reach -6 . $(-2)(+3) = -6$



Directions Find each product.

- | | | |
|--------------------|---------------------|---------------------|
| 1. $(-5)(8)$ _____ | 8. $(-4)(8)$ _____ | 15. $(-5)(7)$ _____ |
| 2. $(8)(6)$ _____ | 9. $(6)(8)$ _____ | 16. $(2)(5)$ _____ |
| 3. $(-6)(7)$ _____ | 10. $(-2)(9)$ _____ | 17. $(-3)(7)$ _____ |
| 4. $(3)(2)$ _____ | 11. $(5)(4)$ _____ | 18. $(7)(6)$ _____ |
| 5. $(2)(3)$ _____ | 12. $(-1)(5)$ _____ | 19. $(-4)(9)$ _____ |
| 6. $(-7)(1)$ _____ | 13. $(-9)(2)$ _____ | 20. $(1)(6)$ _____ |
| 7. $(9)(9)$ _____ | 14. $(3)(1)$ _____ | |

Directions Tell whether each product is *positive* or *negative*.

- | | |
|------------------------|------------------------|
| 21. $(-334)(89)$ _____ | 26. $(675)(57)$ _____ |
| 22. $(-53)(34)$ _____ | 27. $(-522)(43)$ _____ |
| 23. $(76)(43)$ _____ | 28. $(500)(69)$ _____ |
| 24. $(39)(643)$ _____ | 29. $(-124)(65)$ _____ |
| 25. $(-78)(28)$ _____ | 30. $(43)(56)$ _____ |

Multiplying by Negative Integers

EXAMPLE

Find the product $(-2)(-4)$.

The product of $(-2)(-4)$ is $+8$.

When you multiply a negative number and a negative number, the product is positive.

Directions Tell whether each product is *positive* or *negative*.

- | | |
|--------------------------|--------------------------|
| 1. $(-52)(-45)$ _____ | 15. $(-68)(-123)$ _____ |
| 2. $(56)(-432)$ _____ | 16. $(583)(-44)$ _____ |
| 3. $(34)(-33)$ _____ | 17. $(-346)(-721)$ _____ |
| 4. $(-864)(-42)$ _____ | 18. $(57)(-33)$ _____ |
| 5. $(456)(-129)$ _____ | 19. $(-233)(-661)$ _____ |
| 6. $(-843)(-93)$ _____ | 20. $(-672)(-423)$ _____ |
| 7. $(-123)(-96)$ _____ | 21. $(278)(-467)$ _____ |
| 8. $(462)(-34)$ _____ | 22. $(-652)(-597)$ _____ |
| 9. $(532)(-405)$ _____ | 23. $(55)(-622)$ _____ |
| 10. $(-831)(-100)$ _____ | 24. $(-18)(-577)$ _____ |
| 11. $(800)(-52)$ _____ | 25. $(457)(-24)$ _____ |
| 12. $(-23)(-115)$ _____ | 26. $(-33)(-744)$ _____ |
| 13. $(76)(-341)$ _____ | 27. $(934)(-35)$ _____ |
| 14. $(-43)(-733)$ _____ | 28. $(43)(-34)$ _____ |

Directions Solve each problem.

29. The temperature fell 4°F each day for six days. What was the total change in temperature? _____
30. When initially started, a commercial freezer will cool at a rate of -20°F an hour. How much colder will the freezer be in two hours? _____

Dividing Positive and Negative Integers

EXAMPLE

Find the quotient of $-36 \div -4$.

The quotient of $-36 \div -4$ is 9.

When you divide a negative number by a negative number, the quotient is positive.

Directions Find each quotient.

- | | | |
|----------------------------|-------------------------------|-----------------------------|
| 1. $16 \div 4$ _____ | 8. $80 \div (-10)$ _____ | 15. $(-28) \div 7$ _____ |
| 2. $(-25) \div (-5)$ _____ | 9. $(-14) \div 7$ _____ | 16. $15 \div (-5)$ _____ |
| 3. $42 \div (-6)$ _____ | 10. $32 \div 8$ _____ | 17. $63 \div 9$ _____ |
| 4. $(-30) \div 6$ _____ | 11. $(-100) \div (-25)$ _____ | 18. $(-36) \div (-6)$ _____ |
| 5. $81 \div (-9)$ _____ | 12. $51 \div 3$ _____ | 19. $100 \div 10$ _____ |
| 6. $(-20) \div 5$ _____ | 13. $(-24) \div (-6)$ _____ | 20. $(-35) \div (-7)$ _____ |
| 7. $(-18) \div 6$ _____ | 14. $64 \div (-8)$ _____ | |

Directions Tell whether each quotient is *positive*, *negative*, or *zero*.

- | | |
|------------------------------|----------------------------------|
| 21. $453 \div (-84)$ _____ | 26. $5,532 \div 124$ _____ |
| 22. $0 \div 515$ _____ | 27. $(-5,089) \div (-301)$ _____ |
| 23. $1,256 \div (-68)$ _____ | 28. $(-854) \div 52$ _____ |
| 24. $(-541) \div 268$ _____ | |
| 25. $4,587 \div (-67)$ _____ | |

Directions Solve each problem.

29. A school has 704 desks. Each classroom has 32 desks.
How many classrooms are in the school? _____
30. The principal of a school bought 1,000 new desks.
There are 25 desks in each classroom. How many
classrooms are in the school? _____

Exponents

EXAMPLE

You can use the symbol 5^3 to show $5 \cdot 5 \cdot 5$.

5^3 5 is the base. 3 is the exponent. 5^3 is read "five to the third power" or "five cubed."

When you write a negative number with an exponent, place the negative number in parentheses, and then write the exponent.

$(-6)^2$ (-6) is the base. 2 is the exponent. $(-6)^2$ is read "negative six to the second power."

m^4 m is the base. 4 is the exponent. m^4 is read " m to the fourth power."

Directions Write an expression for each phrase.

- | | | | |
|---------------------------------------|-------|------------------------------------|-------|
| 1. ten to the second power | _____ | 6. two to the seventh power | _____ |
| 2. four to the tenth power | _____ | 7. a to the fourth power | _____ |
| 3. negative six to the third power | _____ | 8. negative ten to the fifth power | _____ |
| 4. eight to the fourth power | _____ | 9. negative b to the tenth power | _____ |
| 5. negative three to the second power | _____ | 10. nine to the ninth power | _____ |

Directions Name the exponent in each of the following.

- | | | | | | |
|---------------|-------|------------|-------|-----------|-------|
| 11. $(-10)^8$ | _____ | 13. 5^n | _____ | 15. 7^3 | _____ |
| 12. 2^9 | _____ | 14. 12^1 | _____ | | |

Directions Name the base in each of the following.

- | | | | | | |
|---------------|-------|-----------------|-------|--------------|-------|
| 16. 5^2 | _____ | 18. 2^4 | _____ | 20. $(-n)^4$ | _____ |
| 17. 15^{10} | _____ | 19. $(-5)^{11}$ | _____ | | |

Directions Rewrite each of the following using exponents.

- | | | | |
|--|-------|----------------------------------|-------|
| 21. $(-7) \cdot (-7) \cdot (-7) \cdot (-7) \cdot (-7)$ | _____ | 24. $(-c) \cdot (-c) \cdot (-c)$ | _____ |
| 22. $4 \cdot 4$ | _____ | 25. $12 \cdot 12 \cdot 12$ | _____ |
| 23. $8 \cdot 8 \cdot 8 \cdot 8$ | _____ | | |

Multiplying with Exponents

EXAMPLE

If two terms with exponents have the same base, you can multiply the terms by adding exponents.

$$4^2 \cdot 4^3$$

The base of both terms is 4.

$$\begin{aligned} 4^2 \cdot 4^3 &= (4 \cdot 4) \cdot (4 \cdot 4 \cdot 4) \\ &= 4 \cdot 4 \cdot 4 \cdot 4 \cdot 4 \end{aligned}$$

$$4^2 \cdot 4^3 = 4^5$$

$$b^2 \cdot b^2$$

The base of both terms is b .

$$\begin{aligned} b^2 \cdot b^2 &= (b \cdot b) \cdot (b \cdot b) \\ b^2 \cdot b^2 &= b^4 \end{aligned}$$

$$3^n \cdot 3^n$$

The base of both terms is 3.

$$\begin{aligned} 3^n \cdot 3^n &= 3^{n+n} \\ 3^n \cdot 3^n &= 3^{2n} \end{aligned}$$

Directions Simplify each expression.

1. $7^4 \cdot 7^2$ _____

2. $6^2 \cdot 6$ _____

3. $(-m)^2 \cdot (-m)^8$ _____

4. $2^4 \cdot 2^3$ _____

5. $n^3 \cdot n$ _____

6. $14^4 \cdot 14^7$ _____

7. $a^5 \cdot a^2$ _____

8. $(-10)^2 \cdot (-10)^3$ _____

9. $3^{2y} \cdot 3^y$ _____

10. $6^5 \cdot 6^5$ _____

11. $2^{3p} \cdot 2^{3p}$ _____

12. $15^5 \cdot 15^6$ _____

13. $3^3 \cdot 3^4$ _____

14. $b^3 \cdot b^3$ _____

15. $(-n)^2 \cdot (-n)^2$ _____

Directions Tell whether each statement is *true* or *false*. If a statement is false, tell why.

16. $(-8)^8 \cdot (-8)^8 = (-8)^{16}$ _____

17. $5^3 \cdot 5^4 = 5^{12}$ _____

18. $6^{4n} \cdot 6^{3n} = 6^{7n}$ _____

19. $b^7 \cdot b^2 = b^5$ _____

20. $25^5 \cdot 25 = 25^6$ _____

21. $3^4 \cdot 3^2 = 3^8$ _____

22. $2^6 \cdot 2^6 = 2^{12}$ _____

23. $2^n \cdot 2^{3n} = 2^{4n}$ _____

24. $7^7 \cdot 7^4 = 7^{11}$ _____

25. $b^2 \cdot b^{10} = b^{12}$ _____

Dividing with Exponents

EXAMPLE

If two terms with exponents have the same base, you can divide the terms by subtracting exponents.

$$8^6 \div 8^3 = \frac{8^6}{8^3}$$

The base of both terms is 8.

$$= \frac{(8 \cdot 8 \cdot 8 \cdot 8 \cdot 8 \cdot 8)}{(8 \cdot 8 \cdot 8)}$$

$$= (8 \cdot 8 \cdot 8)$$

$$8^6 \div 8^3 = 8^{6-3} = 8^3$$

$$a^4 \div a^2 = \frac{a^4}{a^2}$$

$$= \frac{(a \cdot a \cdot a \cdot a)}{(a \cdot a)}$$

$$a^4 \div a^2 = a^{4-2} = a^2$$

$$6^{2n} \div 6^n = \frac{6^{2n}}{6^n}$$

$$= \frac{(6^n \cdot 6^n)}{(6^n)}$$

$$6^{2n} \div 6^n = 6^{2n-n} = 6^n$$

Directions Simplify each expression.

1. $7^{6n} \div 7^{3n}$ _____

2. $8^8 \div 8^2$ _____

3. $m^4 \div m^4$ _____

4. $22^8 \div 22^4$ _____

5. $k^2 \div k$ _____

6. $10^9 \div 10^7$ _____

7. $(-y)^6 \div (-y)^3$ _____

8. $11^{10} \div 11^{10}$ _____

9. $7^{14} \div 7^7$ _____

10. $10^3 \div 10$ _____

11. $(-6)^{6n} \div (-6)^{2n}$ _____

12. $2^5 \div 2^5$ _____

13. $30^4 \div 30^3$ _____

14. $d^5 \div d^2$ _____

15. $17^8 \div 17^2$ _____

Directions Tell whether each statement is *true* or *false*. If a statement is false, tell why.

16. $4^4 \div 4^4 = 4$ _____

17. $12^3 \div 12 = 12^2$ _____

18. $3^{8n} \div 3^{6n} = 3^{2n}$ _____

19. $9^7 \div 9^2 = 9^5$ _____

20. $1^5 \div 1^2 = 1^3$ _____

21. $16^4 \div 16^2 = 16^6$ _____

22. $4^6 \div 4^4 = 4^2$ _____

23. $10^{10} \div 10^3 = 10^7$ _____

24. $(-j)^7 \div (-j)^2 = (-j)^9$ _____

25. $5^{12} \div 5^2 = 5^{10}$ _____

Squares

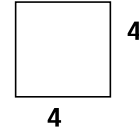
EXAMPLE

Write an expression for the area of a square.

Area of a square = length • width = $4 \cdot 4 = 4^2$

or Area of a square = side squared, or $s^2 = 4 \cdot 4 = 4^2$

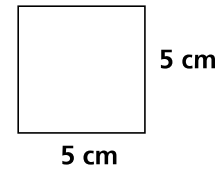
That is why 4^2 can be read as "4 squared."



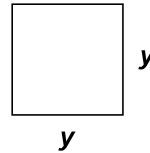
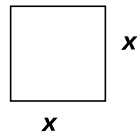
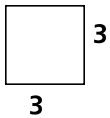
Find the area of a square in square units by multiplying.

Area of a square = $s^2 = 5^2$

$= 5^2 = 5 \cdot 5 = 25$ sq cm



Directions Write an expression for the area of each square.



1. _____

2. _____

3. _____

Directions Multiply to find the area of each square. Use the formula $\text{Area} = s^2$.

4. Square with sides 7 centimeters long _____

5. Square with sides 2 centimeters long _____

6. Square with sides 6 centimeters long _____

Directions Write an expression to describe the problem. Then solve the problem.

7. Alicia has a board game that is 18 inches wide and 18 inches long.
What is the area of the board game? _____

8. Harris is cultivating a garden that is 20 feet long and 20 feet wide.
What is the area of his garden? _____

9. The floor plan for the game room in the new recreation center is 40 feet by 40 feet. What is the floor area in the game room? _____

10. Iris bought a new square tablecloth for the kitchen table. The cloth is 5 feet by 5 feet. What is its area? _____

Cubes

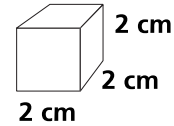
EXAMPLE

Write an expression for the volume of a cube.

$$\text{Volume} = \text{length} \cdot \text{width} \cdot \text{height} = 2 \cdot 2 \cdot 2 = 2^3$$

$$\text{or Volume} = \text{side cubed, or } s^3 = 2 \cdot 2 \cdot 2 = 2^3$$

That is why 2^3 can be read as "two cubed."

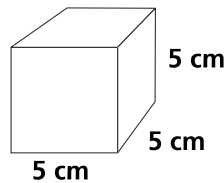


Find the volume of the cube in cubic units by multiplying.

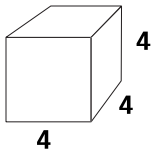
$$\text{Volume} = s^3$$

$$\text{Volume} = 5^3$$

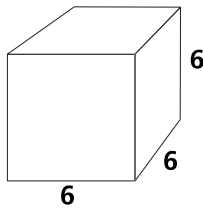
$$= 5 \cdot 5 \cdot 5 = 125 \text{ cubic cm}$$



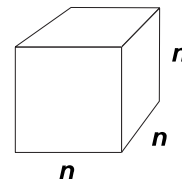
Directions Write an expression for the volume of each cube.



1. _____



2. _____



3. _____

Directions Multiply to find the volume of each cube. Use the formula $\text{Volume} = s^3$.

4. Cube with sides 7 centimeters long _____

5. Cube with sides 1 centimeter long _____

Directions Use a calculator to find the volume of each cube. Use the formula $\text{Volume} = s^3$.

6. Cube with sides 9 centimeters long _____

7. Cube with sides 13 centimeters long _____

8. Cube with sides 35 centimeters long _____

Directions Use the formula for volume to solve each problem.

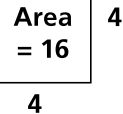
9. Ana Maria keeps her hats and scarves in a decorated box with sides 8 inches long. What is the volume of the box? _____

10. Victor's computer monitor came in a packing box with sides 3 feet long. What is the volume of the packing box? _____

Square Roots

EXAMPLE

Find the length of the side of a square.



Recall that the formula for area is $A = s^2$. For this square, $A = s^2 = 4^2 = 16$.

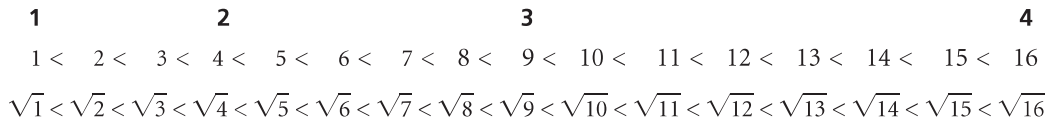
To find the length of a side of the square, you must find the square root.

$$s = \sqrt{A} = \sqrt{16} = 4$$

EXAMPLE

Find the square root of 5.

You can use a number line to estimate the square roots of numbers that are not perfect squares.



From the number line, you can see that $\sqrt{5}$ is between 2 and 3.

$$2 < \sqrt{5} < 3$$

To find the accurate decimal square root, use a calculator.

Round the decimal to the nearest hundredth. $\sqrt{5} = 2.24$

Directions Use the number line to make each statement true. Then use a calculator to find a decimal value of each square root. Round the decimal to the nearest hundredth.

1. $\square < \sqrt{15} < \square$ _____

5. $\square < \sqrt{3} < \square$ _____

2. $\square < \sqrt{12} < \square$ _____

6. $\square < \sqrt{7} < \square$ _____

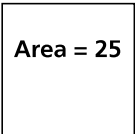
3. $\square < \sqrt{8} < \square$ _____

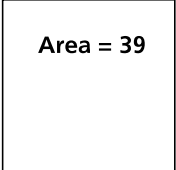
7. $\square < \sqrt{14} < \square$ _____

4. $\square < \sqrt{11} < \square$ _____

8. $\square < \sqrt{6} < \square$ _____

Directions Find the length of a side of the square. You may use your calculator. Round to the nearest hundredth if necessary.

9.  _____

10.  _____

Irrational Numbers and Square Roots

EXAMPLE

The square roots of some numbers are whole numbers. Whole numbers are rational numbers. For example, $\sqrt{25} = 5$, which is a whole number and is a rational number.

The square roots of some numbers are not whole numbers. They are irrational numbers. For example, $\sqrt{3} = 1.73$, which is not a whole number and is an irrational number.

You can use a graph to find the approximate value of an irrational number.

Find the value of $\sqrt{50}$ on the graph below.

Step 1 Estimate the value of $\sqrt{50}$. 50 is between the perfect squares 49 and 64, so $\sqrt{50}$ is between 7 and 8.

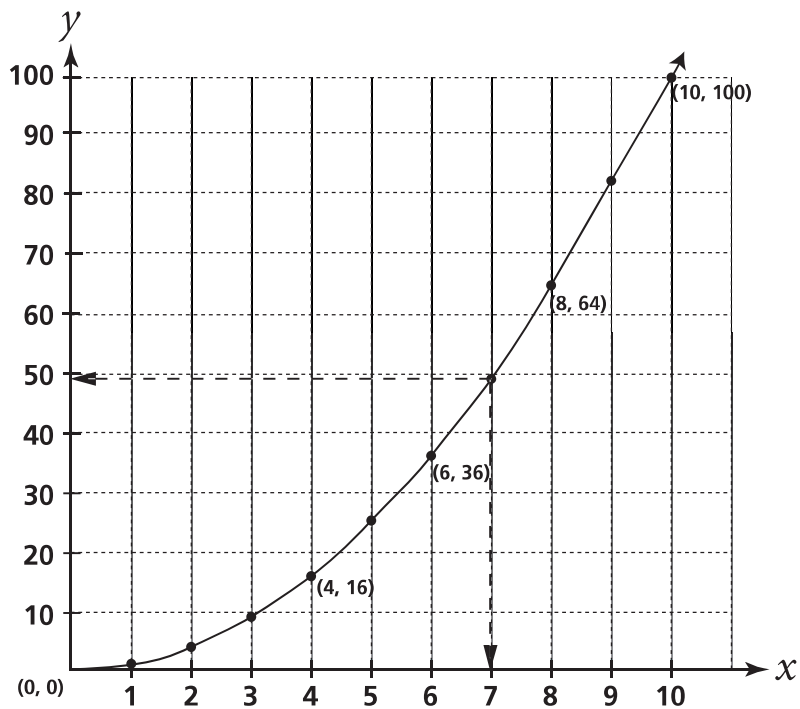
Step 2 Find 50 on the left-hand scale and draw a straight line to the graph.

Step 3 Draw a straight line from the point of the graph to the bottom axis. That line will cross the axis at about $\sqrt{50}$. The value is about 7.1.

Step 4 Compare your estimated value to the calculator value, which is 7.07. So 7.1 for the graph is close to the calculator value of 7.07 rounded to the nearest hundredth.

Directions Use the graph to estimate these values.

1. $\sqrt{95}$ _____
2. $\sqrt{90}$ _____
3. $\sqrt{85}$ _____
4. $\sqrt{80}$ _____
5. $\sqrt{75}$ _____
6. $\sqrt{70}$ _____
7. $\sqrt{65}$ _____
8. $\sqrt{60}$ _____
9. $\sqrt{45}$ _____
10. $\sqrt{40}$ _____
11. $\sqrt{35}$ _____
12. $\sqrt{30}$ _____
13. $\sqrt{25}$ _____
14. $\sqrt{20}$ _____
15. $\sqrt{15}$ _____



Pythagorean Theorem

EXAMPLE

In any right triangle, sides a and b are the sides of the triangle that form the right angle. Side c is the hypotenuse, or longest side, of a right triangle. If you know the length of two sides of a right triangle, you can use the Pythagorean theorem to find the length of the third side.

The Pythagorean theorem is this formula: $a^2 + b^2 = c^2$.

Use the Pythagorean theorem to find the hypotenuse of this right triangle.

Step 1 Substitute the values in the equation. Then square the values.

$$c^2 = a^2 + b^2$$

$$c^2 = 6^2 + 8^2$$

$$c^2 = 36 + 64$$

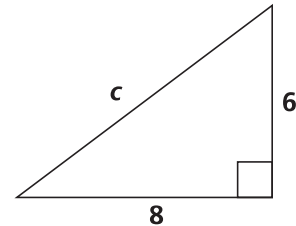
Step 2 Take the square root of each side of the equation.

$$\sqrt{c^2} = \sqrt{36 + 64}$$

$$c = \sqrt{100}$$

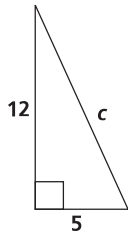
$$c = 10$$

The hypotenuse is 10 units long.

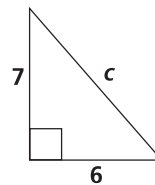


Directions Use the Pythagorean theorem to find the length of the side not given. You may use a calculator. If necessary, round to the nearest tenth.

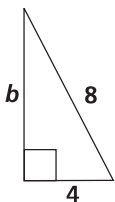
1.



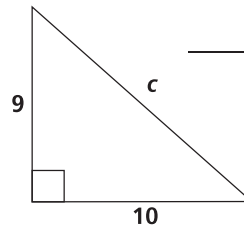
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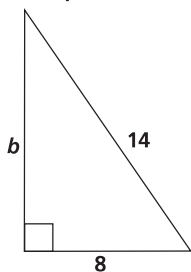
3.



4.



5.



More About Triangles

EXAMPLE

Is this scalene triangle a right triangle?

Step 1 Write the Pythagorean formula.

$$a^2 + b^2 = c^2$$

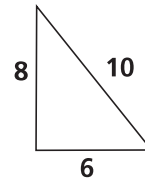
Step 2 Substitute the triangle's values for a , b , and c .

$$a^2 + b^2 = c^2$$

$$6^2 + 8^2 = 10^2$$

$$36 + 64 = 100$$

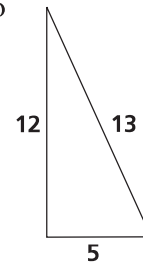
The equation is true, so this scalene triangle is also a right triangle.



Directions Answer the question. Then use the Pythagorean theorem to determine whether the triangle is also a right triangle.

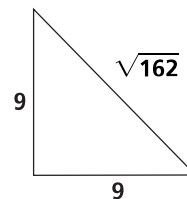
1. Is this triangle a scalene triangle, an isosceles triangle, or an equilateral triangle?

_____ Is it a right triangle? _____



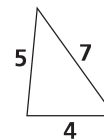
2. Is this triangle a scalene triangle, an isosceles triangle, or an equilateral triangle?

_____ Is it a right triangle? _____



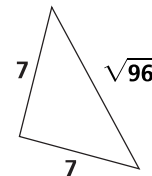
3. Is this triangle a scalene triangle, an isosceles triangle, or an equilateral triangle?

_____ Is it a right triangle? _____



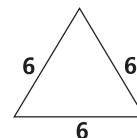
4. Is this triangle a scalene triangle, an isosceles triangle, or an equilateral triangle?

_____ Is it a right triangle? _____



5. Is this triangle a scalene triangle, an isosceles triangle, or an equilateral triangle?

_____ Is it a right triangle? _____

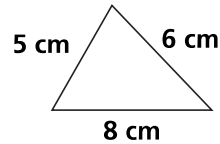
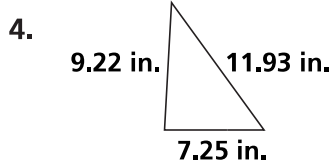
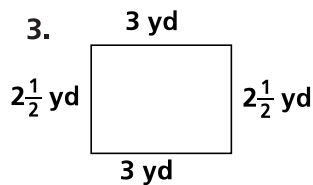
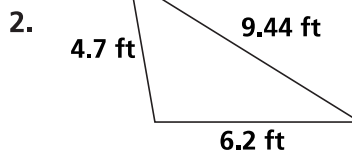
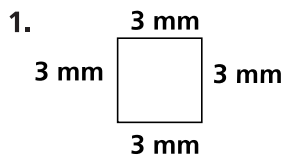


Perimeters of Polygons

EXAMPLE

Find the perimeter of this figure.

Perimeter = $5 + 6 + 8 = 19$ cm

**Directions** Find the perimeter of each figure.**Directions** Solve each problem to find the perimeter.

5. The sides of a quadrilateral measure $6\frac{7}{8}$ ft, $4\frac{1}{2}$ ft, $3\frac{1}{8}$ ft, and $7\frac{1}{2}$ ft. What is the perimeter? _____
6. Two sides of an isosceles triangle measure 6.42 m each. The remaining side measures 9.73 m. What is the perimeter of the triangle? _____
7. Each side of an equilateral triangle measures 48 yards. What is the perimeter? _____
8. A scalene triangle has sides measuring 532.6 ft, 429.3 ft, and 830.6 ft. What is the perimeter? _____

Directions Solve each problem.

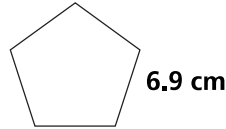
9. Hector made a dog kennel in his backyard. He used a total of 28 feet of fencing, including the gate. If two sides of the kennel are ten feet each, what are the lengths of the other two sides? _____
10. Maya has 13.75 inches of gold string, which she wants to glue around a picture frame in the shape of an equilateral triangle. Each side of the triangle is 4.25 inches. Does she have enough string? _____

Perimeters of Regular Polygons

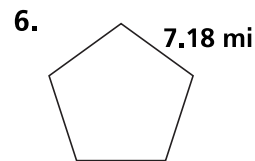
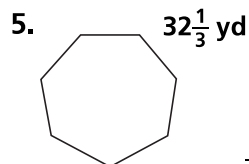
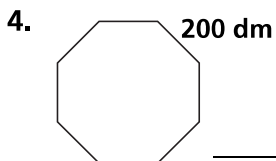
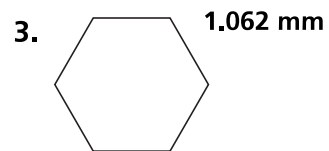
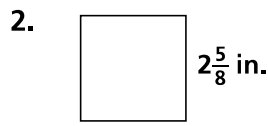
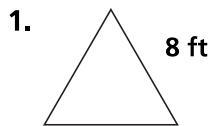
EXAMPLE

Each side of a regular pentagon measures 6.9 cm. Find the perimeter.

$$P = 5(6.9) = 34.5 \text{ cm}$$



Directions Find the perimeter of each regular polygon.



Directions Find the number of sides that each shape has.

7. Each side of a regular polygon measures 3.67 m. The perimeter of the polygon is 47.71 m. How many sides does this regular polygon have?

8. The perimeter of a regular polygon is 1,071 cm. Each side of the polygon measures 63 cm. How many sides does this regular polygon have?

9. The sum of all sides of a regular polygon is 253 ft. Each side measures 11 ft. How many sides does this regular polygon have?

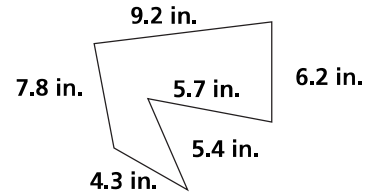
10. The perimeter of a regular polygon is 13.125 ft. Each side measures 1.875 ft. How many sides does this regular polygon have?

Perimeters of Irregular Polygons

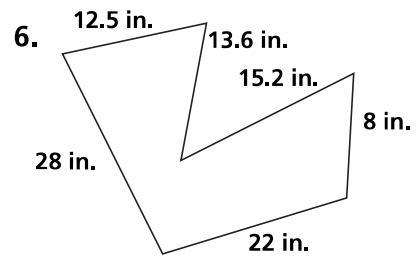
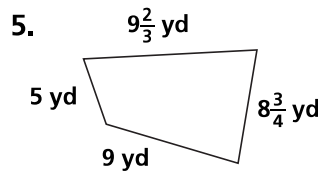
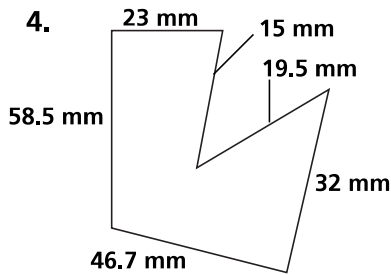
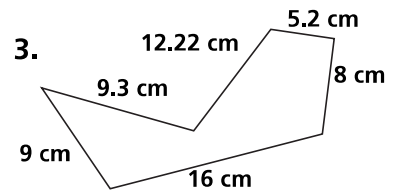
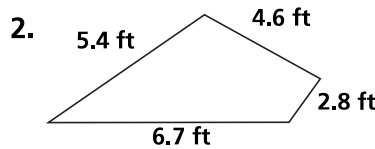
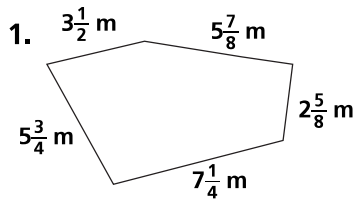
EXAMPLE

Find the perimeter of this polygon.

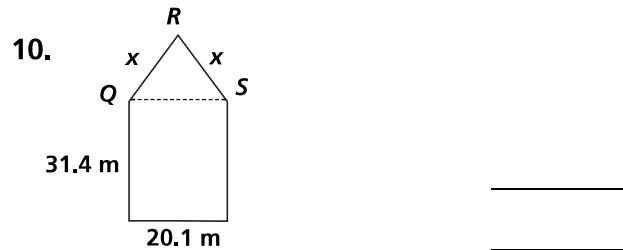
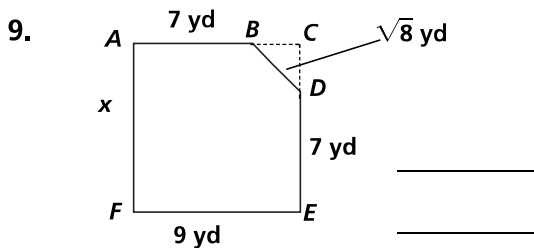
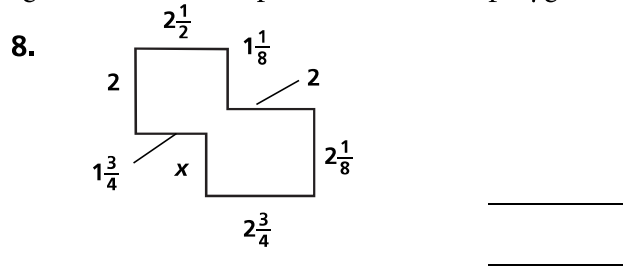
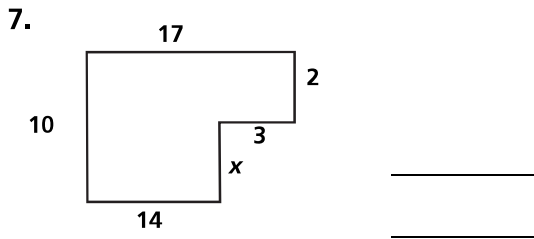
$$P = 6.2 + 5.7 + 5.4 + 4.3 + 7.8 + 9.2 = 38.6 \text{ in.}$$



Directions Find the perimeter of each polygon.



Directions Find the measure of each missing x . Then find the perimeter of each polygon.



$ACEF$ is a square.

Triangle QRS is an equilateral triangle.

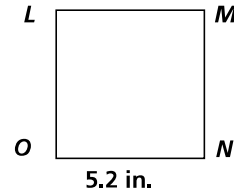
Areas of Rectangles and Squares

EXAMPLE

Find the area of square $LMNO$.

Substitute 5.2 into the formula $A = s^2$.

$$A = (5.2)^2 = 27.04 \text{ in.}^2$$



Directions Find the area of each rectangle.

- Rectangle with $l = 8$ ft and $w = 6$ ft _____
- Rectangle with $l = 13$ m and $w = 4$ m _____
- Rectangle with $l = 15.5$ cm and $w = 8$ cm _____
- Rectangle with $l = 4\frac{1}{2}$ yd and $w = 6\frac{1}{4}$ yd _____

Directions Find the area of each square.

- Square with $s = 10$ mm _____
- Square with $s = 21$ ft _____
- Square with $s = 4.2$ cm _____
- Square with $s = 5\frac{1}{2}$ m _____

Directions Use the formula $A = s^2$ and a calculator to find the area of each square.

- $s = 23$ m _____
- $s = 6.7$ ft _____
- $s = 8.5$ cm _____
- $s = 42$ in. _____
- $s = 1.42$ mi _____

Directions Solve each problem.

- Allen is painting a family room. Two walls are 8 ft high and 15 ft long. The other two walls are 8 ft high and 9 ft long. Allen has one gallon of paint, which will cover 400 ft^2 of walls. Will he have enough paint? Explain.

- Consuela cuts lawns as a part-time job. The last lawn she cut was rectangular and totaled $1,365 \text{ yd}^2$. One side of the lawn was 35 yards long. What was the length of the other side?

Areas of Triangles

EXAMPLE

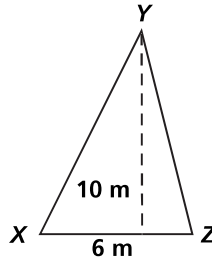
Find the area of triangle XYZ.

Use the formula $A = \frac{1}{2}bh$.

$$A = \frac{1}{2}(6)(10)$$

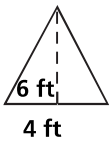
$$A = \frac{1}{2}(60)$$

$$A = 30 \text{ m}^2$$

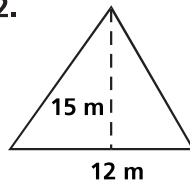


Directions Find the area of each figure.

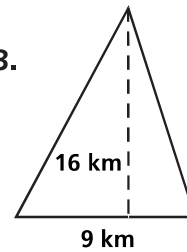
1.



2.



3.



Directions Find the base or height of each triangle.

4. The area of a triangle is 12 ft^2 and the base is 4 ft. What is the height? _____
5. The area of a triangle is 32 in.^2 and the height is 8 in. What is the base? _____
6. The area of a triangle is 15 m^2 and the base is 10 m. What is the height? _____
7. The area of a triangle is 36 yd^2 and the height is 9 yd. What is the base? _____
8. The area of a triangle is 36 km^2 and the height is 12 km. What is the base? _____

Directions Solve these problems.

9. Howard is constructing a triangular garden edge out of brick. The base of the garden is 15 ft. The area is 165 ft^2 . What is the height of the triangle?

10. Jana is making curtains in the shape of triangles. She needs to make two triangle curtains for one window. The triangles have a base of 2 ft and a height of 4 ft. What is the total area of the triangle curtains for one window?

Areas of Trapezoids and Parallelograms

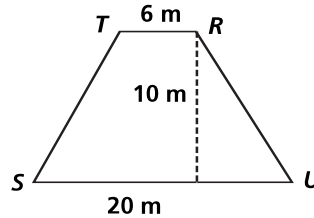
EXAMPLE

Find the area of trapezoid $STRU$.

$$A = \frac{b_1 + b_2}{2}h$$

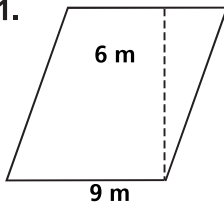
$$A = \frac{6 + 20}{2}(10) = \frac{26}{2}(10)$$

$$A = (13)(10) = 130 \text{ m}^2$$

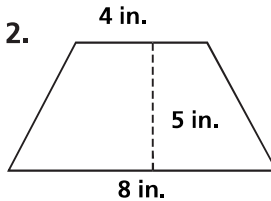


Directions Find the area of each quadrilateral.

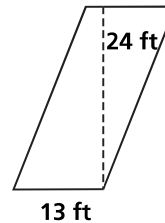
1.



2.



3.



Directions Find the base or height of each quadrilateral.

4. A parallelogram has a height of 9 cm and an area of 108 cm^2 .

What is the length of its base? _____

5. A trapezoid has one base 6 ft long and another base 8 ft long. Its area is 240 ft^2 .

What is its height? _____

6. If a parallelogram has a base of 11 m and an area of 176 m^2 , what is its height?

7. A parallelogram has a height of 12 in. and an area of 168 in.^2 .

What is the length of its base? _____

8. The bases of a trapezoid equal 16 km and its area is 32 km^2 . What is its height? _____

9. If a parallelogram has a base of 13 mm and an area of 78 mm^2 ,

what is its height? _____

10. The bases of a trapezoid equal 17 yd and its area is 68 yd^2 . What is its height? _____

Areas of Irregular Polygons

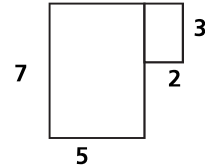
EXAMPLE

Find the area of this polygon.

Divide the polygon into smaller regions to calculate the areas.

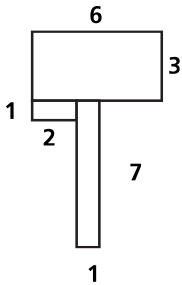
$$A = (5 \cdot 7) + (2 \cdot 3)$$

$$A = 35 + 6 = 41 \text{ units}^2$$

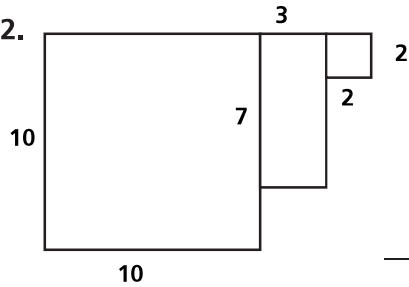


Directions Find the area of each polygon.

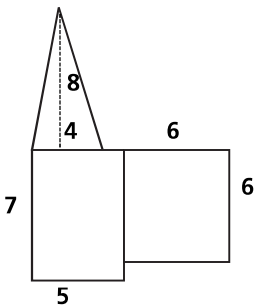
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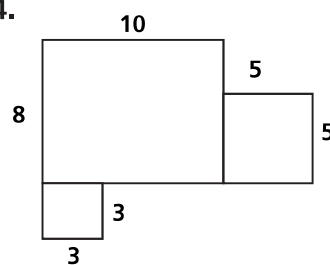
2.



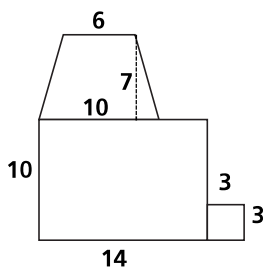
3.



4.



5.



Working with Areas of Shapes

Directions Find the area of each rectangle or square.

1. Rectangle with $l = 9$ in. and $w = 3.85$ in. _____
2. Rectangle with $l = 3\frac{1}{3}$ mi and $w = 7\frac{1}{2}$ mi _____
3. Square with $s = 16.3$ yd _____
4. Square with $s = 3\frac{1}{4}$ ft _____
5. Square with $s = 12.33$ mi _____

Directions Use the area to find the base or height of each triangle, trapezoid, or parallelogram.

6. The area of a triangle is 14 ft^2 and the base is 7 ft. What is the height? _____
7. The area of a triangle is 15 mm^2 and the height is 5 mm. What is the base? _____
8. The area of a triangle is 9 cm^2 and the base is 3 cm. What is the height? _____
9. The area of a triangle is 50 in.^2 and the base is 10 in. What is the height? _____
10. The area of a triangle is 80 m^2 and the height is 8 m. What is the base? _____
11. The area of a triangle is 40.5 ft^2 and the base is 9 ft. What is the height? _____
12. The area of a triangle is 17.5 dm^2 and the height is 7 dm. What is the base? _____
13. A trapezoid has one base 23 in. long and another base 27 in. long. Its area is 400 in.^2 .
What is its height? _____
14. The bases of a trapezoid equal 68 mm and its area is $1,768 \text{ mm}^2$.
What is its height? _____
15. A parallelogram has a height of 23 mi and an area of 667 mi^2 .
What is the length of its base? _____

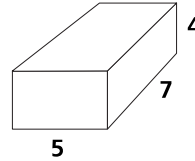
Volume

EXAMPLE

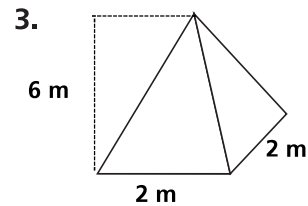
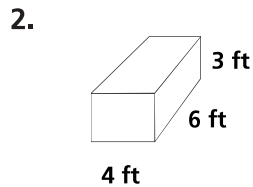
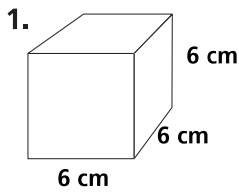
Find the volume of this rectangular prism.

$$V = lwh$$

$$V = (7)(5)(4) = 140 \text{ in.}^3$$



Directions Find the volume of each figure.



Directions Use the formula $V = e^3$ and a calculator to find the volume of each cube.

4. $e = 23 \text{ mm}$ _____

10. $e = 68 \text{ dm}$ _____

5. $e = 1.8 \text{ in.}$ _____

11. $e = 43 \text{ m}$ _____

6. $e = 126 \text{ ft}$ _____

12. $e = 19.2 \text{ in.}$ _____

7. $e = 0.9 \text{ mi}$ _____

13. $e = 202 \text{ ft}$ _____

8. $e = 50 \text{ cm}$ _____

9. $e = 1.02 \text{ km}$ _____

Directions Solve each problem.

14. Marcus is shipping books to his brother in New York. The box is 10 inches by 10 inches and 6 inches deep. Each book is 5 inches by 5 inches and 2 inches thick. How many books can Marcus ship in one package? _____

15. Lisa's suitcase is 18 inches wide, 32 inches high, and 36 inches long. What is the volume of the suitcase? _____

Circumferences and Areas of Circles

EXAMPLE

Find the circumference and area of a circle with a radius of 5 feet.

To find the circumference, use the formula $C = \pi d$.

First, calculate the diameter.

$$2 \cdot 5 = 10 \text{ feet}$$

$$C = (3.14)(10) = 31.4 \text{ feet}$$

To find the area, use the formula $A = \pi r^2$.

$$A = (3.14)(5^2) = 78.5 \text{ feet}^2$$

Directions Find the circumference of a circle with the given radius or diameter. Use the formula $C = \pi d$. Use 3.14 for π .

- | | |
|--------------------------|---------------------------|
| 1. radius = 4 in. _____ | 4. diameter = 10 mm _____ |
| 2. diameter = 6 ft _____ | 5. radius = 7 km _____ |
| 3. radius = 2 m _____ | |

Directions Find the area of a circle with the given radius or diameter. Use the formula $A = \pi r^2$. Use 3.14 for π .

- | | |
|-----------------------------|----------------------------|
| 6. radius = 3 yd _____ | 11. radius = 6 km _____ |
| 7. diameter = 10 cm _____ | 12. radius = 5 mi _____ |
| 8. radius = 7 ft _____ | 13. diameter = 6 in. _____ |
| 9. diameter = 4 m _____ | 14. radius = 8 ft _____ |
| 10. diameter = 14 in. _____ | 15. radius = 10 m _____ |

Directions Use a calculator and the formula $A = \pi r^2$ to find the areas of circles with the following measures. Use 3.14 for π .

- | | |
|------------------------------|----------------------------|
| 16. diameter = 1.25 yd _____ | 19. diameter = 9.5 m _____ |
| 17. radius = 215 mi _____ | 20. radius = 1.8 km _____ |
| 18. radius = 6.7 ft _____ | |

Volumes of Cylinders and Spheres

EXAMPLE

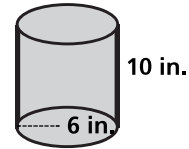
Find the volume of this cylinder.

Use the formula $V = \pi r^2 h$.

$$V = (3.14)(6)^2(10)$$

$$V = (3.14)(36)(10)$$

$$V = 1,130.4 \text{ in.}^3$$



Directions Find the volume of a cylinder with the given height and radius or diameter. Use the formula $V = \pi r^2 h$. Use 3.14 for π .

- | | |
|---|---|
| 1. diameter = 6 in.; height = 5 in. _____ | 6. diameter = 4 cm; height = 4 cm _____ |
| 2. radius = 4 ft; height = 7 ft _____ | 7. radius = 9 m; height = 13 m _____ |
| 3. diameter = 10 mm; height = 8 mm _____ | 8. radius = 1 ft; height = 6 ft _____ |
| 4. radius = 3 cm; height = 2 cm _____ | 9. radius = 7 cm; height = 14 cm _____ |
| 5. diameter = 2 yd; height = 6 yd _____ | 10. diameter = 6 yd; height = 50 yd _____ |

Directions Find the volume of a sphere with the given radius or diameter. Use the formula $V = \frac{4}{3}\pi r^3$. Use 3.14 for π .

- | | |
|----------------------------|-----------------------------|
| 11. radius = 3 cm _____ | 15. diameter = 30 cm _____ |
| 12. radius = 6 ft _____ | 16. radius = 12 ft _____ |
| 13. diameter = 48 mm _____ | 17. diameter = 21 m _____ |
| 14. radius = 9 yd _____ | 18. diameter = 15 in. _____ |

Directions Solve each problem.

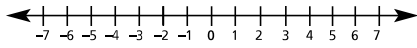
19. George filled a plastic bag with water until it had a diameter of 9 inches. What was the volume of the bag? _____
20. Lin has two boxes to choose from to mail a package to her sister in Florida. One is a rectangular box measuring 12 inches long, 9 inches high, and 10 inches wide. The other is a cylinder with a diameter of 10 inches and a height of 14 inches. She wants the larger box. Which one should she pick? Explain.
- _____

Graphing Equalities

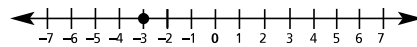
EXAMPLE

Graph the solution $x = -3$ on a number line.

Step 1 Draw a number line.



Step 2 Make a shaded circle on the number line at -3 .



Directions Graph each solution on a number line.

1. $t = 5$

5. $y = -3$

9. $s = -\frac{1}{3}$

2. $a = 3$

6. $q = -10$

10. $m = 2$

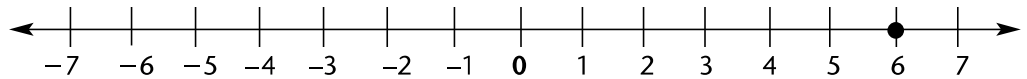
3. $d = -5$

7. $j = 6$

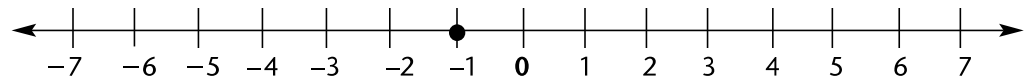
4. $x = 0$

8. $z = -2$

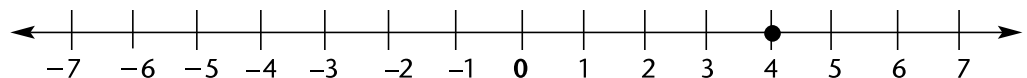
Directions Write a solution for each equality. Use x as the variable in each of the solutions.



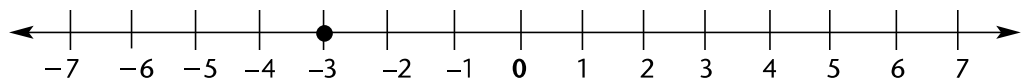
11. _____



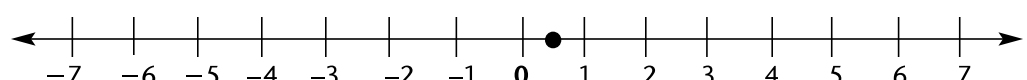
12. _____



13. _____



14. _____



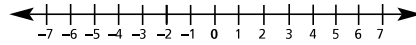
15. _____

Graphing Inequalities

EXAMPLE

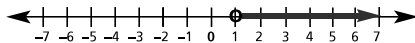
Graph the solution $y > 1$ on a number line.

Step 1 Draw a number line.



Step 2 Note that $y > 1$ means the solution is greater than 1.

Step 3 Make an open circle on 1 with a line extending right and an arrow pointing right.



Directions Graph each solution on a number line.

1. $y > 8$

5. $a \geq 6$

9. $l \neq 8$

2. $x < 4$

6. $w < -5$

10. $k \geq -3$

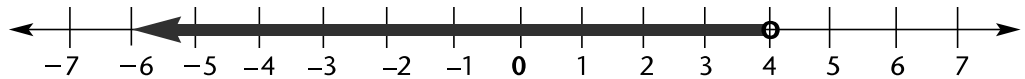
3. $t \leq -2$

7. $h > -9$

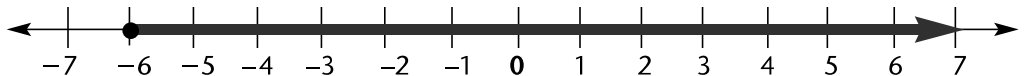
4. $s > 0$

8. $j \leq 12$

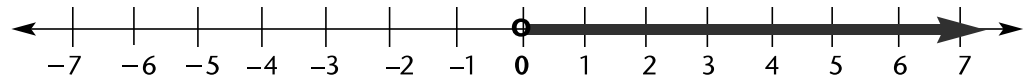
Directions Write a solution for each inequality. Use x as the variable in each of the solutions.



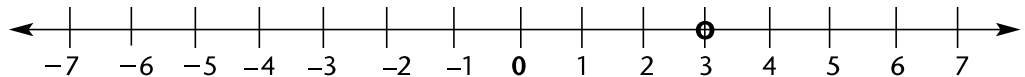
11. _____



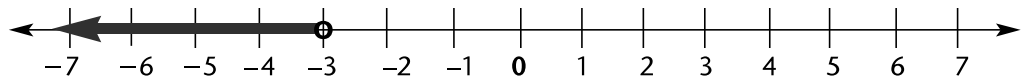
12. _____



13. _____



14. _____



15. _____

Graphing Solutions of Equalities

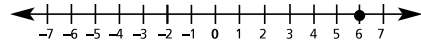
EXAMPLE

Solve $c + 4 = 10$ for c . Then graph the solution.

Step 1 Solve for c by subtracting 4 from each side of the equality.

$$c + 4 - 4 = 10 - 4 \quad c = 10 - 4 \quad c = 6$$

Step 2 Graph the solution on a number line.



Step 3 Check your work by substitution.

$$c + 4 = 10 \quad 6 + 4 = 10 \quad \text{True}$$

Directions Solve each equality for the variable. Then graph and check each solution.

- | | | | |
|-----------------|-------|-------------------|-------|
| 1. $x + 3 = 7$ | _____ | 10. $p - 3 = -5$ | _____ |
| 2. $5 + c = 4$ | _____ | 11. $y + 5 = -3$ | _____ |
| 3. $h - 3 = 0$ | _____ | 12. $t - 7 = -6$ | _____ |
| 4. $m + 6 = -3$ | _____ | 13. $a + 9 = 9$ | _____ |
| 5. $4 + j = -1$ | _____ | 14. $e - 8 = 5$ | _____ |
| 6. $s - 2 = 4$ | _____ | 15. $l - 2 = 3$ | _____ |
| 7. $g + 7 = 3$ | _____ | 16. $b + 10 = -5$ | _____ |
| 8. $7 + v = 9$ | _____ | 17. $-5 + n = -3$ | _____ |
| 9. $d - 1 = 7$ | _____ | 18. $z - 3 = 4$ | _____ |

Directions Write and solve an equality for each problem. Use x as the variable in the equality. Graph your solution on a number line.

19. Calvin sprinted 300 meters more today than yesterday. He sprinted 900 meters today. How many meters did he sprint yesterday? _____
20. Maria jumped 3 inches farther in the long jump Thursday than Friday. She jumped 6 feet 8 inches on Friday. How far did she jump on Thursday? _____

Graphing Solutions of Inequalities

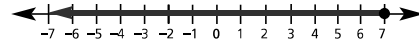
EXAMPLE

Solve $m + 3 \leq 10$ for m . Then graph the solution.

Step 1 Solve for m by subtracting 3 from each side of the inequality.

$$m + 3 - 3 \leq 10 - 3 \quad m \leq 7$$

Step 2 Graph the solution on a number line.



Step 3 Check your work by substitution.

$$7 + 3 \leq 10 \quad 10 \leq 10 \quad \text{True}$$

Directions Solve each equality or inequality for the variable. Then graph and check each solution.

- | | | | |
|---------------------|-------|---------------------|-------|
| 1. $x + 4 \leq 6$ | _____ | 13. $s - 9 > -6$ | _____ |
| 2. $p - 3 < 8$ | _____ | 14. $g + 7 \geq 9$ | _____ |
| 3. $2 + d > -2$ | _____ | 15. $n - 8 \leq -5$ | _____ |
| 4. $t - 2 > -4$ | _____ | 16. $m - 2 \geq 8$ | _____ |
| 5. $r - 6 \geq -1$ | _____ | 17. $k + 8 < 7$ | _____ |
| 6. $e + 3 < -4$ | _____ | 18. $p - 6 > 5$ | _____ |
| 7. $w - 5 \leq 6$ | _____ | 19. $w + 2 \leq -1$ | _____ |
| 8. $q + 5 \leq 2$ | _____ | 20. $4 + u > 8$ | _____ |
| 9. $a - 7 < 2$ | _____ | 21. $d - 7 < -5$ | _____ |
| 10. $b - 1 > -3$ | _____ | 22. $i - 4 \geq 1$ | _____ |
| 11. $x + 4 < -6$ | _____ | 23. $-1 + z \geq 0$ | _____ |
| 12. $2 + f \geq -4$ | _____ | | |

Directions Write and solve an inequality for each problem. Use x as the variable in the inequality. Graph your solution on a number line.

- | | |
|--|---|
| <p>24. The results of a survey taken at Washington High School showed that 6 or fewer of every 10 people said rock music was their favorite type of music. How many people did not choose rock music?</p> <p>_____</p> | <p>25. The number of students attending a home basketball game at Washington High School is always at least 25 more than the number of rows in the bleachers. There are 10 rows of bleachers. How many people attend each home game?</p> <p>_____</p> |
|--|---|

The Coordinate System—Locating Points

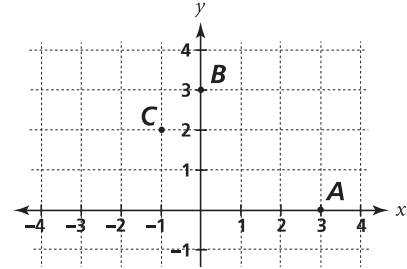
EXAMPLE

Locate points A , B , and C . Remember to always read the x -axis first, then the y -axis.

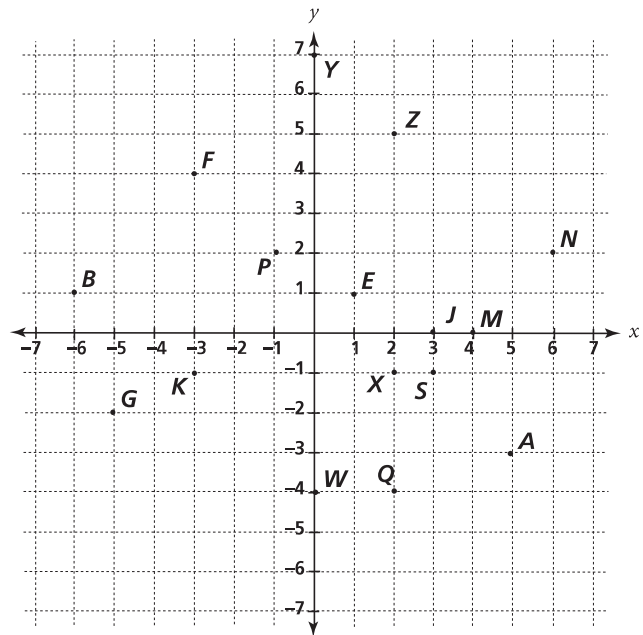
The ordered pair for Point A is $(3, 0)$.

The ordered pair for Point B is $(0, 3)$.

The ordered pair for Point C is $(-1, 2)$.



Directions Write the ordered pair that describes the location of each point.



- | | | |
|--------------------|---------------------|---------------------|
| 1. Point E _____ | 6. Point Q _____ | 11. Point M _____ |
| 2. Point J _____ | 7. Point Y _____ | 12. Point X _____ |
| 3. Point K _____ | 8. Point B _____ | 13. Point A _____ |
| 4. Point N _____ | 9. Point F _____ | 14. Point G _____ |
| 5. Point P _____ | 10. Point W _____ | 15. Point Z _____ |

Directions Identify the quadrant in which each of these points is located.

- | | | |
|---------------------|---------------------|---------------------|
| 16. Point N _____ | 18. Point B _____ | 20. Point Z _____ |
| 17. Point A _____ | 19. Point G _____ | |

The Coordinate System—Plotting Points

EXAMPLE

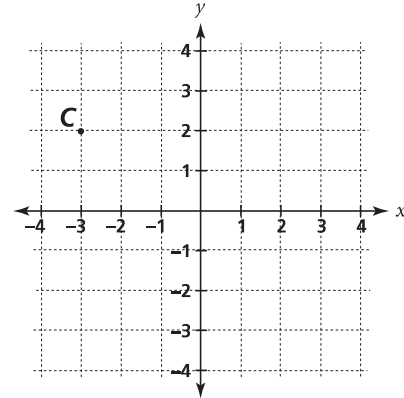
Plot a point at $(-3, 2)$. Label the point C.

Step 1 Construct a coordinate system large enough to include the ordered pair $(-3, 2)$.

Step 2 To plot $(-3, 2)$, begin at the origin $(0,0)$. Move 3 units *left* on the x -axis.

Step 3 Move 2 units up.

Step 4 Make a shaded circle at $(-3, 2)$.



Directions On a sheet of graph paper, draw a coordinate system. Then use it to plot and label each point shown in problems 1–20.

- | | | |
|-----------------------|------------------------|------------------------|
| 1. Point X $(5, 6)$ | 8. Point D $(3, -4)$ | 15. Point B $(-1, 5)$ |
| 2. Point Q $(2, -5)$ | 9. Point C $(-5, -4)$ | 16. Point Y $(-7, -8)$ |
| 3. Point A $(-5, 0)$ | 10. Point V $(0, 6)$ | 17. Point H $(-6, -7)$ |
| 4. Point W $(-1, -3)$ | 11. Point F $(-6, -3)$ | 18. Point N $(7, -6)$ |
| 5. Point S $(-2, 5)$ | 12. Point R $(-7, 5)$ | 19. Point J $(4, 4)$ |
| 6. Point Z $(1, 3)$ | 13. Point T $(5, -5)$ | 20. Point M $(2, -6)$ |
| 7. Point E $(-4, 6)$ | 14. Point G $(4, 6)$ | |

Directions Using the above points, identify the quadrant in which each point is located.

21. Point F _____
22. Point N _____
23. Point G _____
24. Point B _____
25. Point Q _____

Determining the Points of a Line

EXAMPLE

Complete the table of values for the line $y = x + 3$.

Step 1 Substitute -2 for x and solve for y .

$$y = x + 3 \quad y = -2 + 3 \quad y = 1$$

Step 2 Substitute 3 for y and solve for x .

$$y = x + 3 \quad 3 = x + 3 \quad 3 - 3 = x + 3 - 3 \quad 0 = x$$

Step 3 Substitute 4 for x and solve for y .

$$y = x + 3 \quad y = 4 + 3 \quad y = 7$$

Step 4 Complete the table of values.

$y = x + 3$	
x	y
-2	
	3
4	

$y = x + 3$	
x	y
-2	1
0	3
4	7

Directions Complete each table of values.

1.

$y = x + 5$	
x	y
-3	
2	
6	

2.

$y = x - 4$	
x	y
-2	
-1	
	-1

3.

$y = x + 7$	
x	y
-4	
	7
4	

4.

$y = x - 3$	
x	y
	1
	-3
	-5

5.

$y = x + 9$	
x	y
	6
	9
5	

6.

$y = x + 8$	
x	y
	1
0	
	10

7.

$y = x - 2$	
x	y
-1	
	1
	4

8.

$y = x + 6$	
x	y
-7	
	2
-1	

Directions Use a calculator to complete the tables of values.

9.

$y = x + 25.7$	
x	y
	18.8
-3.4	
8.7	

10.

$y = x - 12.3$	
x	y
-7.8	
	-8.2
	10.9

Tables of Values and Coordinate Systems

Directions Make a table of values for each linear equation.

1.

$y = x + 1$	
x	y

2.

$y = x - 5$	
x	y

3.

$y = x - 7$	
x	y

4.

$y = x - 1$	
x	y

5.

$y = x + 2$	
x	y

6.

$y = x + 4$	
x	y

Directions On a sheet of graph paper, draw a coordinate system with x values from -7 to 7 and y values from -7 to 7 . Suppose that the system stands for a grid to map a lake. Use it to answer these questions.

7. How far away is the sandbar $(2, 0)$ from the boat $(2, 6)$?

8. Willie drives the boat $(2, 6)$ to the sandbar $(2, 0)$ and then to the deepest part of the lake $(-4, 0)$. How far does he drive the boat?

9. Sarah swims from the end of the sandbar $(-1, 0)$ to the boat dock $(-1, -7)$. How far does she swim?

10. Zach walks along the sandbar $(2, 0)$ to the end of the sandbar $(-1, 0)$ and back again. How far does he walk?

Graphing Lines

EXAMPLE

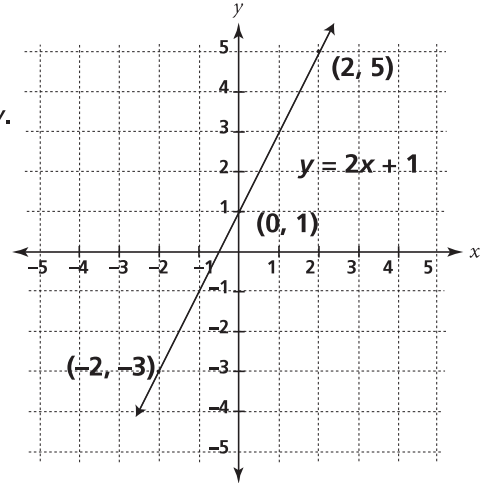
Graph the linear equation $y = 2x + 1$.

Step 1 Make a table of values.

Step 2 Choose three different values for x and solve for y .

Step 3 Draw a coordinate system and plot the points from the table of values. Connect the points, draw arrows at the ends of the line, and label the line $y = 2x + 1$.

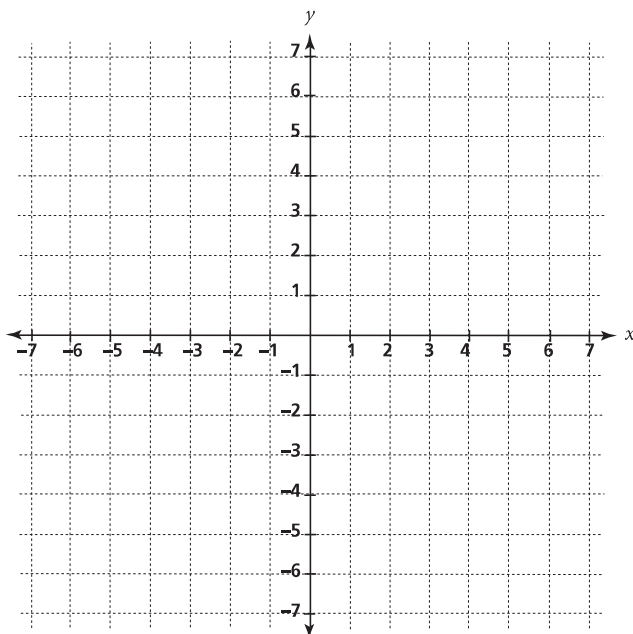
$y = 2x + 1$	
x	y
-2	-3
0	1
2	5



Directions Complete each table of values. Graph the first linear equation here and the others on graph paper.

1.

$y = x + 3$	
x	y



2.

$y = 2x + 4$	
x	y

3.

$y = x - 1$	
x	y

4.

$y = 3x$	
x	y

5.

$y = -x$	
x	y

The Slope of a Line

EXAMPLE

What is the slope of a roof that is 20 feet long and falls 5 feet in that distance?

Step 1 Express the slope as the fraction $\frac{\text{rise}}{\text{run}}$.

Step 2 $\frac{\text{rise}}{\text{run}} = \frac{-5}{+20}$

Step 3 Simplify if possible. $\frac{-5}{+20} = \frac{-1}{4}$

A slope of $\frac{-1}{4}$ means that for every 4 feet of horizontal distance, the roof falls 1 foot.

On a calculator, press $-5 \div 20$. The display shows -0.25 .

Directions In this chart, *Distance* is a horizontal measure and *Change in Elevation* is a vertical measure. Use a calculator to find each slope.

Distance	Change in Elevation	Slope
1. 8 mi	6 mi	
2. 80 ft	70 ft	
3. 63.2 yd	151.38 yd	
4. 5.2 m	-3.588 m	
5. 4.2 cm	7.686 cm	
6. 5.1 mm	0.102 mm	
7. 9 in.	-117 in.	
8. 8.1 km	18.225 km	
9. 6.6 yd	6.138 yd	
10. 24 mi	144 mi	
11. 15 m	11.55 m	
12. 13 in.	-416 in.	
13. 6.6 cm	29.04 cm	
14. -8.5 km	2.55 km	
15. 3.25 ft	-83.2 ft	

Formula for the Slope of a Line

EXAMPLE

A line passes through points (0, 0) and (2, 4). Find the slope of the line.

Step 1 Substitute the values for (x_1, y_1) and (x_2, y_2) into the formula $m = \frac{y_2 - y_1}{x_2 - x_1} = \frac{4 - 0}{2 - 0} = \frac{4}{2}$.

Remember that points (0, 0) and (2, 4) are written in the form (x_1, y_1) and (x_2, y_2) .

Step 2 Simplify. $\frac{4 - 0}{2 - 0} = \frac{4}{2} = 2$

The slope of a line passing through points (0, 0) and (2, 4) is 2.

Directions Find the slope of a line that passes through the given points.

- | | |
|------------------------------|---------------------------------|
| 1. (0, 2) and (3, 11) _____ | 10. (2, -4) and (6, 3) _____ |
| 2. (4, 12) and (-1, 7) _____ | 11. (-3, -3) and (-8, -4) _____ |
| 3. (8, 4) and (-6, -3) _____ | 12. (6, 2) and (3, 8) _____ |
| 4. (4, 2) and (-8, -1) _____ | 13. (0, 1) and (5, 7) _____ |
| 5. (5, 4) and (7, -2) _____ | 14. (-3, 0) and (1, 8) _____ |
| 6. (-1, 8) and (5, 8) _____ | 15. (1, 1) and (5, 9) _____ |
| 7. (3, 1) and (2, 5) _____ | 16. (5, 3) and (9, 2) _____ |
| 8. (7, 9) and (-5, -1) _____ | 17. (3, -3) and (4, -5) _____ |
| 9. (7, 8) and (0, 3) _____ | |

Directions Answer each question.

18. In a soapbox derby, the first part of a hill has a slope of $\frac{-5}{25}$ and the second part of the hill has a slope of $\frac{-4}{16}$. Which part of the hill has the steeper slope? Explain. _____
19. A bicycle trail has two slopes. The first slope is $\frac{-3}{20}$ and the second slope is $\frac{5}{15}$. Which is the easier to ride? Explain. _____
20. Tae wants to exercise by jogging up a hill. One hill has a slope of $\frac{3}{20}$. Another hill has a slope of $\frac{6}{40}$. Which hill will be more difficult to jog up? Explain. _____

The Slope-Intercept Form of a Line

EXAMPLE

Find the slope, x -intercept, and y -intercept of the line $2y = 6x + 4$.

Step 1 Write $2y = 6x + 4$ in the slope-intercept form by solving for y .

$$\frac{2y}{2} = \frac{6x}{2} + \frac{4}{2} \quad y = 3x + 2$$

Step 2 Determine the slope by looking at the form $y = mx + b$.

$$y = 3x + 2 \quad \text{The slope is 3, since it corresponds to } m.$$

Step 3 Determine the y -intercept by looking at the form $y = mx + b$.

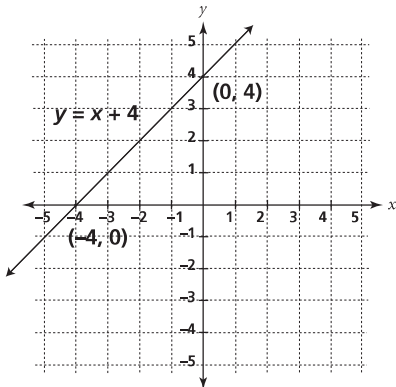
$$y = 3x + 2 \quad \text{The } y\text{-intercept is 2, since it corresponds to } b.$$

Step 4 Determine the x -intercept by substituting 0 for y and solving for x .

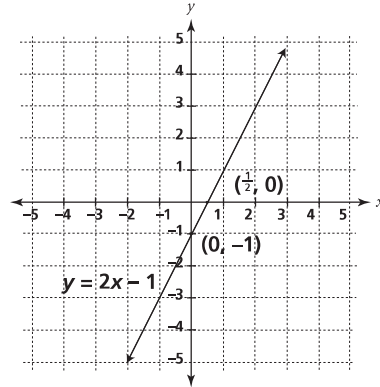
$$y = 3x + 2 \quad 0 = 3x + 2 \quad -3x = 2 \quad x = \frac{-2}{3} \quad \text{The } x\text{-intercept of the line is } \frac{-2}{3}.$$

Directions Identify the slope, x -intercept, and y -intercept of each line.

1.



2.



Directions Write each of these linear equations in slope-intercept form.

3. $4y = 8x + 20$ _____

6. $-3y = 6x + 3$ _____

4. $-y = -x + 8$ _____

7. $4y = 4x - 28$ _____

5. $2y = -6x + 6$ _____

8. $-2y = 2x - 1$ _____

Directions Find the slope, x -intercept, and y -intercept of each line.

9. $y = x - 5$ _____

13. $y = 4x + 1$ _____

10. $y = 2x + 4$ _____

14. $2y = -2x + 6$ _____

11. $y = -3x - 1$ _____

15. $-3y = 6x - 15$ _____

12. $y = x - 2$ _____

Angles and Angle Measures

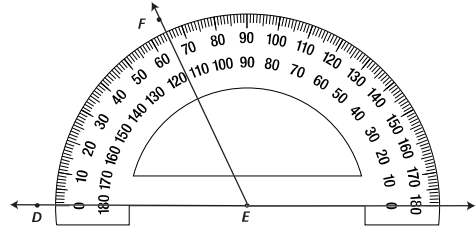
EXAMPLE

Find the measure of $\angle DEF$.

Step 1 Place the center of the protractor at the vertex of the angle.

Step 2 Place the 0° line of the protractor along one of the rays in the angle.

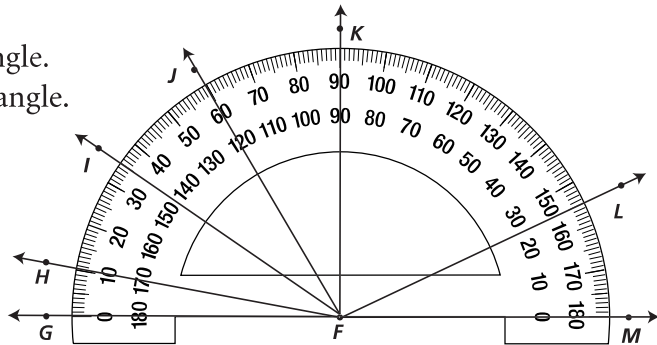
Step 3 Read the measure of the angle, counting up from 0° . The measure of $\angle DEF = 65^\circ$.



Directions Use the illustration at the right.

Name the rays that make each angle.

Then write the measure of each angle.



Angle

Rays

Measure

1. GFH

2. GFI

3. GFJ

4. GFK

5. GFL

Angle

Rays

Measure

6. LFM

7. KFM

8. JFM

9. IFM

10. HFM

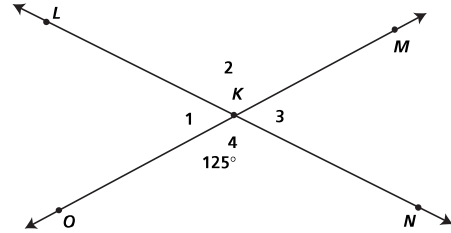
Identifying and Classifying Angles

EXAMPLE

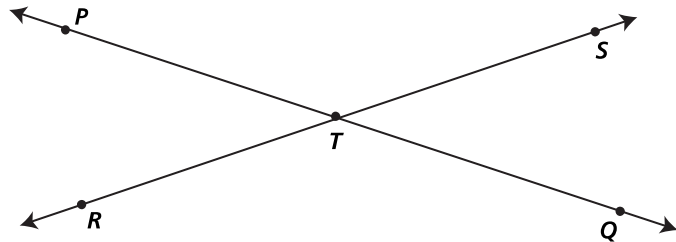
Name two angles adjacent to $\angle LKO$.
Name the angle that is vertical to $\angle 1$.

$\angle OKN$ and $\angle LKM$ are adjacent to $\angle LKO$ because they have point K as their vertex and a common side (LK or OK).

$\angle 1$ and $\angle 3$ are vertical angles, because $\angle 3$ is opposite $\angle 1$.



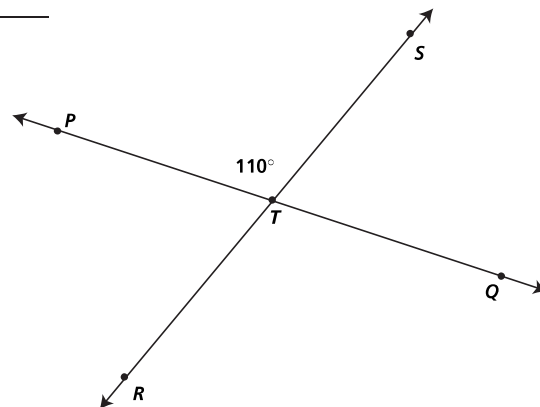
Directions Identify these angles.
Write *adjacent*, *vertical*, *acute*, or *obtuse*. Some angles may have more than one description.



1. $\angle PTS$ and $\angle RTQ$ _____
2. $\angle PTS$ and $\angle STQ$ _____
3. $\angle PTS$ _____
4. $\angle PTR$ _____
5. $\angle RTP$ and $\angle PTS$ _____
6. $\angle RTP$ and $\angle STQ$ _____
7. $\angle QTS$ _____
8. $\angle RTQ$ _____

Directions Find the measures.

9. $m\angle STQ$ _____
10. $m\angle RTQ$ _____



Complementary and Supplementary Angles

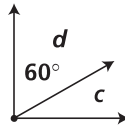
EXAMPLE

If the sum of the measures of two angles is 90° , the angles are complementary. Angles c and d are complementary. Write an equation to find $m\angle c$.

$$m\angle c + 60^\circ = 90^\circ$$

$$m\angle c = 90^\circ - 60^\circ$$

$$m\angle c = 30^\circ$$



Directions $\angle x$ and $\angle y$ are complementary. Write an equation to find the measure of $\angle y$.

- $m\angle x = 50^\circ$ _____
- $m\angle x = 20^\circ$ _____
- $m\angle x = 45^\circ$ _____
- $m\angle x = 30^\circ$ _____

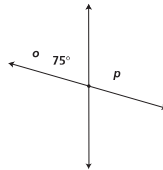
EXAMPLE

If the sum of the measures of two angles is 180° , the angles are supplementary. Angles o and p are supplementary. Write an equation to find $m\angle p$.

$$m\angle p + 75^\circ = 180^\circ$$

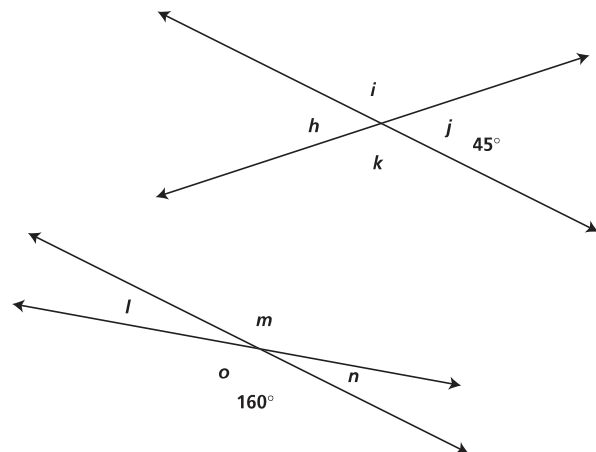
$$m\angle p = 180^\circ - 75^\circ$$

$$m\angle p = 105^\circ$$



Directions Find the measures.

- What is the measure of $\angle h$? _____
- What is the measure of $\angle k$? _____
- What is the measure of $\angle i$? _____
- What is the measure of $\angle m$? _____
- What is the measure of $\angle l$? _____
- What is the measure of $\angle n$? _____



Angle Measure in a Triangle

EXAMPLE

Write an equation to find the missing measure.

$$m\angle KLM + 70^\circ = 180^\circ$$

$$m\angle KLM = 180^\circ - 70^\circ$$

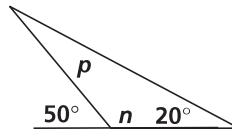
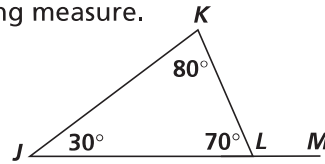
$$m\angle KLM = 110^\circ$$

Find $m\angle p$.

$$n = 180^\circ - 50^\circ$$

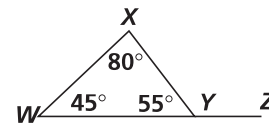
$$n = 130^\circ$$

$$130^\circ + 20^\circ + p = 180^\circ \quad p = 30^\circ$$

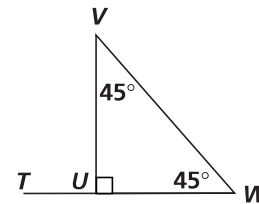


Directions Write an equation to find the missing measure.

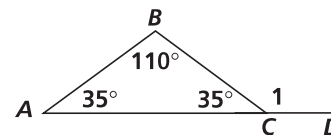
1. $m\angle XYZ$ _____



2. $m\angle TUV$ _____



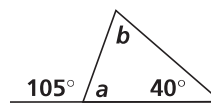
3. $m\angle 1$ _____



Directions Find the measures.

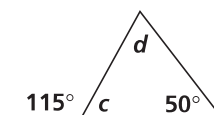
4. $m\angle a$ _____

$m\angle b$ _____



5. $m\angle c$ _____

$m\angle d$ _____

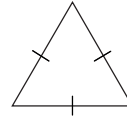


Naming Triangles

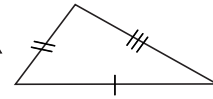
EXAMPLE

Tick marks show whether sides have the same or different lengths.

This triangle has 3 sides of the same length.

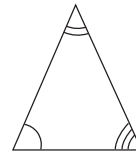


This triangle has sides of 3 different lengths.

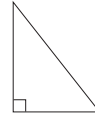


Arcs show whether angles are the same or different.

This triangle has angles with 3 different measures.

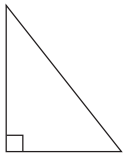


A square is used to show a 90° angle.

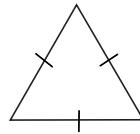


Directions Write the name of each triangle. Some triangles may have more than one name.

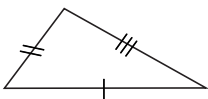
1.



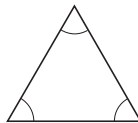
2.



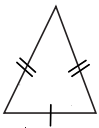
3.



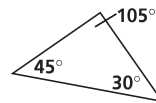
4.



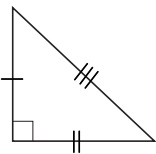
5.



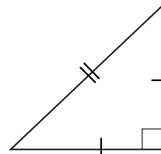
6.



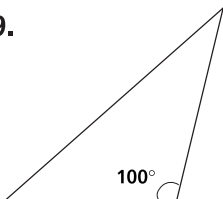
7.



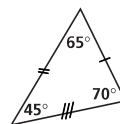
8.



9.



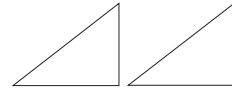
10.



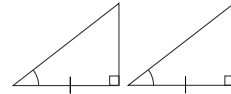
Congruent Triangles

EXAMPLE

Are these 2 triangles congruent?
Measure the sides and angles of both triangles.

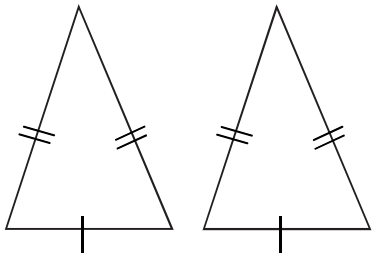


Label the sides and angles that match. Because the triangles have 2 angles and an included side that are equal, they are congruent. (ASA)

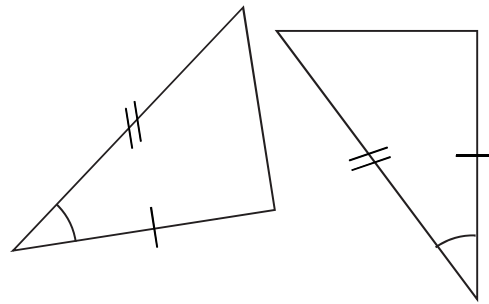


Directions Are the triangles in each pair congruent? Tell why or why not.

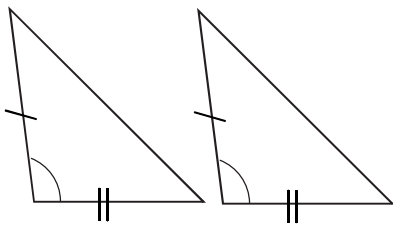
1.



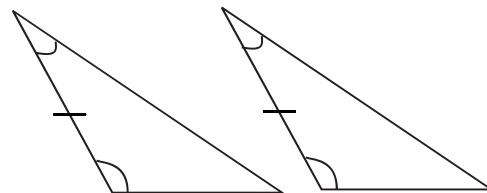
2.



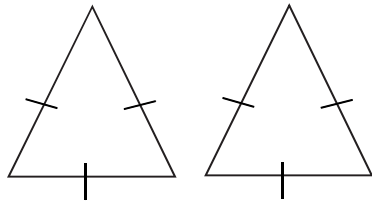
3.



4.



5.



Similar Triangles

EXAMPLE

$\triangle PLM \sim \triangle PNO$. Study the measurements given. Find $m\angle N$ and $m\angle L$.
Find the length of \overline{PO} .

Step 1 The triangles are similar so the two angles will have the same measurement.

Step 2 $m\angle L + 75^\circ + 45^\circ = 180^\circ$

$$m\angle L = 180^\circ - 75^\circ - 45^\circ \qquad m\angle L = 60^\circ$$

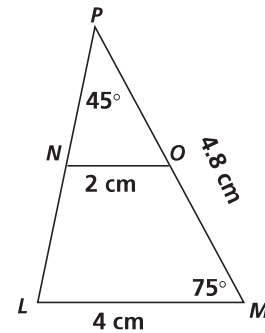
$$m\angle N = 60^\circ$$

Step 3 The triangles are similar so the corresponding sides form equal ratios.

Step 4 $\frac{LM}{NO} = \frac{PM}{PO}$

$$\frac{4}{2} = \frac{4.8}{PO} \qquad PO = 4.8\left(\frac{2}{4}\right)$$

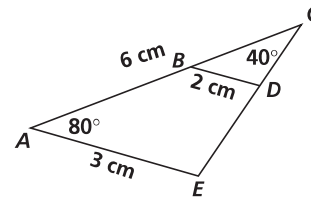
$$PO = 2.4 \text{ cm}$$



Directions Study the illustrations. Find the measures.

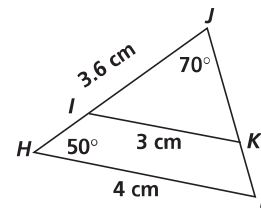
1. $m\angle D$ _____

2. m of \overline{CB} _____

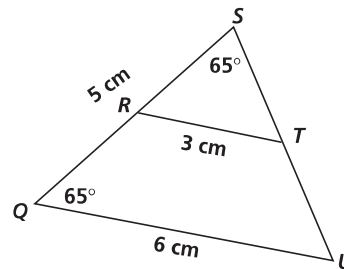


3. $m\angle K$ _____

4. m of \overline{IJ} _____



5. $m\angle T$ _____



Parallelograms

EXAMPLE

Describe the properties of this quadrilateral. Then name it.

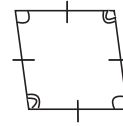
All sides are the same length.

It has 2 pairs of parallel sides.

The opposite sides are the same length.

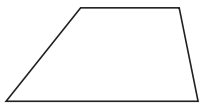
The opposite angles are equal.

It is a rhombus.

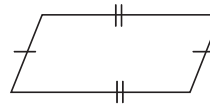


Directions Name 2 properties of each figure. Then name the figure.

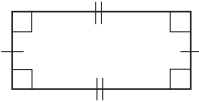
1.



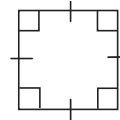
2.



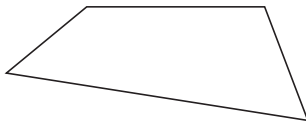
3.



4.



5.



6.



Directions Tell whether each statement is *true* or *false*.

7. A rhombus is also a parallelogram. _____
8. A parallelogram is also a quadrilateral. _____
9. A trapezoid is also a rhombus. _____
10. A square is also a rectangle. _____

Quadrilaterals and Diagonals

EXAMPLE

Use the Pythagorean theorem to find the length of the diagonal.
Use a scientific calculator and round your answer to the nearest hundredth.

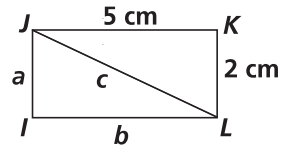
$$a^2 + b^2 = c^2$$

$$2^2 + 5^2 = c^2$$

$$4 + 25 = c^2$$

$$\sqrt{29} = c$$

$$5.39 = c$$

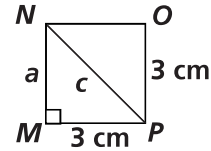


Directions Answer the questions about these rectangles. Use a scientific calculator and round your answer to the nearest hundredth.

1. What is the length of MN ? _____

2. Use the Pythagorean theorem to find c . _____

3. Is $\triangle NMP$ congruent to $\triangle NPO$? _____

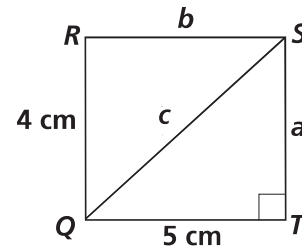


4. What is the $m\angle R$? Explain. _____

5. What is the length of ST ? _____

6. Find the length of SQ . _____

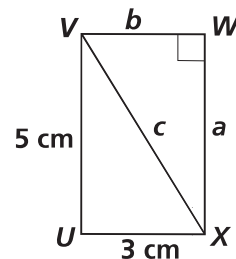
7. What would be the length of RT ? _____



8. What is the length of VW ? _____

9. What is $m\angle VUX$? _____

10. Is $\triangle VUX$ congruent to $\triangle VXW$? _____



Polygons and Diagonals

EXAMPLE

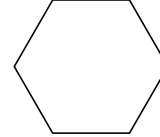
Find the sum of the measures of the angles and the measure of each interior and exterior angle.

To find the sum of all the angle measures in a regular hexagon:

$$(6 - 2)180^\circ = a$$

$$(4)180^\circ = a$$

$$720^\circ = a$$



To find the measure of each interior angle:

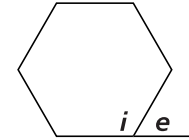
$$\frac{720^\circ}{6} = 120^\circ$$

To find the measure of each exterior angle:

$$120^\circ + e = 180^\circ$$

$$e = 180^\circ - 120^\circ$$

$$e = 60^\circ$$

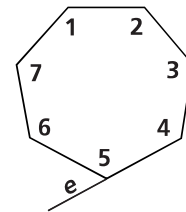


Directions Find the measures of these regular polygons.

1. $m\angle 6$

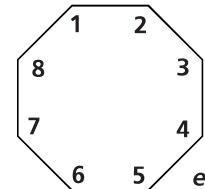
2. $m\angle e$

3. The sum of all interior angles



4. $m\angle 8$

5. $m\angle e$

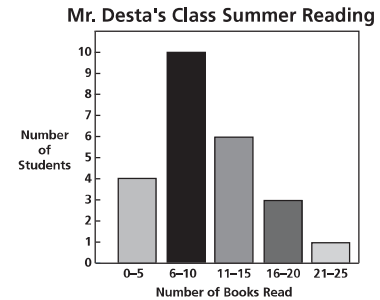


Bar Graphs

EXAMPLE

A bar graph uses rectangular bars to organize and display data. It is made up of these individual parts:

- a title
- a horizontal axis with labels
- a vertical axis with labels
- an interval
- data



Directions Suppose you were asked to construct a bar graph that organizes and displays the data shown in this table. The table shows the results of a class election for president.

Election Results	
Candidate A	10 votes
Candidate B	12 votes
Candidate C	4 votes

1. What title would you choose for the bar graph?

2. What label would you choose for the horizontal axis?

3. What label would you choose for the vertical axis?

4. What interval would you use? Explain.

5. Use your answers from problems 1–4 to construct a bar graph for the data on your own paper.

Circle Graphs

EXAMPLE

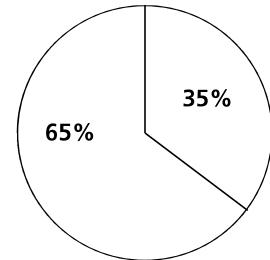
A circle graph uses parts of a circle to organize and display data.

The part of this graph labeled 65% makes up 234° of the graph because 65% of $360^\circ = 0.65 \cdot 360^\circ = 234^\circ$.

The part of this graph labeled 35% makes up 126° of the graph because 35% of $360^\circ = 0.35 \cdot 360^\circ = 126^\circ$.

You can check your work by finding the sum of the parts.

$$234^\circ + 126^\circ = 360^\circ \quad \checkmark$$



Directions Study this circle graph. Answer the questions that follow.

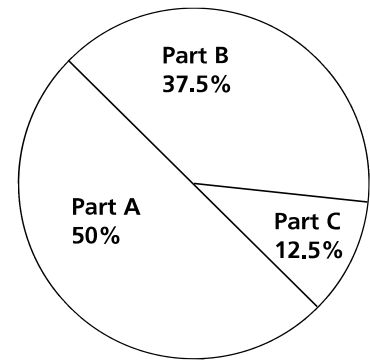
1. Name the fraction in simplest form, the decimal, and the number of degrees that represent Part A of the graph.

2. Name the fraction in simplest form, the decimal, and the number of degrees that represent Part B of the graph.

3. Name the fraction in simplest form, the decimal, and the number of degrees that represent Part C of the graph.

4. Describe how a circle graph can be checked for accuracy.

5. In the graph, suppose that Part A represents 500 votes. How many votes altogether are represented by the graph?



Frequency Tables

EXAMPLE

Suppose two 1–6 number cubes are tossed at the same time and the outcomes of the cubes are added to create a sum.

For example, if the outcome on the first cube is 3 and the outcome on the second cube is 4, the sum of the outcomes is $3 + 4$ or 7.

This frequency table shows the number of different ways various sums can be made by tossing two 1–6 number cubes.

Outcome Sum	Tally	Frequency
2		1
3		2
4		3
5		4
6	+	5
7	+	6
8	+	5
9		4
10		3
11		2
12		1

Directions Answer these questions about the frequency table in the example.

1. What is the greatest possible sum that can be created by tossing two 1–6 number cubes? Explain how that sum can be created.

2. What is the least possible sum that can be created by tossing two 1–6 number cubes? Explain how that sum can be created.

3. How many tosses of the number cubes are shown in the data? Tell how you know.

4. Based on the data, which sum will occur most often when two 1–6 number cubes are tossed? Which sums will occur least often?

5. What interval was used to create this frequency table? Is there a better interval that could have been used? Explain.

Mean

EXAMPLE

Study the data shown in the table. The data show the average amount of precipitation received each month in Miami, Florida.

Month	Precipitation in Inches	Month	Precipitation in Inches
January	2.0	July	5.7
February	2.1	August	7.6
March	2.4	September	7.6
April	2.9	October	5.6
May	6.2	November	2.7
June	9.3	December	1.8

To find the mean of a set of data, find the sum of the data values in the set, then divide by the number of data values.

Directions Answer these questions about the data table in the example.

1. What useful information do the labels in the table provide?

2. How many data values does the set of data contain? _____

3. What is the sum of the data values? _____

4. Identify the steps to follow to determine the mean of the set of data.

5. What is the mean amount of precipitation received each month in Miami, Florida? Round your answer to the nearest hundredth inch.

Median

EXAMPLE

Study the data shown in the table. The data show the inauguration ages of some U.S. presidents.

The median of a set of data is the middle value when the set is ordered from greatest to least or least to greatest. To find the mean of a set of data, order the values in the set from greatest to least or least to greatest. Cross off the greatest and least values in the set. The median is the middle data value, or the mean of the two middle values.

President	Inauguration Age (in years)
Washington	57
Jefferson	57
Lincoln	52
Harrison	55
Cleveland	55
McKinley	54
Wilson	56
Hoover	54
L. Johnson	55
Carter	52

Directions Answer these questions about the data table in the example.

1. Order the data values from greatest to least or from least to greatest.

2. Does the set of data have an even number or an odd number of data values?

3. How is finding the median of a data set with an even number of values different from finding the median of a data set with an odd number of values?

4. What is the median inauguration age of the presidents shown in the table?

5. President Bill Clinton was 46 years old at inauguration, and President Truman was 60 years old. Suppose these two presidents were added to the table. Would the median change? If so, to what?

Mode

EXAMPLE

Study the data shown in the table. The data show elevation in feet above sea level of selected U.S. cities.

The mode of a set of data is the value or values that occur most often. To determine the mode of a set of data, count the number of times each value appears. The value or values that appear most often are the mode.

City	Elevation Above Sea Level (in feet)
San Diego, CA	20
Bellingham, WA	60
Galveston, TX	5
Cambridge, MA	20
Orlando, FL	70
Wilmington, NC	35
New Haven, CT	40
Baltimore, MD	20
Key West, FL	5
Albany, NY	20

Directions Answer these questions about the data table in the example.

1. What useful information do the labels in the table provide?

2. How many different data values appear in the table? What are those values?

3. How could you determine the mode of the data?

4. What is the mode of the data?

5. Suppose each value in a set of data occurs the same number of times. What is the mode of the set of data?

Range

EXAMPLE

Study the data shown in the table. The data show the lengths in miles of selected rivers in North America.

The range of a set of data is the difference between the greatest and least values.

River	Length (miles)
Missouri	2,315
Kentucky	259
Arkansas	1,459
Milk	625
Porcupine	569
Snake	1,038
Mississippi	2,340
White	722
Yukon	1,979
Pecos	926

Directions Answer these questions about the data table in the example.

1. What is the longest river shown in the table? What is its length?

2. What is the shortest river shown in the table? What is its length?

3. How could you determine the range of the data?

4. What is the range of the data?

5. In order to find the range of a set of data, is it necessary to order data in a set from greatest to least or from least to greatest? Explain.

Data and Statistics

EXAMPLE

Study the data shown in this table. The data show the locations and heights in feet of famous waterfalls.

Waterfall	Location	Height (in feet)
Panther	Alberta, Canada	600
Multnomah	Oregon, U.S.	620
Augrabies	South Africa	480
Feather	California, U.S.	640
Marina	Guyana	500
Bridalveil	Yosemite National Park, U.S.	620

Directions Answer these questions about the data table in the example.

1. What data are represented in the table? _____
2. How many data values does the table display? _____
3. Suppose you were asked to display the data using a bar graph. What interval would you use? Explain.

4. When should you break the vertical axis of a bar graph? Explain.

5. Would it be easy or difficult to display the waterfall data in a circle graph? Tell why.

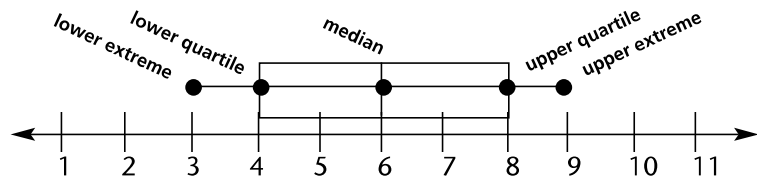
6. Is a frequency table the best way to organize and display the data in the table? Tell why or why not.

7. Find the mean of the data. Round your answer to the nearest whole number. _____
8. Find the median of the data. _____
9. Find the mode of the data. _____
10. Find the range of the data. _____

Box-and-Whiskers Plots

EXAMPLE

Study the data shown in this box-and-whiskers plot.



To construct a box-and-whiskers plot:

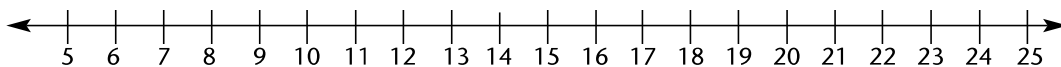
- Find the median of the entire set of data. Label this value *median*.
- Find the median of all values below the median. Label this value *lower quartile*.
- Find the median of all values above the median. Label this value *upper quartile*.
- Find the least value in the set of data. Label this value *lower extreme*.
- Find the greatest value in the set of data. Label this value *upper extreme*.

Directions Use the set of data shown below for problems 1–5.

{16 19 11 23 15 18 22 17 10 12 21}

1. Order the data in the set from greatest to least or from least to greatest.

2. What is the median of the set of data? _____
3. What value represents the lower quartile? _____ The upper quartile? _____
4. What value represents the lower extreme? _____ The upper extreme? _____
5. Construct a box-and-whiskers plot of the data using this number line.



The Probability Fraction

EXAMPLE

Consider the frequency table that shows the number of different ways various sums can be made by tossing two 1–6 number cubes.

When two 1–6 number cubes are tossed at the same time, 36 different outcomes are possible.

Outcome Sum	Tally	Frequency
2		1
3		2
4		3
5		4
6	+	5
7	+	6
8	+	5
9		4
10		3
11		2
12		1

Directions Use the probability fraction $P = \frac{\text{number of favorable outcomes}}{\text{number of possible outcomes}}$ and the frequency table to find each of the following probabilities. Whenever possible, express your answer in simplest form.

1. $P(10)$ _____

5. $P(\text{an even sum})$ _____

2. $P(5)$ _____

6. $P(\text{an odd sum})$ _____

3. $P(3)$ _____

4. $P(12)$ _____

7. Which outcome shown in the table is most likely? _____

8. Which outcomes are least likely? _____

9. Which outcome is twice as likely as an outcome of 4? _____

Which outcomes are $\frac{1}{3}$ as likely as an outcome of 7? _____

10. Some board games require a player to roll two number cubes. How might knowing the probability of which sums are more likely to occur help you become a better board game player?

The Fundamental Principle of Counting

EXAMPLE

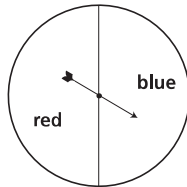
These combinations show all of the different ways the letters a , b , and c can be arranged if the letters cannot be used more than once in any arrangement.

abc acb bac bca cab cba

Another way to determine the number of different ways the letters can be arranged is to use the fundamental principle of counting. It states that three letters can be arranged $3 \cdot 2 \cdot 1$ or 6 different ways.

Directions Use the fundamental principle of counting or draw a diagram to determine the number of arrangements in each of the following problems.

- How many different ways can two students seat themselves in two chairs? _____
- How many different four-digit whole numbers can be made using the digits 1, 3, 5, and 7 if the digits can appear only once in each number? _____
- Angela is choosing a skirt and a blouse to wear from five skirts and four blouses. How many different combinations of one skirt and one blouse does Angela have to choose from? _____
- Suppose the 1–6 number cube and the spinner shown below are each used once. How many different outcomes are possible? _____



- How many different three-digit numbers are possible when each spinner shown below is spun once? The left spinner will provide the first digit of the number, the center spinner will provide the second digit, and the right spinner will provide the third digit. _____

